

Chapter 6, Solution 6.

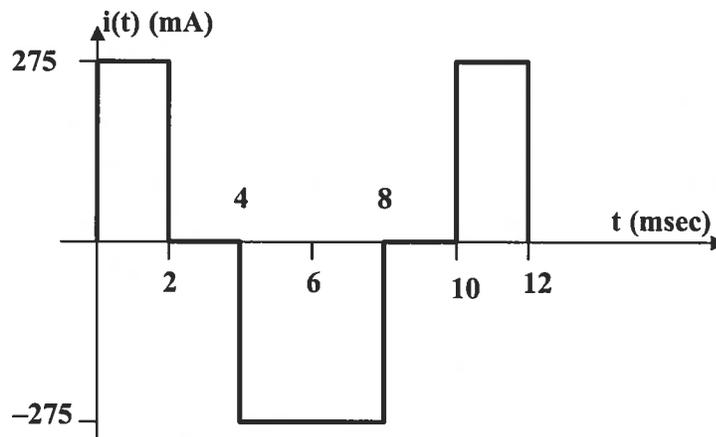
$$i = C \frac{dv}{dt} = 55 \times 10^{-6} \text{ times the slope of the waveform.}$$

For example, for $0 < t < 2$,

$$\frac{dv}{dt} = \frac{10}{2 \times 10^{-3}}$$

$$i = C \frac{dv}{dt} = (55 \times 10^{-6}) \frac{10}{2 \times 10^{-3}} = 275 \text{ mA}$$

Thus the current $i(t)$ is sketched below.



Chapter 6, Solution 12.

$i_R = V/R = (30/12)e^{-2000t} = 2.5 e^{-2000t}$ and $i_C = C(dv/dt) = 0.1 \times 30(-2000) e^{-2000t}$
 $= -6000 e^{-2000t}$ A. Thus, $i = i_R + i_C = -5,997.5 e^{-2000t}$. The power is equal to:

$$v_i = -179.925 e^{-4000t} \text{ W.}$$

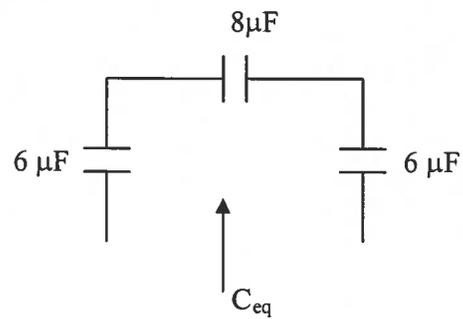
Chapter 6, Solution 18.

$4\ \mu\text{F}$ in parallel with $4\ \mu\text{F} = 8\ \mu\text{F}$

$4\ \mu\text{F}$ in series with $4\ \mu\text{F} = 2\ \mu\text{F}$

$2\ \mu\text{F}$ in parallel with $4\ \mu\text{F} = 6\ \mu\text{F}$

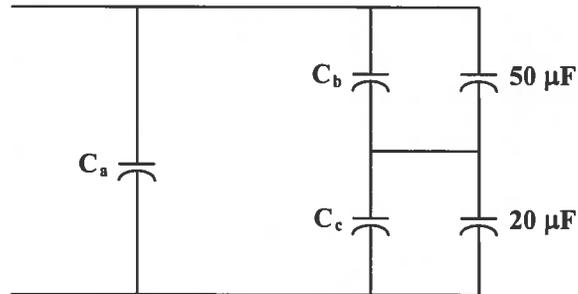
Hence, the circuit is reduced to that shown below.



$$\frac{1}{C_{eq}} = \frac{1}{6} + \frac{1}{6} + \frac{1}{8} = 0.4583 \quad \longrightarrow \quad C_{eq} = \underline{2.1818\ \mu\text{F}}$$

Chapter 6, Solution 28.

We may treat this like a resistive circuit and apply delta-wye transformation, except that R is replaced by 1/C.



$$\frac{1}{C_a} = \frac{\left(\frac{1}{10}\right)\left(\frac{1}{40}\right) + \left(\frac{1}{10}\right)\left(\frac{1}{30}\right) + \left(\frac{1}{30}\right)\left(\frac{1}{40}\right)}{\frac{1}{30}}$$
$$= \frac{3}{40} + \frac{1}{10} + \frac{1}{40} = \frac{2}{10}$$

$$C_a = 5\mu\text{F}$$

$$\frac{1}{C_b} = \frac{\frac{1}{400} + \frac{1}{300} + \frac{1}{1200}}{\frac{1}{10}} = \frac{2}{30}$$

$$C_b = 15\mu\text{F}$$

$$\frac{1}{C_c} = \frac{\frac{1}{400} + \frac{1}{300} + \frac{1}{1200}}{\frac{1}{40}} = \frac{4}{15}$$

$$C_c = 3.75\mu\text{F}$$

$$C_b \text{ in parallel with } 50\mu\text{F} = 50 + 15 = 65\mu\text{F}$$

$$C_c \text{ in series with } 20\mu\text{F} = 23.75\mu\text{F}$$

$$65\mu\text{F} \text{ in series with } 23.75\mu\text{F} = \frac{65 \times 23.75}{88.75} = 17.39\mu\text{F}$$

$$17.39\mu\text{F} \text{ in parallel with } C_a = 17.39 + 5 = 22.39\mu\text{F}$$

$$\text{Hence } C_{eq} = 22.39\mu\text{F}$$

Chapter 6, Solution 32.

(a) $C_{\text{eq}} = (12 \times 60) / 72 = 10 \mu\text{F}$

$$v_1 = \frac{10^{-3}}{12 \times 10^{-6}} \int_0^t 50e^{-2t} dt + v_1(0) = \underline{-2083e^{-2t} \Big|_0^t + 50} = \underline{-2083e^{-2t} + 2133V}$$

$$v_2 = \frac{10^{-3}}{60 \times 10^{-6}} \int_0^t 50e^{-2t} dt + v_2(0) = \underline{-416.7e^{-2t} \Big|_0^t + 20} = \underline{-416.7e^{-2t} + 436.7V}$$

(b) At $t=0.5\text{s}$,

$$v_1 = -2083e^{-1} + 2133 = 1366.7, \quad v_2 = -416.7e^{-1} + 436.7 = 283.4$$

$$w_{12\mu\text{F}} = \frac{1}{2} \times 12 \times 10^{-6} \times (1366.7)^2 = \underline{11.207 \text{ J}}$$

$$w_{20\mu\text{F}} = \frac{1}{2} \times 20 \times 10^{-6} \times (283.4)^2 = \underline{803.2 \text{ mJ}}$$

$$w_{40\mu\text{F}} = \frac{1}{2} \times 40 \times 10^{-6} \times (283.4)^2 = \underline{1.6063 \text{ J}}$$