

S/H

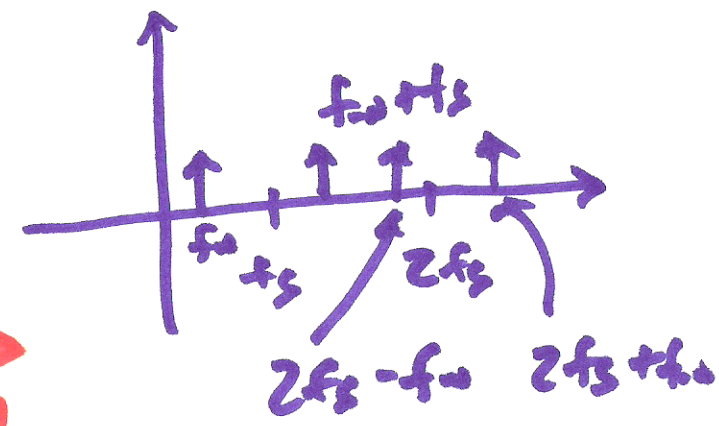
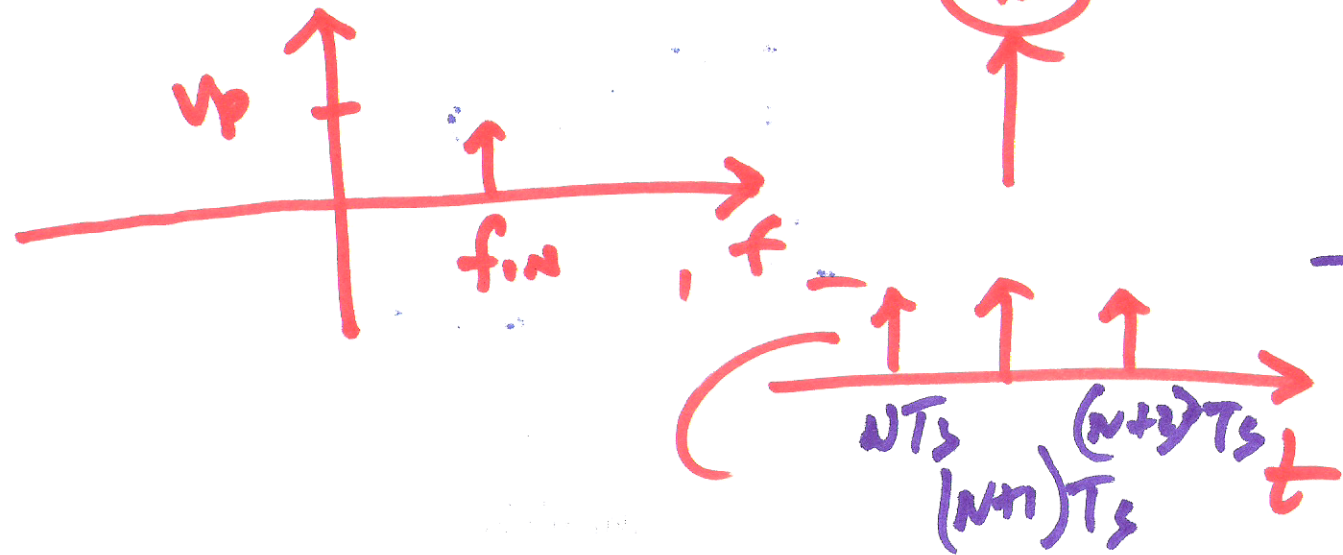
Sept. 8, 2014

The S/H

2.1  
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$$y(t) = \sum_{N=-\infty}^{\infty} V_p \sin(2\pi f_{in} t) \cdot \delta(t - nT_s)$$

