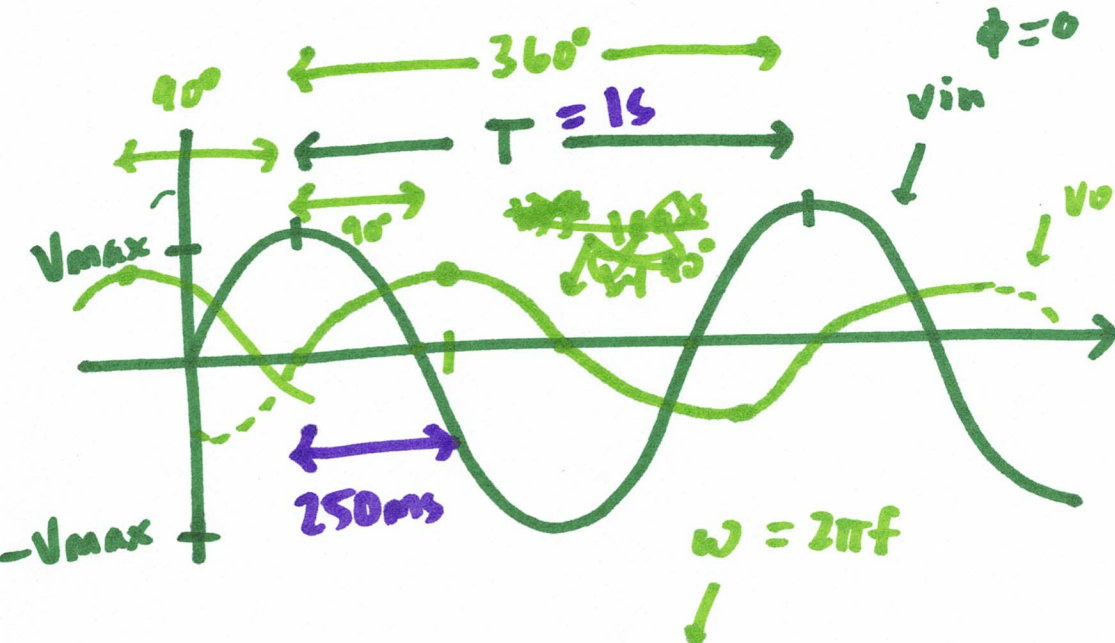


EE 220: Circuits I



$$T = \frac{1}{f} \leftrightarrow f = \frac{1}{T}$$

T (seconds/cycle)
f (cycles/second) (Hz)

$$\omega = 2\pi f$$

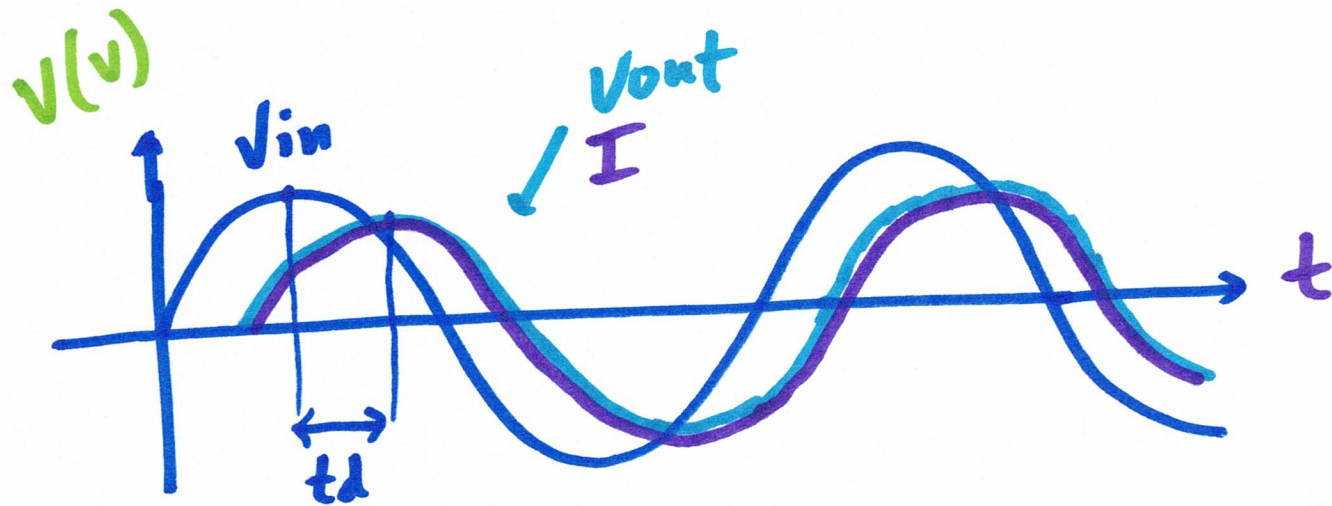
$$v(t) = V_{max} \cdot \sin(2\pi ft + \phi)$$

