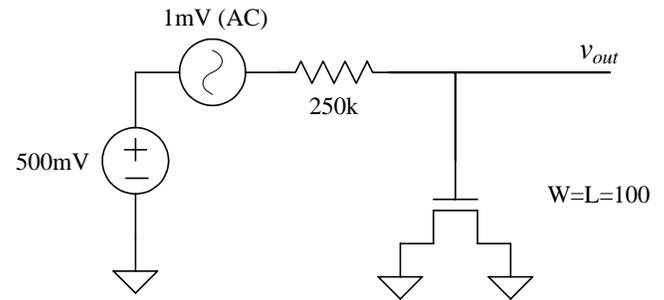


- 6.1) Plot the magnitude and phase of  $v_{out}$  (AC) in the following circuit, Fig. 6.20. Assume that the MOSFET was fabricated using the 50nm process (see Table 5.1) and is operating in strong inversion. Verify your answer with SPICE.

Sol: -From Fig. 6.20



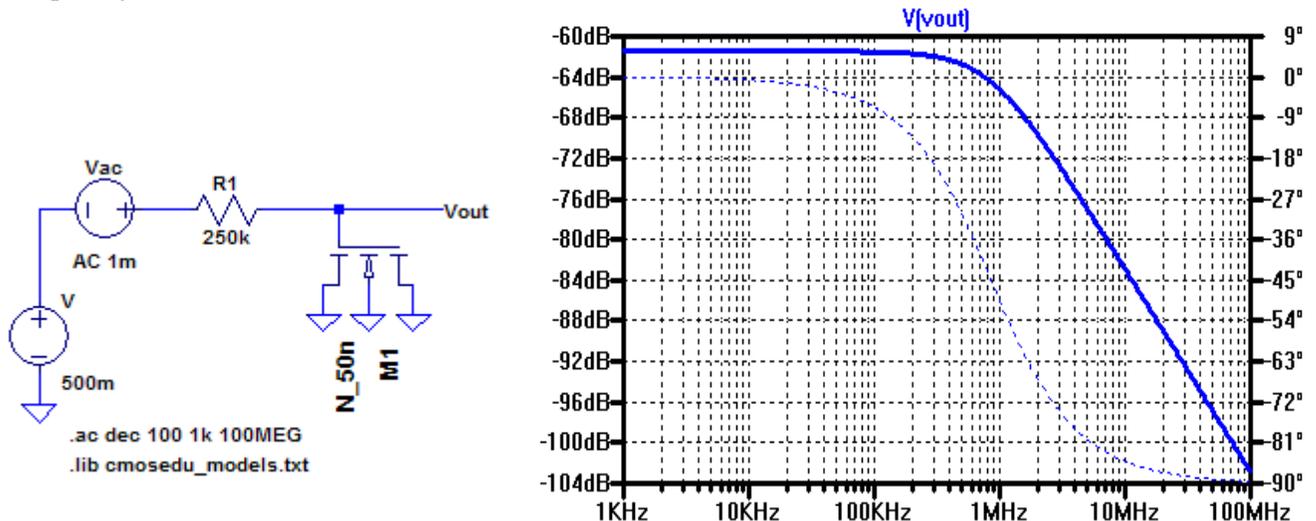
MOSFET is operating in strong inversion region and source, drain and body are connected to ground (body connection not shown). The device acts as MOSCAP, value of this capacitance can be calculated with the help of table 5.1 for 50nm process.

$$C_{total} = C'_{ox} \times W \times L = 25fF/\mu m^2 \times (100 \times 50nm) \times (100 \times 50nm) = 25fF/\mu m^2 \times 25 \mu m^2; C_{total} = 625fF$$

For 1mV AC input the circuit functions as low pass RC circuit with voltage divider equation given as :-

$$V_{out} = V_{in} \left[ \frac{1/j2\pi fC_{total}}{R + 1/j2\pi fC_{total}} \right] = \frac{V_{in}}{1 + j2\pi fRC_{total}}; |V_{out}| = \frac{V_{in}}{\sqrt{1 + (2\pi fRC_{total})^2}}; \angle V_{out} = -\tan^{-1}(2\pi fRC_{total})$$

3db frequency for this case will be  $f_{3db} = \frac{1}{2\pi RC_{total}} \approx 1MHz$  thus simulating the circuit from frequency of 1 kHz to 100MHz



In the above simulation plot we can see the RC response of the circuit. The magnitude plot is at approximately -60 db due to the fact that  $V_{in}$  taken as 1mV which will be equal to -60db. Also at the 1MHz the phase is approximately  $45^\circ$  and magnitude around -63db.

