

# Filtering topologies

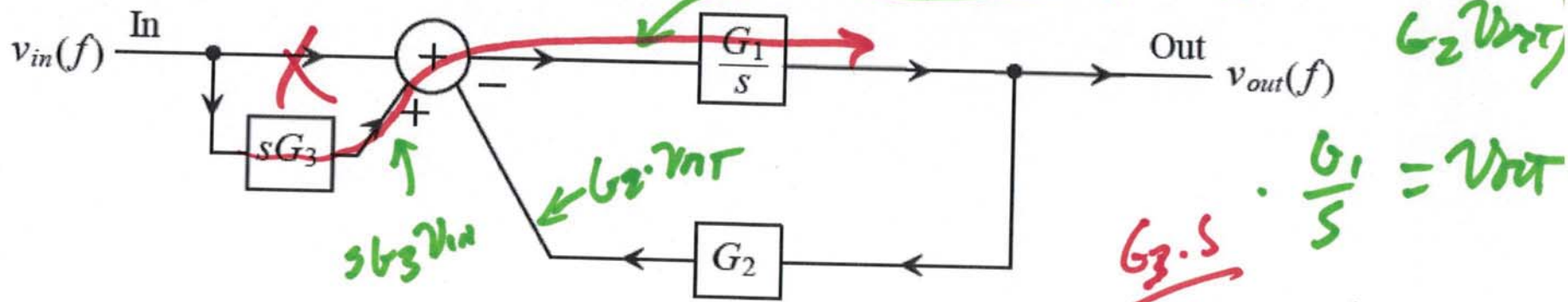