$$V_p \sin(2\pi f_{in} t)$$

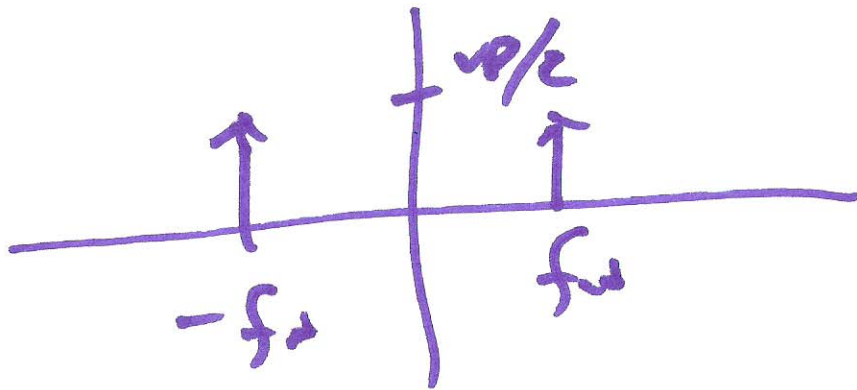


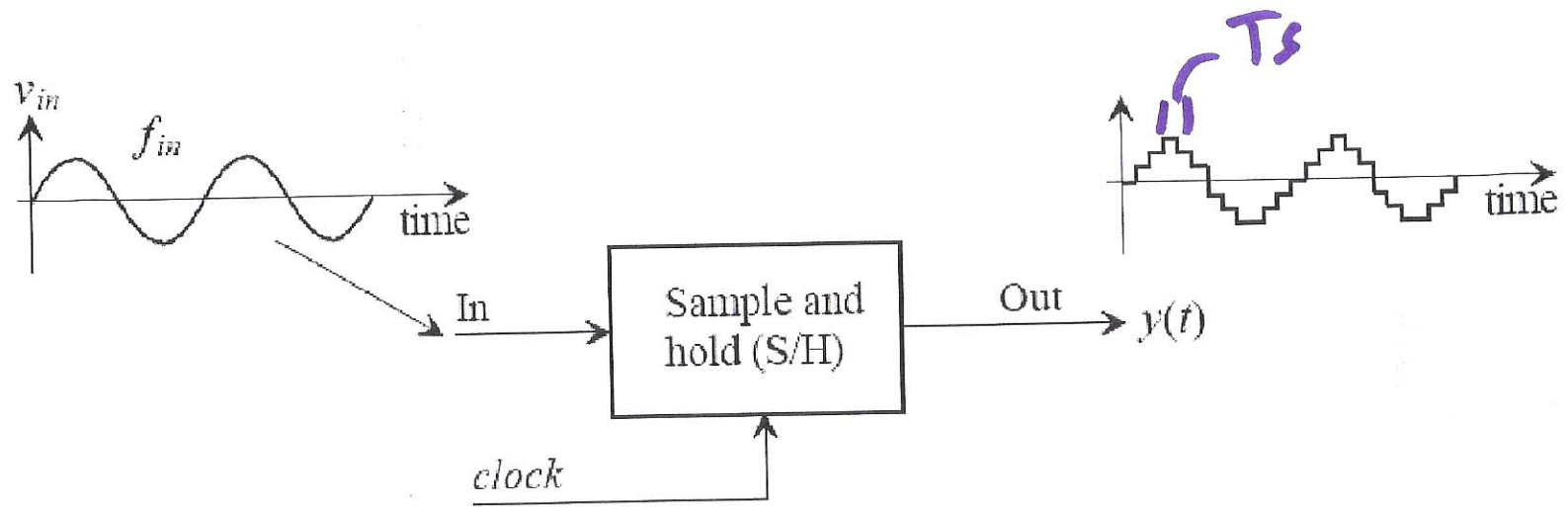
1)