↑ phase shift ↔ time delay

$$\frac{\phi}{360^\circ} \cdot T = t_d$$

↑ period

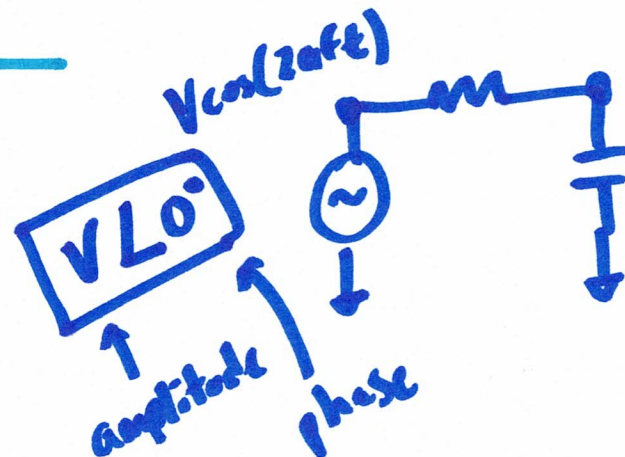
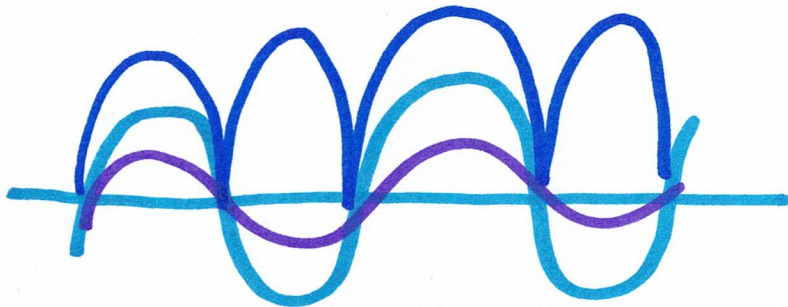
$$\frac{t_d}{T} \cdot 360^\circ = \phi$$



$$P = V \cdot I$$

$$\frac{t_d}{T} \cdot 360^\circ = \phi$$

- 1.) V_{out} lags V_{in} by ϕ
- 2.) V_{out} lags V_{in} by t_d
- 3.) V_{in} leads V_{out} by ϕ
- 4.) V_{in} leads V_{out} by t_d