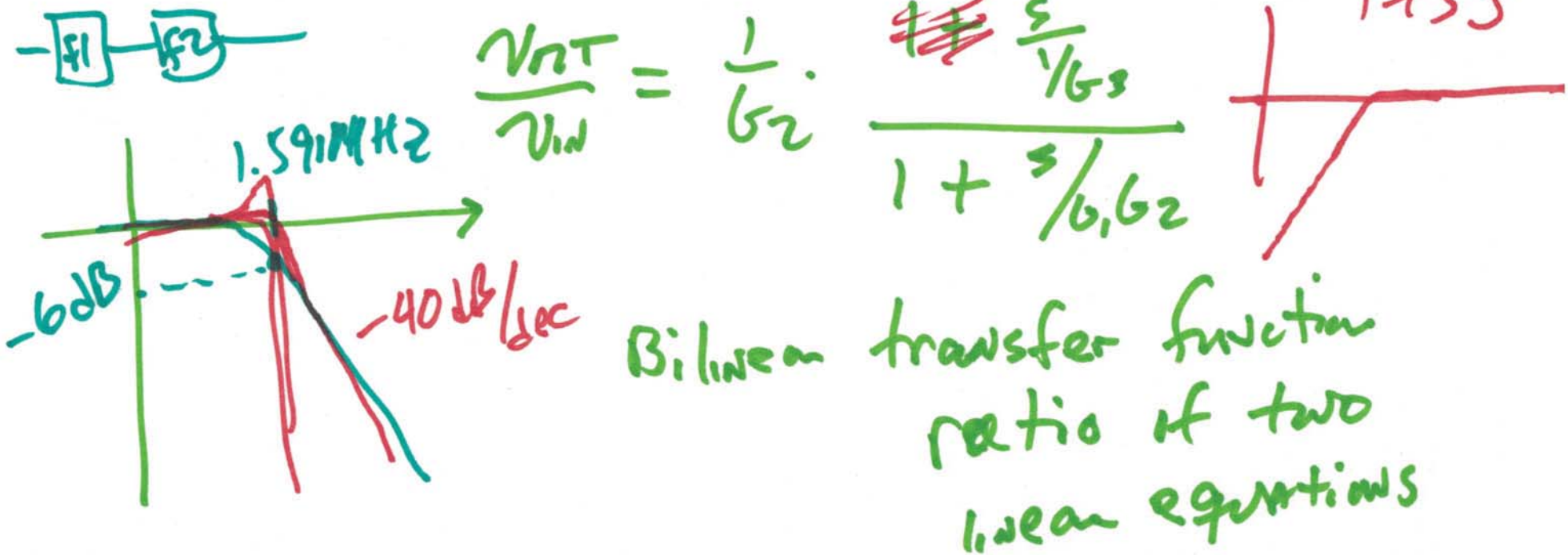
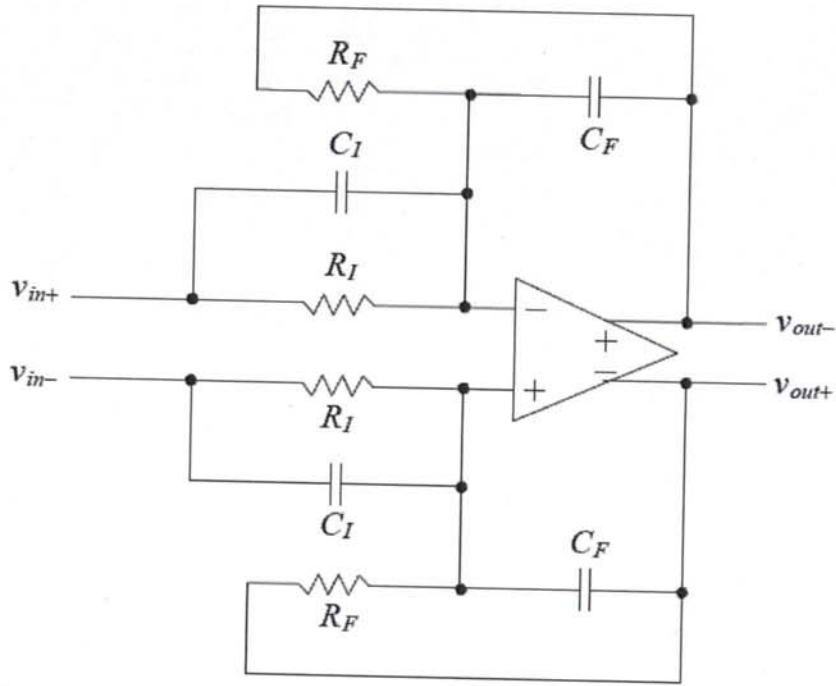