$$y(t) = \sum_{N=-\infty}^{\infty} V_p \sin(2\pi f_s t) \cdot \delta(t - NT_s)$$

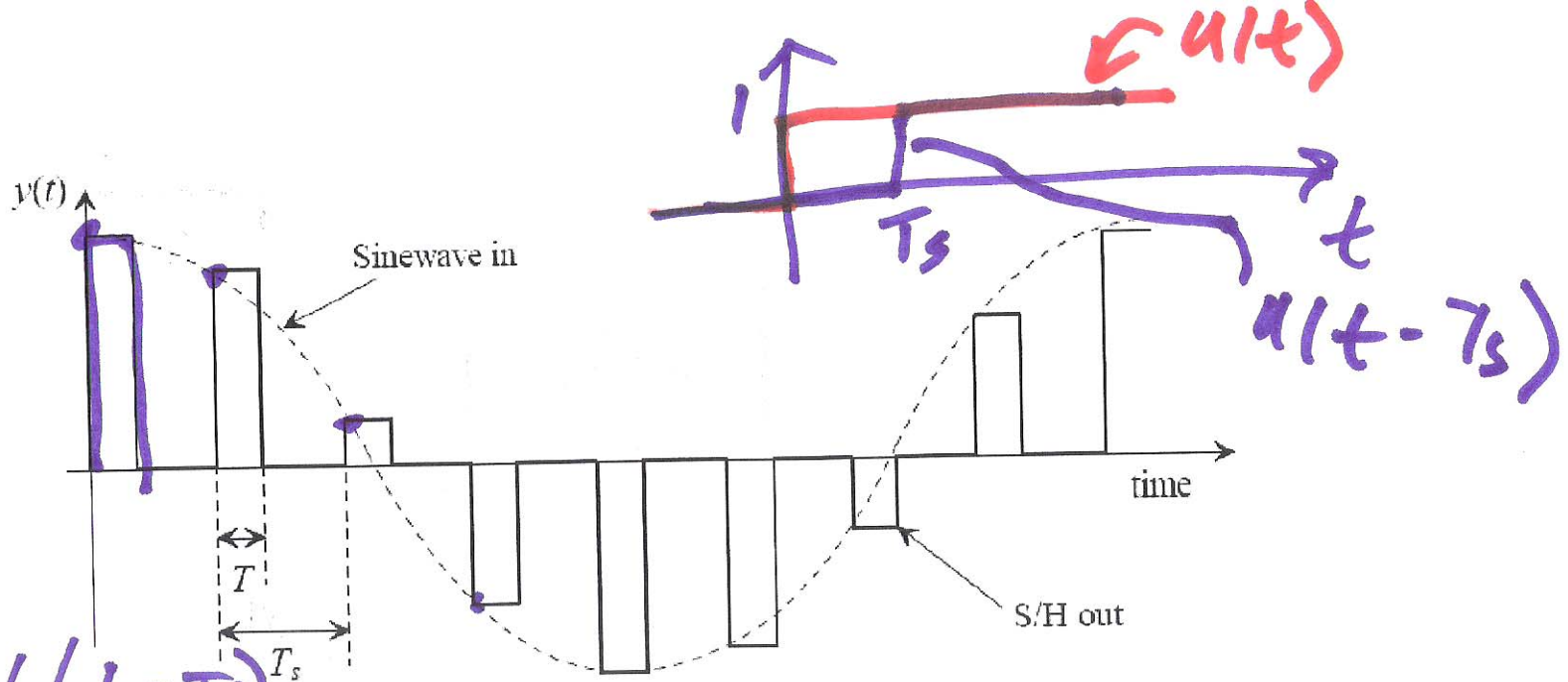
↑  
output of  
impulse  
sampler

$$Y(f) = \frac{V_p}{2jT_s} \sum_{k=-\infty}^{\infty} [\delta(f - f_m - kf_s) - \delta(f + f_m - kf_s)]$$