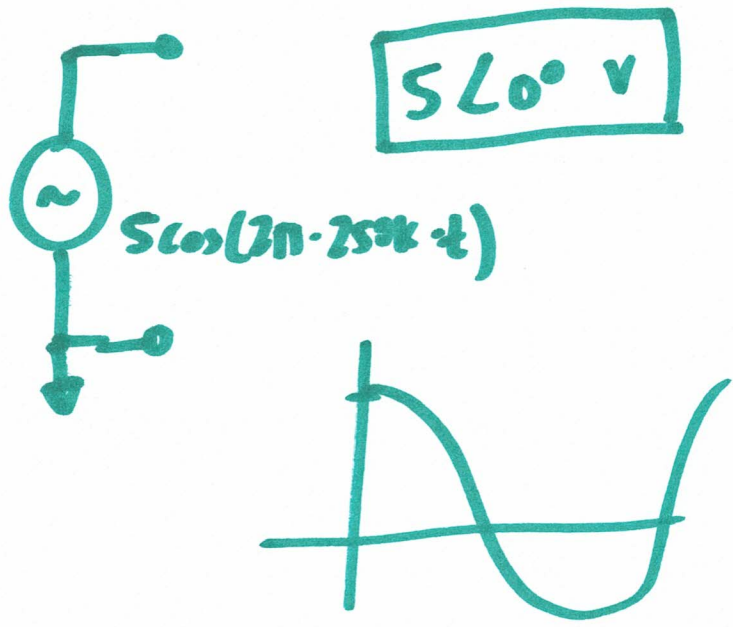
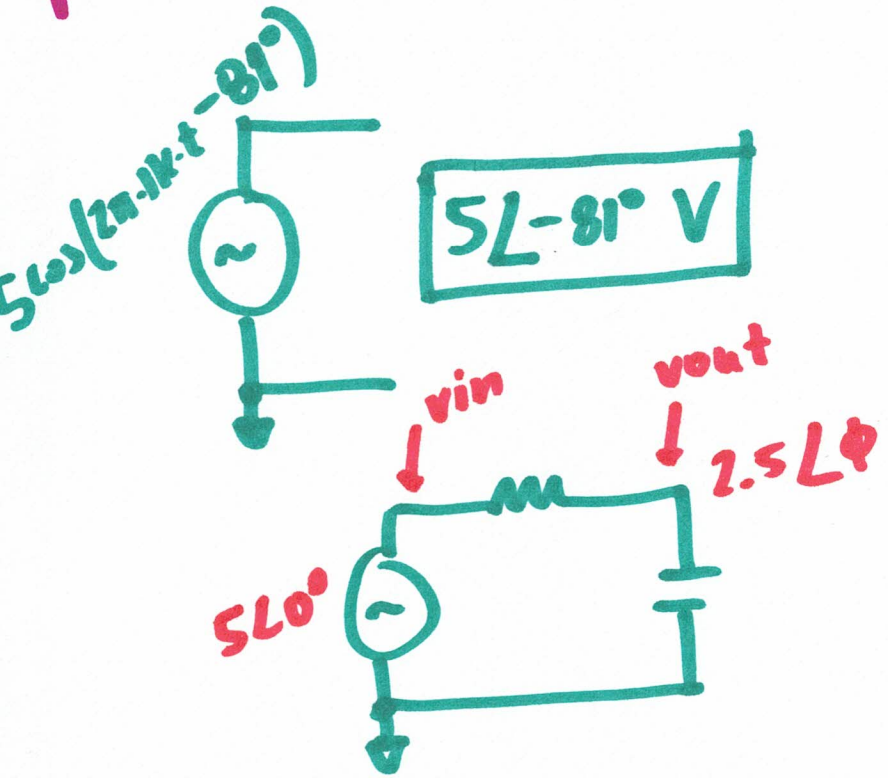
phasors