Figure 3.29 Implementation of a bilinear transfer function using an integrator.





$$\frac{V_{out}}{V_{in}} = \frac{1}{G_2} \cdot \frac{1 + \frac{s}{G_2}}{1 + \frac{s}{G_1 G_2}}$$

$$G_1 = \frac{1}{R_I C_F}$$

$$G_2 = \frac{R_I}{R_F}$$

$$G_3 = R_I C_I$$

$R_I \rightarrow \infty$   
 $G_1 \rightarrow 0$   
 $G_2 \rightarrow \infty$   
 $G_3 \rightarrow \infty$

Figure 3.30 Implementation of an active-RC bilinear transfer function filter.

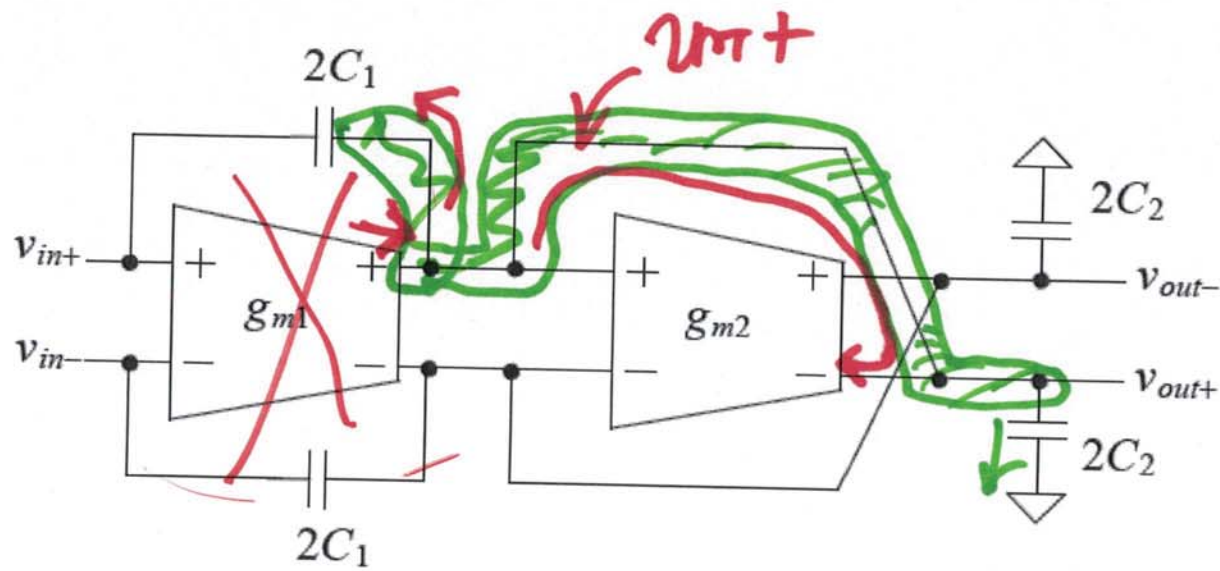
$$\frac{R_F}{R_I} \cdot \frac{1 + s R_I C_I}{1 + s R_F C_F}$$

$\swarrow R_I \rightarrow \infty$   
 $\frac{R_F}{R_I} + s R_F C_I$

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$$1 + s R_F C_F$$

2)



$$G_1 = g_{m1}/(C_1 + C_2)$$

$$G_2 = \frac{g_{m2}}{g_{m1}}$$

$$G_3 = \frac{C_1}{g_{m1}}$$

$g_1 \rightarrow 0$  (remove)

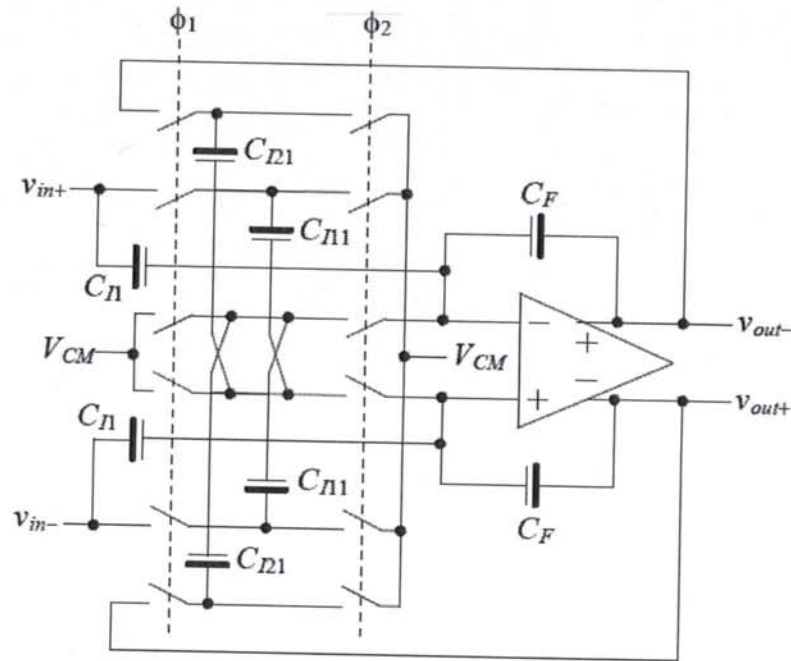
Figure 3.31 Implementation of a bilinear filter using transconductors.

