

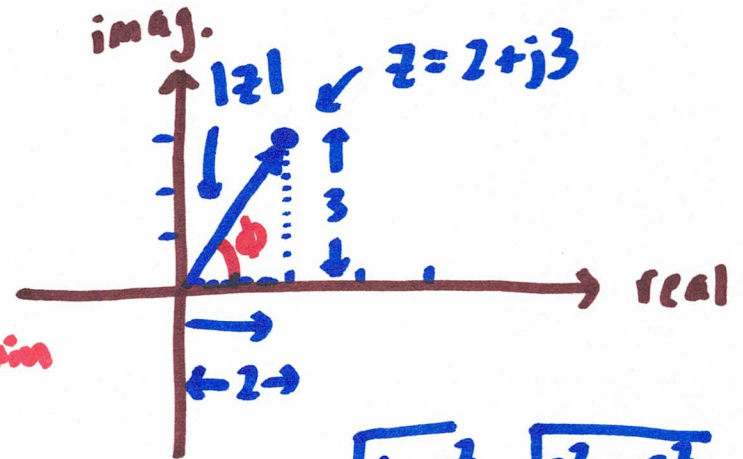
EE 220: Circuits I

$$j = \sqrt{-1}$$

Complex numbers:

$$x + jy$$

↑ ↑
real imaginary



Rectangular

$$z = 2 + j3$$

← imaginary (complex) domain

SOH - CAH - TOA → $\tan \phi = \frac{3}{2}$

$$\sqrt{|z|^2} = \sqrt{2^2 + 3^2}$$

$$|z| = \sqrt{2^2 + 3^2}$$

$$|z| = \sqrt{13}$$

rect. ↓
polar ↓

$$z = 2 + j3$$

$$z = \sqrt{13} \angle 56.3^\circ$$

$$(2 + j3) + (4 + j1) = 6 + j4$$

~~$$\tan^{-1}(\tan(\phi)) = \tan^{-1}\left(\frac{3}{2}\right)$$~~

$$\phi = \tan^{-1}\left(\frac{3}{2}\right)$$

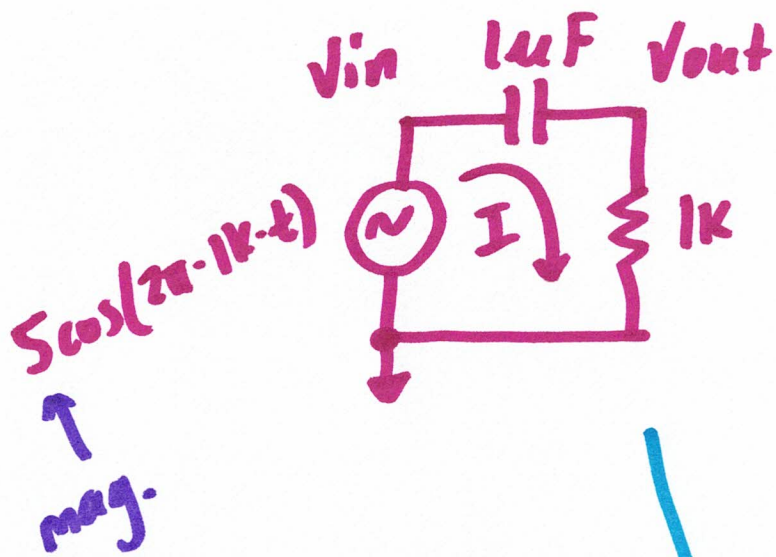
~~the~~ polar →

$$z = |z| \angle \phi$$

$$z = \sqrt{13} \angle 56.3^\circ$$

text 19.377 →

$$\left. \begin{aligned} x &= |z| \cos \phi \\ y &= |z| \sin \phi \end{aligned} \right\} x + jy$$



$V_{in} = 5\angle 0^\circ \text{ V}$

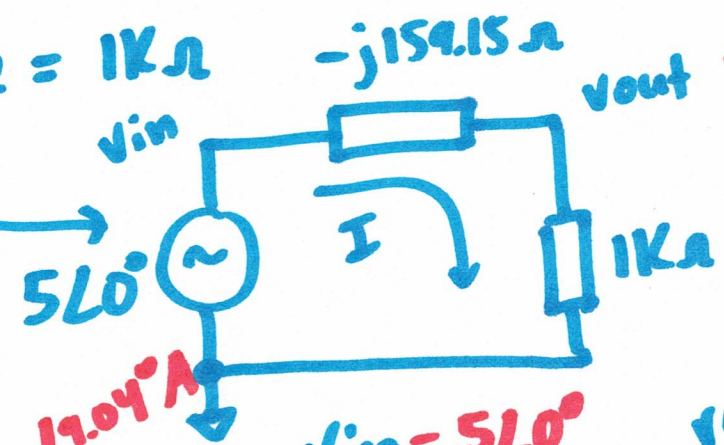
$$z_c = \frac{1}{j \cdot 2\pi \cdot f \cdot C}$$

\uparrow \uparrow
 1K $1\mu\text{F}$

$$z_c = \frac{159.15}{j} = -j159.15 \Omega$$

$$z_R = 1\text{K} \Omega$$

~~DETERMINE~~
 Find phasors for:
 1.) V_{in}
 2.) V_{out}
 3.) I



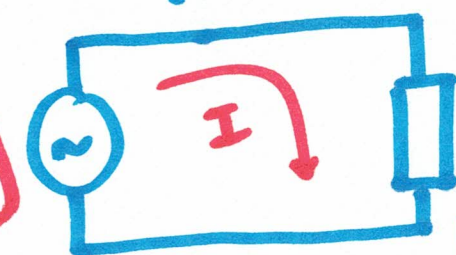
$$\frac{\phi}{360^\circ} \cdot T = t_d$$

$$\frac{9.04}{360} \cdot 1\text{ms} = \underline{\underline{25.1\mu\text{s}}}$$

$I = \frac{V}{R} = \frac{V}{z}$ impedance

$$I = \frac{5\angle 0^\circ}{1.013\text{K} \angle -9.04^\circ} = 4.93\text{m} \angle 9.04^\circ \text{ A}$$