**Figure 2.14** Sampling and holding an input sinewave.



$$u(t) - u(t - T_s)$$

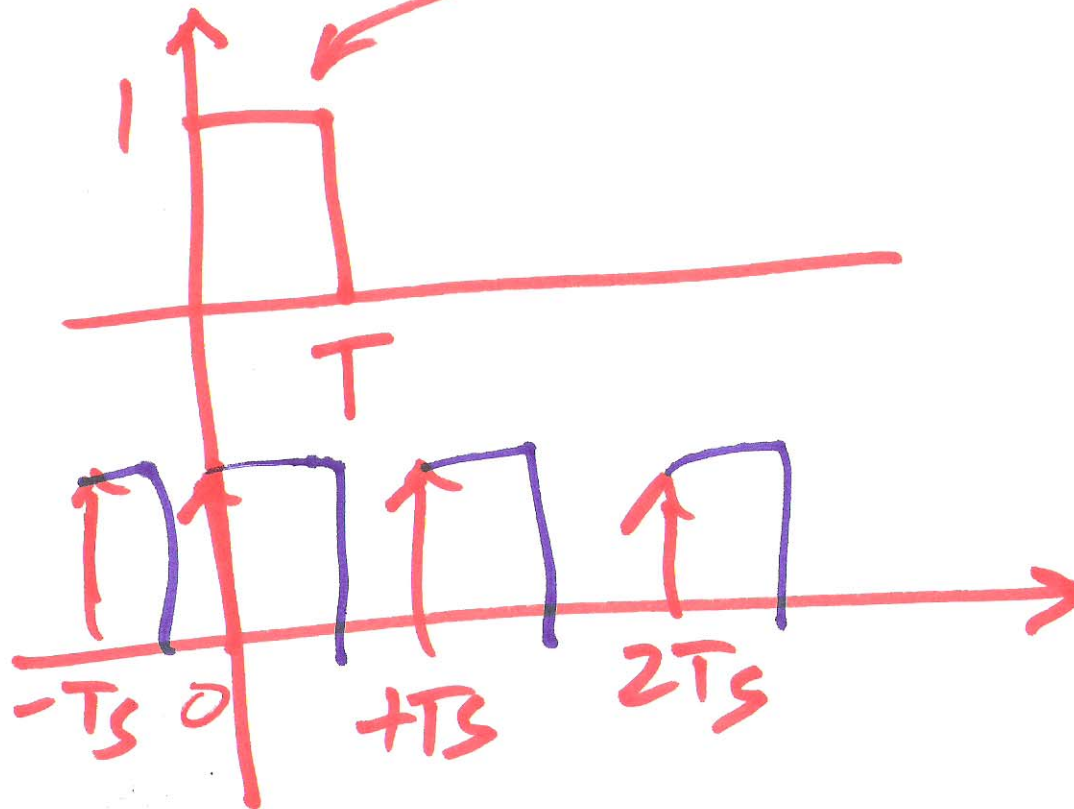
Figure 2.15 Sample-and-hold output with return to zero format.

$$y(t) = \sum_{N=-\infty}^{\infty} V_p \sin(2\pi f_s \cdot N T_s) [u(t - N T_s) - u(t - N T_s - T)]$$

4)

$$u(t - NT_s) - u(t - NT_s - T)$$

$$= \left\{ \delta(t - NT_s) \otimes [u(t) - u(t - T)] \right\}$$



$$y(t) = V_p \sin(2\pi f_w \cdot t) \cdot \sum_{n=-\infty}^{\infty} \delta(t - nT_s) \otimes (*)$$

$P(t)$

$$[u(t) - u(t-T)]$$

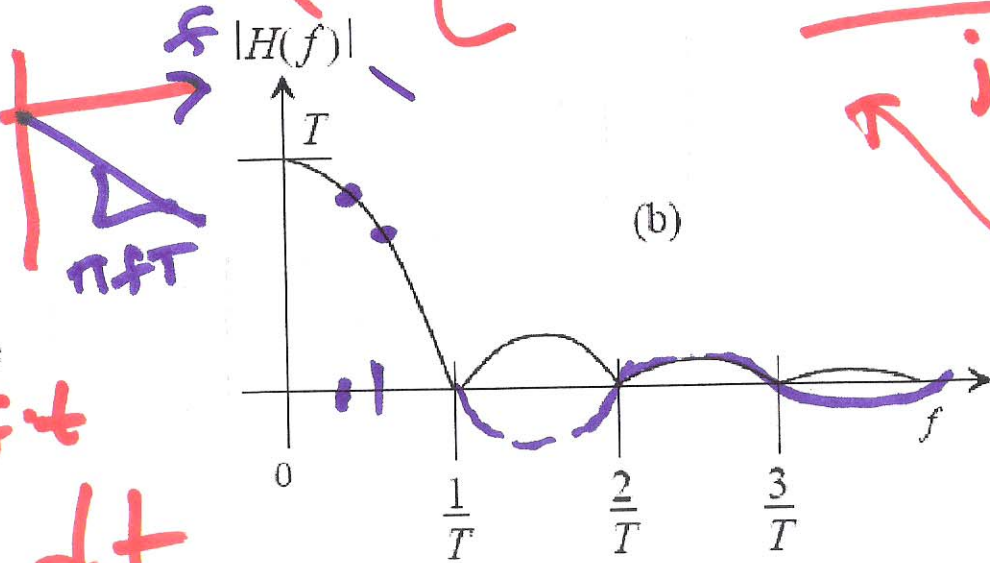
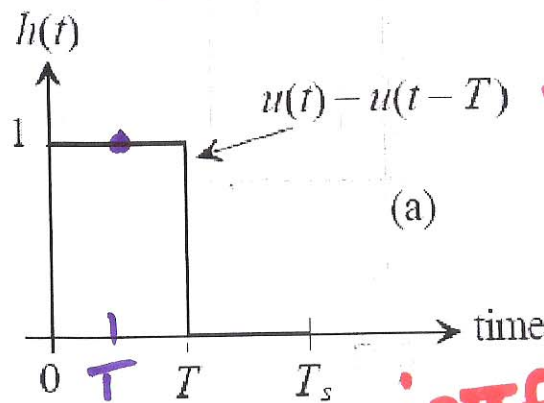
$$y(t) = (u_w(f) \otimes P(f)) \cdot H(f)$$