$b_1 \rightarrow 0$   
 $b_2 \rightarrow \infty$   
 $b_3 \rightarrow \infty$

$$g_{m1}(v_{in})$$

$$= \frac{v_{out} - v_{in}}{1/j\omega C_1} + v_{out} \cdot g_{m2} + \frac{v_{out}}{1/j\omega 2C_2}$$

3)



$$G_1 = \frac{C_{N1}}{C_F} \cdot f_s$$

$$G_2 = \frac{C_{D1}}{C_{N1}}$$

$$G_3 = \frac{C_N}{C_{N1} \cdot f_s}$$

$$\frac{v_{out}(f)}{v_{in}(f)} = \frac{1}{G_2} \cdot \frac{1 + \frac{s}{1/G_3}}{1 + \frac{s}{G_1 G_2}}$$

Figure 3.32 Implementation of a bilinear filter using switched capacitors.

4)



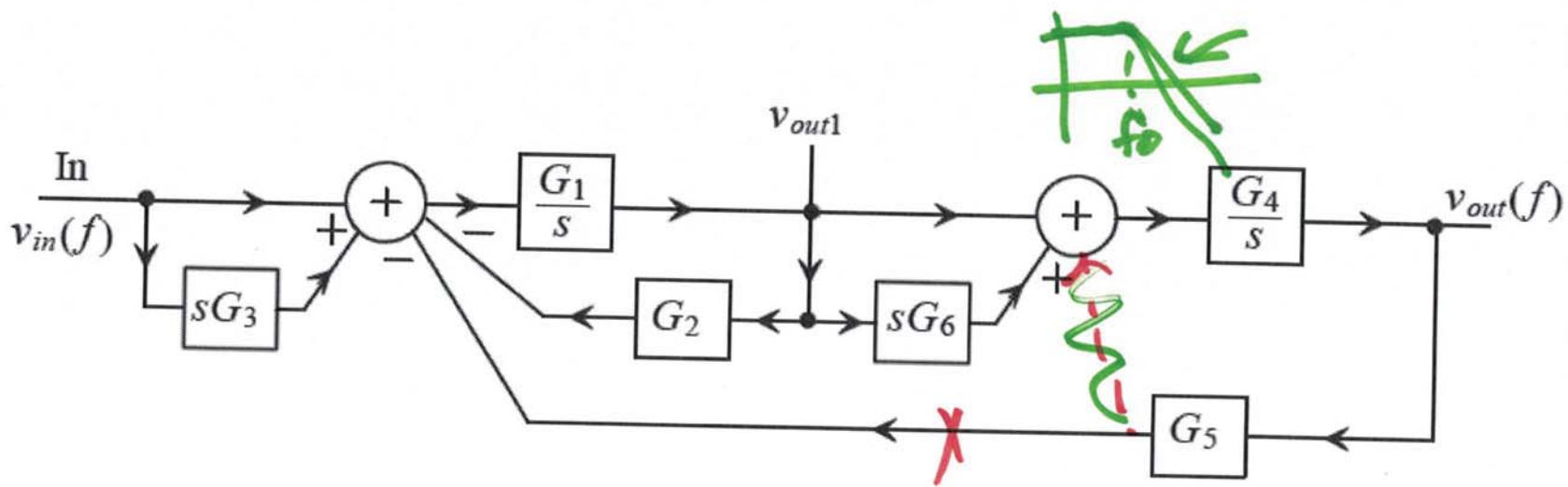


Figure 3.33 Implementation of a biquadratic transfer function using two integrators.