**Problem 6.2****Rupa Balan**

**If a MOSFET is used as a capacitor in the strong inversion region where the gate is one electrode and the source/drain is the other electrode, does the gate overlap of the source/drain change the capacitance? Why? What is the capacitance?**

**Solution:-** In the strong inversion region, the channel of electrons is formed below the gate oxide in case of NMOS shorting the drain and the source.

Since source and drain of NMOS are shorted through channel of electrons, gate overlap of source/drain does not change the gate to source/drain capacitance.

Capacitance between gate and source/drain  $= C_{ox} = C'_{ox} \cdot W \cdot L \cdot (\text{scale})^2$

where  $W = W_{\text{drawn}}$  and  $L = L_{\text{drawn}}$ .

**Problem 6.3****Krishna Duvvada**

**Repeat problem 6.2 when the MOSFET is operating in the accumulation region. Keep in mind that the question is not asking for the capacitance from gate to substrate.**

**Solution:-** When the MOSFET operates in the accumulation region, the gate overlap capacitance affects the capacitance from gate to source/drain. Here the drain and source is separated by the substrate which is the resistance. So the gate to drain/source capacitance is the overlap capacitance.

$$C_{gs} = C'_{ox} \cdot L_{\text{diff}} \cdot W \cdot (\text{scale})^2$$

**Problem 6.4****Surendranath C Eruvuru**

**If the oxide thickness of a MOSFET is 40 Å. What is  $C'_{ox}$ ?**

**Solution:-**  $C'_{ox} = \epsilon_{ox} / T_{ox} = (8.85 \times 3.97 \text{ aF}/\mu\text{m}) / (40 \times 10^{-10} \text{ m}) = \underline{8.784 \text{ fF}/\mu\text{m}^2}$

KRISHNAMRAJU KURRA

**Problem 6.5. Repeat Ex: 6.5 to get a threshold voltage of 0.8V.**

**Solution:** Given  $V_{GS} = V_{THN}$  and  $V_{SB} = 1V$

Then  $V_S = -V_{fp} + V_{SB}$

Where  $V_{fp} = -(KT/q) \ln (N_A/n_i)$

$$= -26 \text{ mV} * \ln [10^{15} (\text{atoms/cm}^3) / 1.45 * 10^{10} (\text{atoms/cm}^3) ]$$

$$= -290\text{mV}$$

We have  $X_d = \sqrt{[2 \times \epsilon_{si} \times |-2V_{fp} + V_{SB}| / qN_A]$

=

$$\sqrt{[2 \times 11.7 \times 8.85 \times 10^{-18} (F / \mu m^2) \times |(-2 \times -0.29) + 1| V / (1.6 \times 10^{-19} (C / atom)) \times 10^{15} (atoms / cm^3) (cm^3 / 10^{12} \mu m^3)]}$$

$$= 1.43 \mu m$$

We have  $Q'_{bo} = q \times N_A \times X_d$

$$= (1.6 \times 10^{-19} (C / atom)) \times 10^{15} (atoms / cm^3) (cm^3 / 10^{12} \mu m^3) \times 1.43 \mu m$$

$$= 229 \text{ aC} / \mu m^2$$

**PROBLEM 6.6**

**Indira Priyadarshini.Vemula**

**Repeat Ex. 6.3 for a p-channel device with a well doping concentration of  $10^{16}$  atoms/cm<sup>3</sup>?**

**Solution:**

Given  $N_D = 10^{16}$  atom/cm<sup>3</sup>

$$\gamma = (2q \epsilon_{si} N_D)^{1/2} / C_{ox}$$

$$\gamma = \frac{(2 * 1.6 * 10^{-19} C/atom * 11.7 * 8.85 \text{ aF}/\mu m^2 * 10^{16} \text{ atom}/\text{cm}^3 * \text{cm}^3 / 10^{12} \mu m^2)^{1/2}}{1.75 \text{ fF}/\mu m^2}$$