We will use cosine

4/18/2022
D. Stealy

time domain $\rightarrow V_A \cdot \cos(2\pi ft + \phi)$

phasor domain $\rightarrow V_A \angle \phi^\circ$

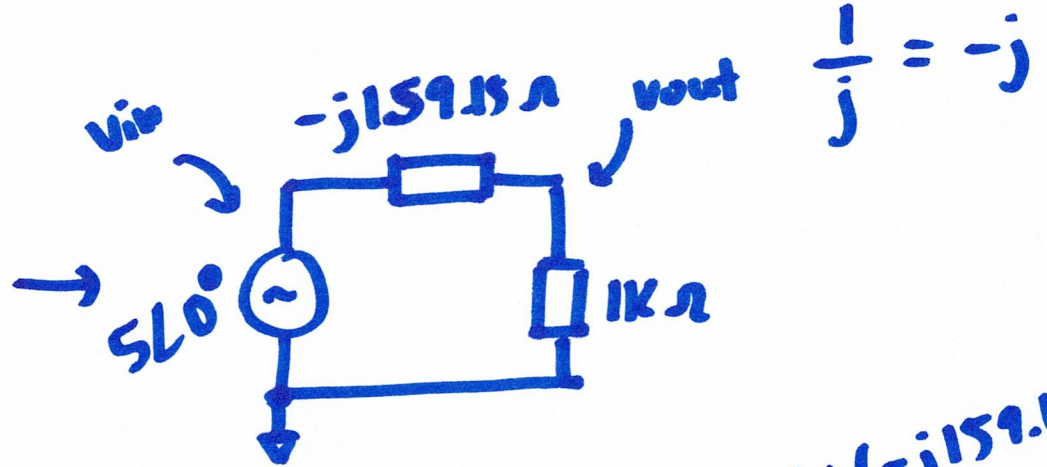
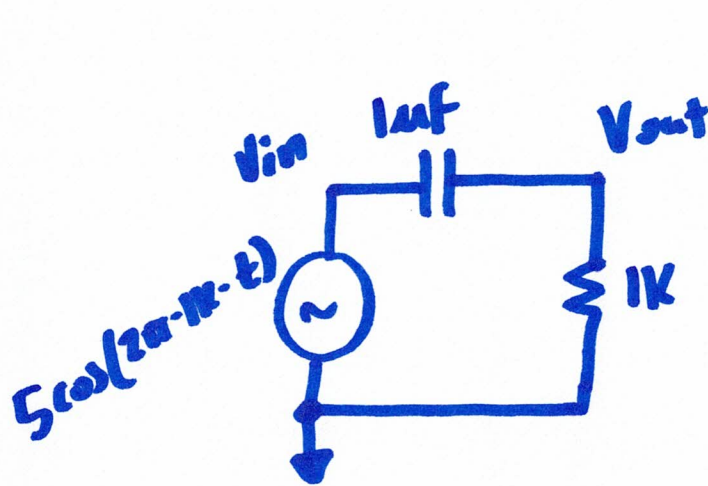


$$j = \sqrt{-1}$$

$$\text{---} \overset{R}{\text{---}} \text{---} \rightarrow Z_R = R(\Omega)$$

$$\text{---} \overset{C}{\text{---}} \text{---} \rightarrow Z_C = \frac{1}{j\omega C}, \omega = 2\pi f \rightarrow \frac{1}{j2\pi f C}(\Omega)$$

$$\text{---} \overset{L}{\text{---}} \text{---} \rightarrow Z_L = j\omega L, \omega = 2\pi f \rightarrow j2\pi f L(\Omega)$$



$$Z_C = \frac{1}{j \cdot 2\pi \cdot 1k \cdot 100\mu f} = \frac{159.15}{j} = -j159.15 \Omega$$

$$Z = x + iy$$

$$Z = x + jy$$

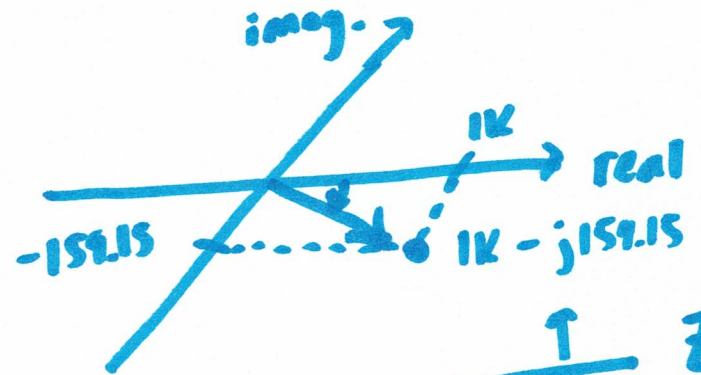
$$Z_T = 1k + (-j159.15)$$

$$Z_T = 1k - j159.15$$

\uparrow real \uparrow imaginary

$$z = x + jy$$

$$V = I \cdot R \rightarrow I = \frac{V}{R}$$



$$\sqrt{(\text{real})^2 + (\text{imag.})^2} = |z|_{\text{max}}$$

$$\boxed{\text{mag: } \sqrt{x^2 + y^2}}$$

$$\text{phase: } \tan(\theta) = \frac{y}{x}$$

$$\boxed{\text{phase: } \phi = \tan^{-1}\left(\frac{y}{x}\right)}$$