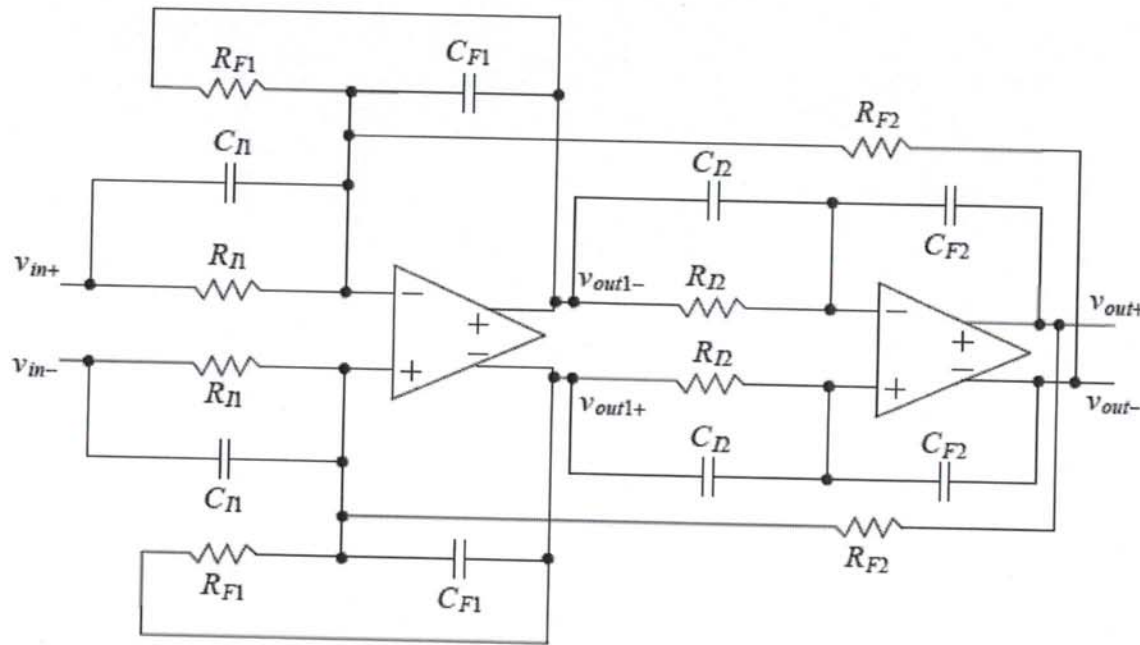
$$\frac{v_{out}}{v_{in}} = \frac{a_2 s^2 + a_1 s + a_0}{s^2 + \left(\frac{2\pi f_0}{Q}\right)s + (2\pi f_0)^2}$$

$\omega_0 = 2\pi f_0$  ← NATURAL  
 $Q = \frac{\text{ENERGY STORED}}{\text{ENERGY LOST}}$

3dB → 900K  
 5dB → 1.1M → Q =  $\frac{f_0}{BW} = \frac{1M}{200K} = 5$

over-damp  
 fcenter

5)

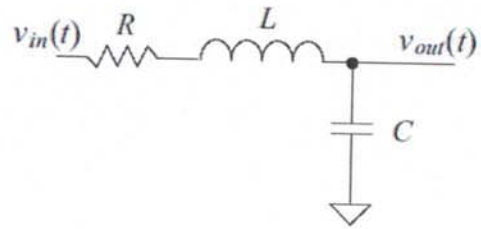


$$G_1 = \frac{1}{R_\Pi C_{F1}} \quad G_2 = \frac{R_\Pi}{R_{F1}} \quad G_3 = R_\Pi C_\Pi \quad G_4 = \frac{1}{R_\Pi C_{F2}} \quad G_5 = \frac{R_\Pi}{R_{F2}} \quad G_6 = R_\Pi C_\Pi$$

$$a_2 = \frac{C_\Pi C_\Pi}{C_{F1} C_{F2}} \quad a_1 = \frac{C_\Pi}{R_\Pi C_{F1} C_{F2}} + \frac{C_\Pi}{R_\Pi C_{F1} C_{F2}} \quad a_0 = \frac{1}{R_\Pi C_{F1} R_\Pi C_{F2}}$$

$$\frac{\omega_0}{Q} = \frac{2\pi f_0}{Q} = \frac{1}{R_{F1} C_{F1}} + \frac{C_\Pi}{C_{F1} R_{F2} C_{F2}} \quad f_0 = \frac{1}{2\pi} \cdot \sqrt{\frac{1}{C_{F1} R_\Pi C_{F2} R_{F2}}}$$

Figure 3.34 Implementation of the active-RC biquadratic transfer function filter.