$$\gamma = 0.328 \text{ V}^{1/2}$$

**Problem 6.7****MESHACK P. APPIKATLA****What is the electrostatic potential of the oxide-semiconductor interface when**

$$V_{GS}=V_{THNO}.$$

**Solution:** It will be equal and opposite to the electrostatic potential of the substrate.

$$V_s = -V_{fp}$$

Where  $V_s$  is the electrostatic potential of the interface and  $V_{fp}$  is the electrostatic potential of the substrate.**Problem 6.8****Edward Kunz****Estimate the ion implant dose required to change the threshold voltage in Ex. 6.4 without Sodium contamination, to 0.8v.****Solution:** Using values from Ex. 6.4

$$V_{THNO} = -0.220v + \frac{qN_I}{C'_{OX}} = 0.8v$$

$$C'_{OX} = 1.75 \frac{fF}{\mu m^2}$$

$$q = 1.6 * 10^{-19} \frac{C}{atom}$$

$$0.8v = -0.220v + \frac{1.6 * 10^{-19} \frac{C}{atom} * N_I}{1.75 \frac{fF}{\mu m^2}}$$

$$N_I = 1.115 * 10^{12} \frac{atoms}{cm^2}$$

**Problem 6.9**

Vinay Dindi

**What happens to the threshold voltage in Problem 6.8 if sodium contamination of  $100 \times 10^9$  sodium ions/cm<sup>2</sup> is present at the oxide-semiconductor interface?**

**Solution:** Given  $N_i = 100 \times 10^9$  atoms/cm<sup>2</sup> = 1000 atoms/μm<sup>2</sup>

From Eq (6.22) and (6.23) and the results from Ex.6.4

$$V_{thno} = -220\text{mV} - qN_s/C'_{ox} + qN_i/C'_{ox}$$

From Prob 6.8), we know  $-220\text{mV} + qN_i/C'_{ox} = 0.8$

$$\text{So, } V_{thno} \text{ with sodium contamination} = 0.8 - (1.6 \times 10^{-19} \times 1000 / 1.75 \text{fF}) = 0.7$$

**Problem 6.10**

Satish Dulam

**How much charge (enhanced electrons) is available under the gate for conducting a drain current at the drain-channel interface when  $V_{ds} = V_{gs} - V_{thn}$ ? Why? Assume the MOSFET is operating in strong inversion,  $V_{gs} > V_{thn}$ .**

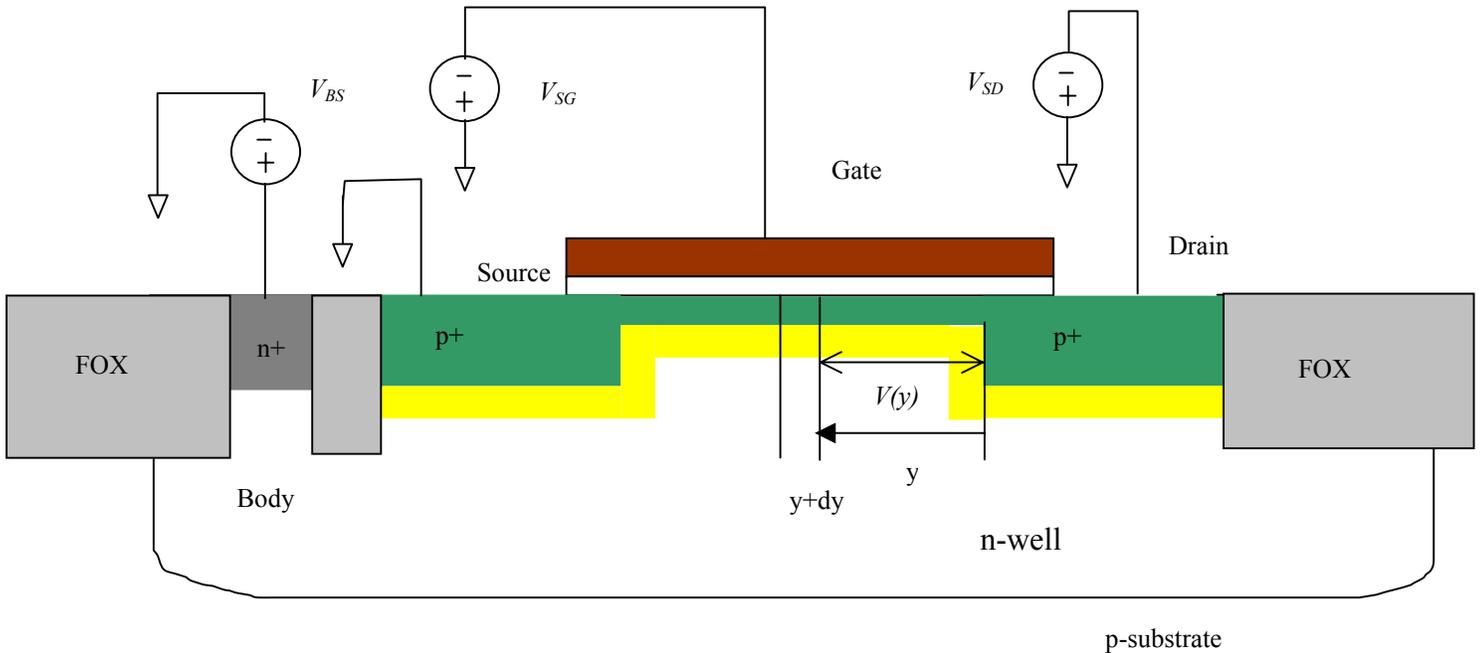
**Solution:** In Strong inversion, the amount of charge present at any point in the channel is given by Eq 6.28. At the drain,  $V(y)$  is equal to  $V_{ds}$ . Given that  $V_{ds}$  is  $V_{gs} - V_{thn}$ . From Eq 6.28, the charge at the drain is zero. When the drain and source are held at ground and the gate voltage is greater than the  $V_{thn}$ , the MOS is already in strong inversion and the channel is uniform along the  $y$ -direction. As the drain voltage is increased, the positive voltage at the drain is removing the electrons from the inverted channel. When the drain voltage reaches  $(V_{gs} - V_{thn})$ , the net charge present at the drain is zero.