$$\frac{V_p}{2iTs} \sum_{k=-\infty}^{\infty} [\delta(f - k/T_s) - \delta(f - (k+1)/T_s)]$$

6)



S/H  $\rightarrow e^{-j2\pi f \frac{T}{2}}$  T S.W.C  $(\pi f T)$   $\leftarrow e^{-j\pi f T}$   $\frac{e^{-j\pi f T} - e^{j\pi f T}}{-e^{j2\pi f T}}$



$$H(f) = \int_{-\infty}^{\infty} h(t) \cdot e^{-j2\pi f t} dt$$

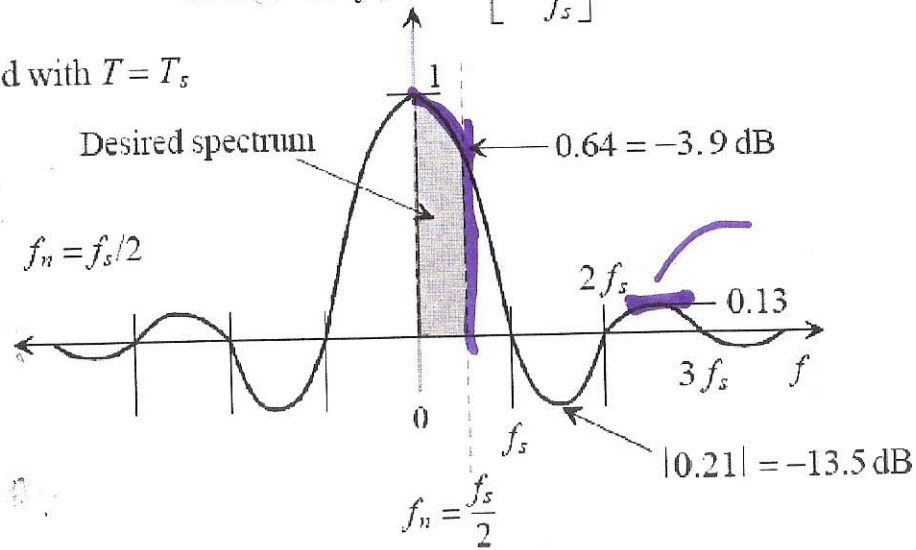
Figure 2.16 (a) Sampling pulse and (b) its spectrum.

$$H(f) = \int_0^T e^{-j2\pi f \cdot t} dt = \frac{1}{-j2\pi f} e^{-j2\pi f \cdot t} \Big|_0^T = -\frac{1}{j2\pi f} [e^{-j2\pi f T} - 1]$$

$$T = T_s$$

$$\text{Sinc}(\pi \cdot T_s \cdot f) = \text{Sinc}\left[\pi \cdot \frac{f}{f_s}\right]$$

Sample-and-hold with  $T = T_s$



Sinc x  
 $\approx$  ~~max~~ x  
 $x \approx 0$

Figure 2.17 The frequency response of a S/H.