$$\frac{v_{out}}{v_{in}} = \frac{\frac{1}{LC}}{s^2 + s\frac{R}{L} + \frac{1}{LC}}$$

$$f_0 = \frac{1}{2\pi\sqrt{LC}}$$

$$Q = \frac{1}{R}\sqrt{\frac{L}{C}}$$

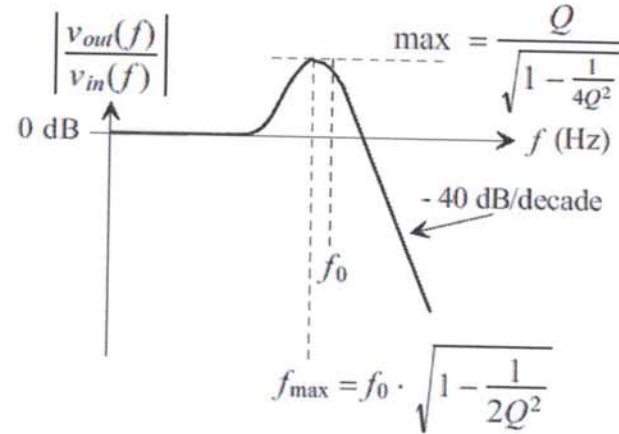
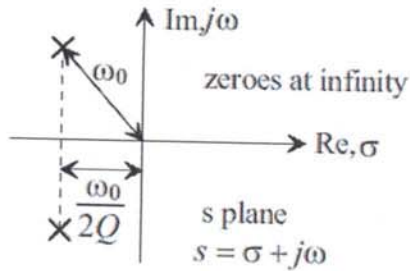


Figure 3.35 Second-order lowpass filter.



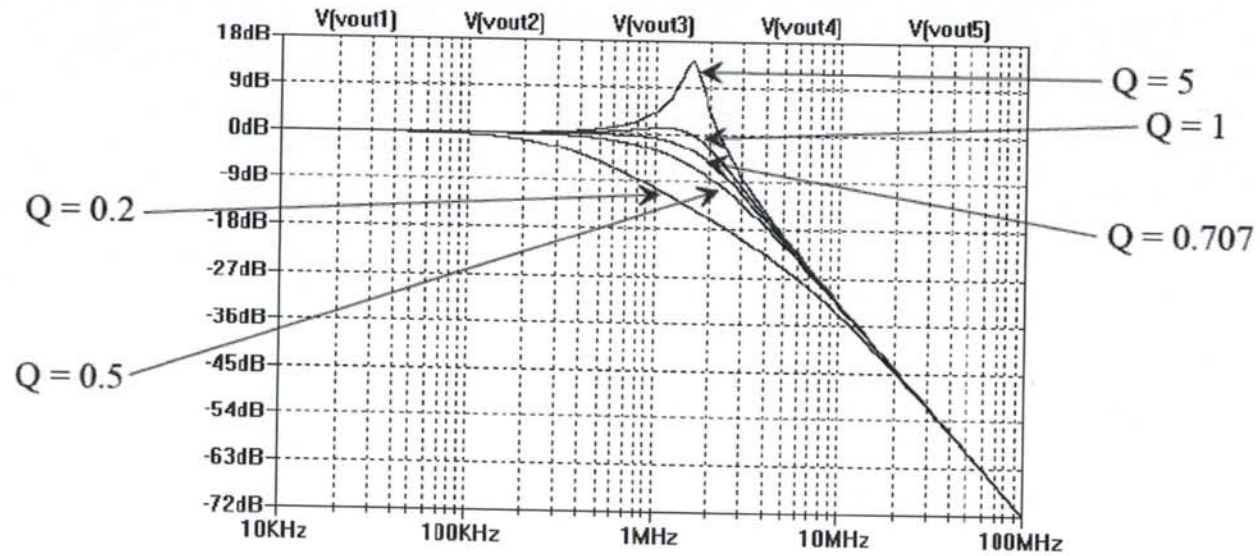


Figure 3.37 The effect of Q on the frequency response of a second-order lowpass filter.

SAW

8)