Show the details of the derivation for Eq. (6.33) for the PMOS device.

**Solution:**

Since the device is a PMOS MOSFET, source and drain are p+ regions and the substrate is an nwell. Therefore, all the bulk is the most positive terminal and source is more positive than drain and gate. We follow the voltage convention of **Figure 6.1** in the book. Also, the threshold for PMOS device ( $V_{THP}$ ) is a negative quantity.

Consider the **Figure 6.11**, where  $V_{SG} > |V_{THP}|$ , so that the surface under the oxide is inverted and  $V_{SD} > 0$ , causing a drift current to flow from the source to the drain.



**Figure 6.11** Calculation of large-signal behavior of the PMOS MOSFET in the triode region

$V(y)$  is the channel voltage with respect to the source of the PMOS (a negative quantity) at a distance  $y$  away from the source. The potential difference between the Gate electrode and the channel is  $V_{SG} - V(y)$ . The charge/unit area in the inversion layer is given by

$$Q'_{ch} = C'_{ox} \cdot [V_{SG} - V(y)] \quad \text{Eq (6.1)}$$

Charge  $Q'_b$  (holes) is present in the inversion layer from the application of the threshold voltage,  $V_{THP}$ , necessary for conduction between the drain and source. This charge is given by,

$$Q'_b = C'_{ox} \cdot |V_{THP}| \quad \text{Eq(6.2)}$$

The total charge available in the channel, for conduction of a current between the source and the drain, is given by the difference between **Equation (6.1)** and **Equation (6.2)**, which is

$$Q'_I(y) = C'_{ox} \cdot [V_{SG} - V(y) - |V_{THP}|] \quad \text{Eq(6.3)}$$

where is the charge in the inverted channel.

The differential resistance of the channel region with a length  $dy$  and a width  $W$  is given by,

$$dR = (1 / \mu_p Q'_I(y)) \cdot dy / W \quad \text{Eq(6.4)}$$

where  $\mu_p$  is the average hole mobility through the channel with units  $\text{cm}^2/\text{V}\cdot\text{sec}$ .