$I = 4.93 \angle 9.04^\circ \text{ mA}$



$$z_T = 1\text{K} - j159.15$$

$$|z_T| = \sqrt{(1\text{K})^2 + (159.15)^2}$$

$$\phi = \tan^{-1}\left(\frac{-159.15}{1000}\right)$$

$z_T = 1.013\text{K} \angle -9.04^\circ \Omega$

real
 ↓
 imaginary

$$V_{in} = 5 \angle 0^\circ$$

$$I = 4.93 \angle 9.04^\circ \text{ mA}$$

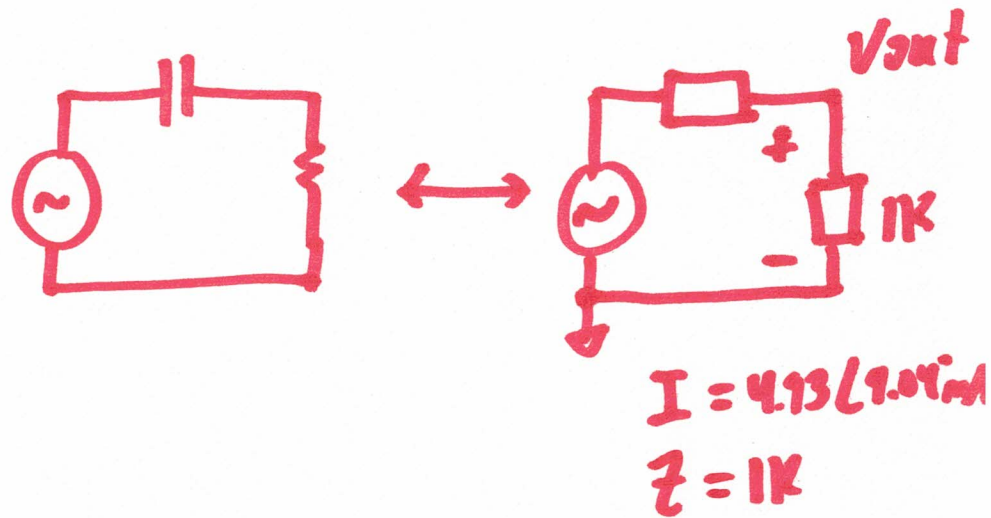
$$V_{out} = 4.93 \angle 9.04^\circ \text{ V}$$

$$1\text{K} + j0$$

$$|Z| = \sqrt{1\text{K}^2 + 0^2} = 1\text{K}$$

$$\phi = \tan^{-1}\left(\frac{0}{1\text{K}}\right) = 0^\circ$$

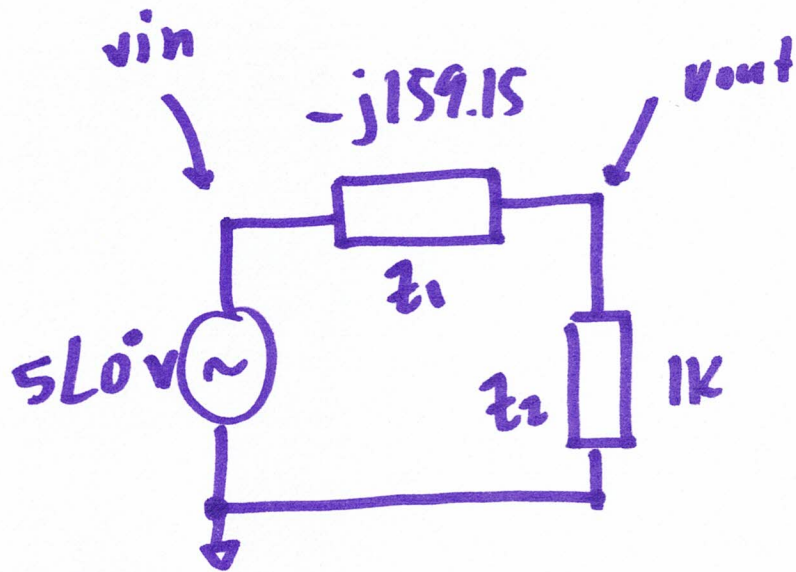
$$Z = 1\text{K} \angle 0^\circ \Omega$$



$$V_{out} = I \cdot Z$$

$$V_{out} = 4.93 \angle 9.04^\circ \text{ mA} \cdot 1\text{K} \angle 0^\circ \Omega$$

$$V_{out} = 4.93 \angle 9.04^\circ \text{ V}$$



$$5\angle 0^\circ = V_{in}$$

$$V_{out} = V_{in} \left(\frac{Z_2}{Z_1 + Z_2} \right)$$

$$V_{out} = 5\angle 0^\circ \left(\frac{1k\angle 0^\circ}{1.013k\angle -9.04^\circ} \right)$$

$$V_{out} = 5\angle 0^\circ (0.987\angle 9.04^\circ)$$

$$V_{out} = 4.93\angle 9.04^\circ \text{ V}$$

$$Z_R = R$$

$$Z_C = \frac{1}{j\omega C}$$

$$Z_L = j\omega L$$

$$\omega = 2\pi f$$

Last Day to do missed quizzes: 4/27/2022