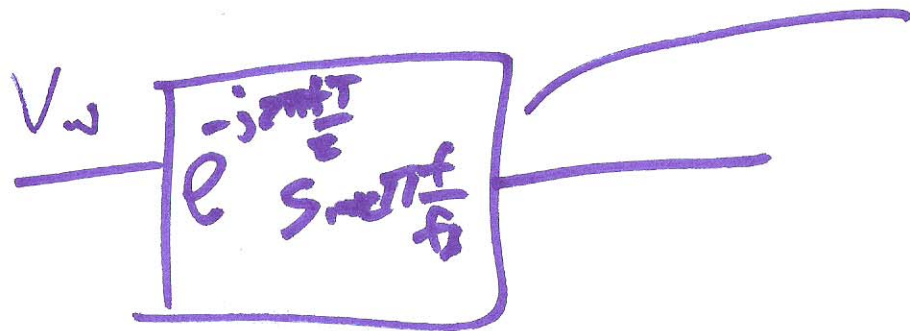
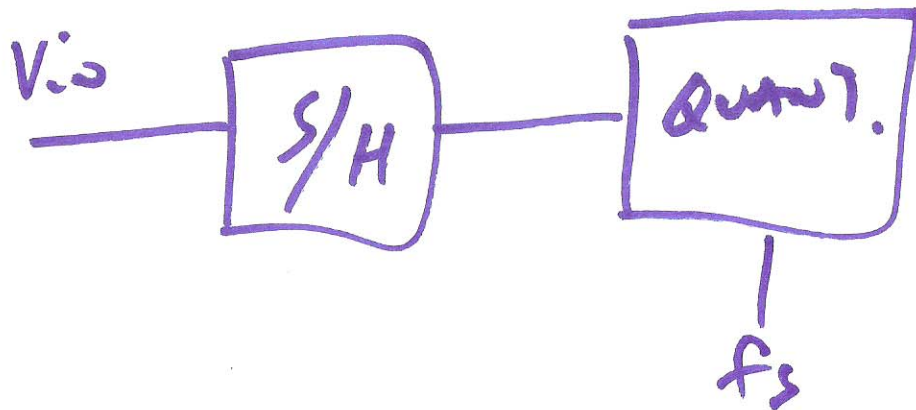
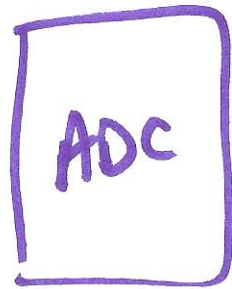
$$\text{Sinc } \pi f/f_s$$

$$\text{Sin } \pi \frac{f}{f_s}$$

$$\frac{\text{Sin } \pi \frac{f}{f_s}}{\pi \frac{f}{f_s}} \approx \frac{\pi \frac{f}{f_s}}{\pi \frac{f}{f_s}} = 1$$

8)





$$\frac{1 - e^{-sT}}{sT}$$

9)