The differential voltage drop across this differential resistance is given by

$$dV(y) = I_D \cdot dR = I_D \cdot dy / (W \mu_p Q'_I(y)) \quad \text{Eq(6.5)}$$

Substituting Equation (6.) and rearranging

$$I_D \cdot dy = W \mu_p C'_{ox} \cdot [V_{SG} - V(y) - |V_{THP}|] \cdot dV(y) \quad \text{Eq(6.6)}$$

We define the transconductance of the PMOS MOSFET as,

$$KP_p = \mu_p C'_{ox} = \mu_p \epsilon_{ox} / t_{ox} \quad \text{Eq(6.7)}$$

The current can be found by integrating the left side of **Equation (6.6)** from source to drain, that is from 0 to  $L$  and the right side from 0 to  $V_{SD}$ . This current flows from source to drain. This is as shown below:

$$I_D \cdot \int_0^L dy = W KP_p \int_0^{V_{SD}} [V_{SG} - V(y) - |V_{THP}|] \cdot dV(y) \quad \text{Eq(6.8)}$$

$$I_D = KP_p (W/L) [ (V_{SG} - |V_{THP}|) V_{SD} - (V_{SD}^2 / 2) ] \quad \text{Eq(6.9)}$$

for  $V_{SG} > |V_{THP}|$  and  $V_{SD} \leq V_{SG} - |V_{THP}|$

This current flows from Source to drain.

**Problem 6.12****John Spratt**

Using Eq. (6.35) estimate the small-signal channel resistance (the change in the drain current with changes in the drain-source voltage) of a MOSFET operating in the triode region (the resistance between the drain and source).

**Solution:**

$$\text{Eq 6.35: } I_D = \beta * [(V_{gs} - V_{thn})V_{ds} - V_{ds}^2/2]$$

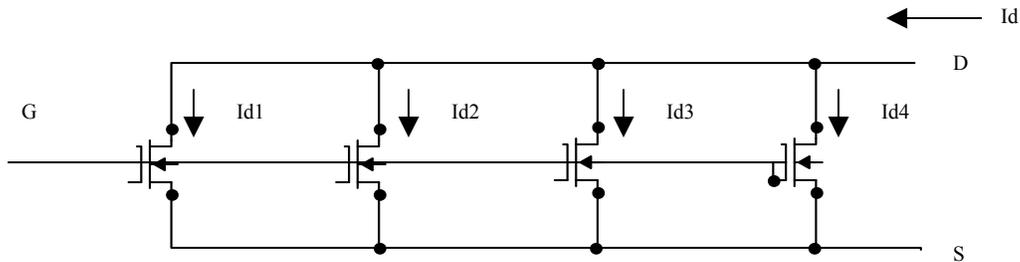
$$\begin{aligned} r &= \Delta V_{ds} / \Delta I_D \\ &= (V_{ds1} - V_{ds2}) / [(\beta * [(V_{gs} - V_{thn}) * (V_{ds1}) - (V_{ds1})^2/2]) - \beta * [(V_{gs} - V_{thn}) * (V_{ds2}) - (V_{ds2})^2/2]] \\ &= (V_{ds1} - V_{ds2}) / [(\beta * [(V_{gs} - V_{thn}) * (V_{ds1} - V_{ds2}) - (V_{ds1})^2/2 + (V_{ds2})^2/2])] \\ &= 1 / [(\beta * [(V_{gs} - V_{thn}) - (V_{ds1} + V_{ds2})/2])] \end{aligned}$$

$$r = 1 / [\beta * (V_{gs} - V_{thn} - V_{ds})]$$

**Problem 6.13**

Steve Bard

**Question:** Show, using Eqs. 6.33 and 6.37, that the parallel connection of MOSFETs shown in Fig. 5.18 behaves as a single MOSFET with a width equal to the sum of the individual MOSFET's widths.



Equivalent of Fig. 5.18

**Solution:** From Kirchoff's Current Law, we know that  $I_d = I_{d1} + I_{d2} + I_{d3} + I_{d4}$ . So if each MOSFET has the same  $KP$ ,  $L$ ,  $V_{GS}$ ,  $V_{DS}$  and  $V_{THN}$ , equations 6.33 and 6.37 become:

$$I_d = KP_n \cdot \frac{W1 + W2 + W3 + W4}{L} \cdot \left[ (V_{GS} - V_{THN})V_{DS} - \frac{V_{DS}^2}{2} \right] \quad \text{for Eq. 6.33}$$

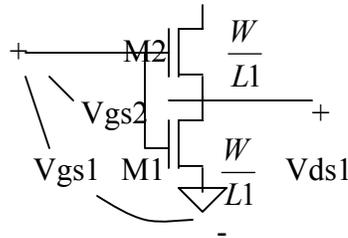
$$I_d = KP_n \cdot \frac{W1 + W2 + W3 + W4}{L} \cdot [(V_{GS} - V_{THN})^2] \quad \text{for Eq. 6.37}$$

This shows that the total drain current,  $I_d$ , is equal to a single MOSFET with a width equal to  $W1 + W2 + W3 + W4$ .

### Problem 6.14

Shambhu Roy

Show that the bottom MOSFET, Fig 6.21, in a series connection of two MOSFETs cannot operate in the saturation region. Neglect the body effect. Hint: Show that M1 is always in either cutoff ( $V_{GS1} < V_{THN}$ ) or triode ( $V_{DS1} < V_{GS1} - V_{THN}$ ).



### Solution:

For  $V_{GS1} < V_{THN}$  both MOSFETs are in the cutoff region.

When  $V_{GS1} > V_{THN}$

$$V_{DS1} = V_{GS1} - V_{GS2}$$

Also

$$V_{DS1} \geq V_{GS1} - V_{THN}$$

$$\Rightarrow V_{GS1} - V_{GS2} \geq V_{GS1} - V_{THN}$$

$$\Rightarrow V_{GS2} < V_{THN}$$

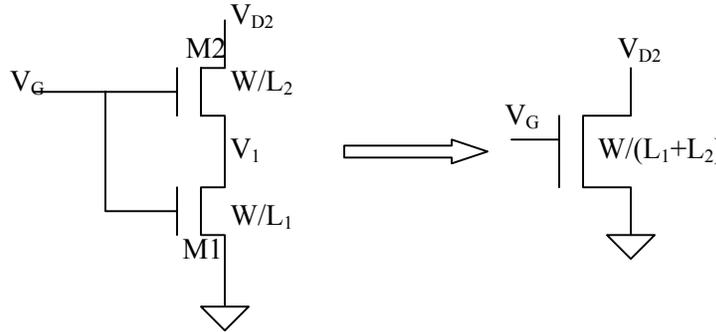
Which cannot be true, therefore if top MOSFET has to operate then the bottom MOSFET cannot be in Saturation.

**Problem 6.15**

**Harish Reddy Singidi**

**Show that the series connection of MOSFETs shown in fig. 6.21 behaves as a single MOSFET with Twice the length of the individual MOSFETs. Again neglect the body effect.**

**Solution:**



Assuming both MOSFETs are in triode region

For M<sub>1</sub> I<sub>D1</sub> = I<sub>D</sub>

$$I_{D1} = I_D = K P_n (W/L_1) [(V_G - V_{THN})V_1 - V_1^2/2]$$

$$(I_D L_1) / (K P_n W) = [(V_G - V_{THN})V_1 - V_1^2/2]$$

As Both MOSFETs are in series i.e., I<sub>D1</sub> = I<sub>D2</sub> = I<sub>D</sub>

For M<sub>2</sub> I<sub>D2</sub> = I<sub>D</sub>

$$I_{D2} = I_D = K P_n (W/L_2) [(V_G - V_1 - V_{THN})(V_{D2}-V_1) - (V_{D2}-V_1)^2/2]$$

$$(I_D L_2) / (K P_n W) = [(V_G - V_1 - V_{THN})(V_{D2}-V_1) - (V_{D2}-V_1)^2/2]$$

$$[(I_D L_1) / (K P_n W)] + [(I_D L_2) / (K P_n W)] = [(V_G - V_{THN})V_1 - V_1^2/2] + [(V_G - V_1 - V_{THN})(V_{D2}-V_1) - (V_{D2}-V_1)^2/2]$$

$$[(I_D (L_1+L_2)) / (K P_n W)] = [(V_G - V_{THN}) V_{D2} - (V_{D2})^2/2]$$

This is the current from drain to source for a single MOSFET with length (L<sub>1</sub>+L<sub>2</sub>)

If L<sub>1</sub>=L<sub>2</sub>=L

$$[(2I_D L) / (K P_n W)] = [(V_G - V_{THN}) V_{D2} - (V_{D2})^2/2]$$

$$I_D = [(K P_n W)/2L] [(V_G - V_{THN}) V_{D2} - (V_{D2})^2/2]$$