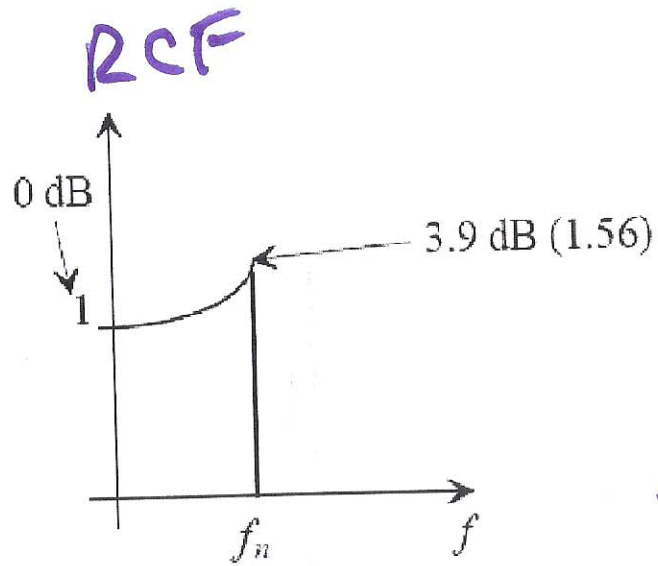
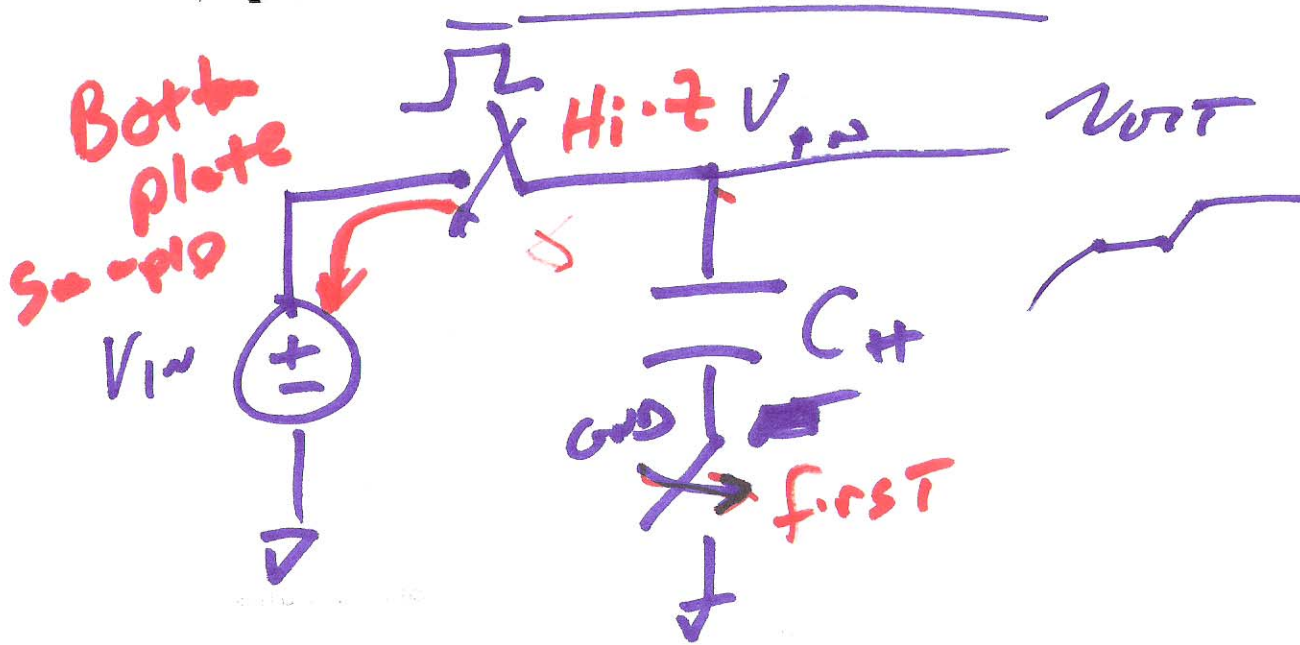


Figure 2.19 Ideal reconstruction filter frequency response for a S/H.



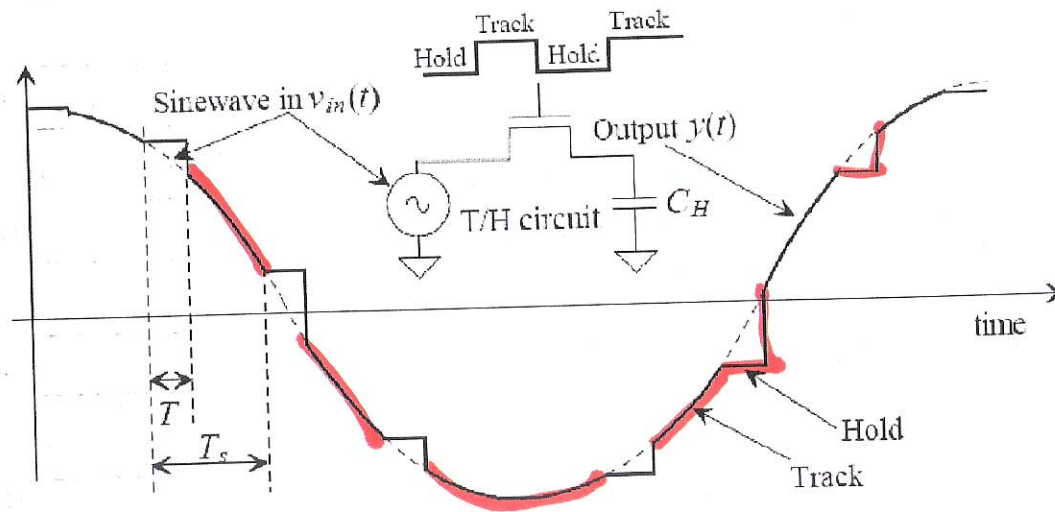


Figure 2.23 Track-and-hold output.