## Switched-mode Power Supply

Using On Semiconductor's 500 nm process
EE 421 Digital Electronics and Digital IC Design (Fall 2017)
Course Project
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## Intro

This project involves designing a CMOS switching-mode power supply (Buck converter) with off-chip inductor and capacitor to generate a constant voltage of 3.75 volts. The circuit should operate at power supply voltages of 4 to 5.5 volts and for load currents of 0 to 100 milliamps.

## Voltage Reference

The power supply's output voltage will be stabilized through the use of negative feedback. The output voltage will have to repeatedly be observed and compared to a voltage reference in order for the circuit to operate correctly. For this design a bandgap circuit was used for a voltage reference. This circuit generates a stable voltage reference of 1.25 volts that varies very little with changes in supply voltage and temperature. This is done by using a combination of PTAT and CTAT voltage references which when used together can create an almost invariable voltage. Using this voltage reference ensures that the output voltage of the power supply is compared to a constant voltage which will reduce the amount a variability in the output voltage.


## Selecting Inductor and Capacitor

The output of the MOSFET switches will be connected to an LC low-pass filter. The equations used to determine the values of the inductor and capacitor are shown below.
$V_{L}=L \frac{d i}{d t}$
$L=\frac{V_{L} \Delta t}{\Delta i}$
$L=\frac{\left(V D D-V_{o}\right) D \cdot T_{C L K}}{\Delta i}$
To select the value of the capacitor the following equations were used.
$I_{C}=C \frac{d V}{d t}$
$C=\frac{I_{C} \cdot \Delta t}{\Delta V}$
$C=\frac{I_{C} \cdot(1-D) \cdot T_{C L K}}{\Delta V}$
Initially a nominal operating frequency was arbitrarily chosen so that the equations above could be used. For this design the operating frequency was chosen at 10 MHz . Using this value as well as the duty cycle (D) for a VDD of 5 volts resulted in the following,
$L=\frac{(5-3.75)(0.75)}{(10 \mathrm{MHz})(1 \mathrm{~mA})}=93.8 u \mathrm{H}$
$C=\frac{(1 \mathrm{~mA}) \cdot(0.25)}{(10 \mathrm{MHz})(1 \mathrm{mV})}=25 \mathrm{nF}$
The inductor value was rounded up to 100 uH and the capacitor was increased to 250 nF . After performing some simulations, these values were found to be too low as the operating frequency of the power supply was in the 100 kHz range.
The final components were selected through some trial and error with some intuition from analyzing the output as an RLC circuit. The final components chosen were a 4.7 uF capacitor and a $470 \mu \mathrm{H}$ inductor.

| Current Ripple |  |  |
| :--- | :--- | :--- |
|  | $F=100 \mathrm{kHz}$ | $\mathrm{F}=1 \mathrm{MHz}$ |
| $\mathrm{VDD}=4 \mathrm{v}$ | 4.99 mA | $499 \mu \mathrm{~A}$ |
| $\mathrm{VDD}=5.5 \mathrm{v}$ | 25.4 mA | 2.54 mA |

*assuming $I_{C}=1 \mathrm{~mA}$

| Voltage Ripple |  |  |
| :--- | :--- | :--- |
|  | $\mathrm{F}=100 \mathrm{kHz}$ | $\mathrm{F}=1 \mathrm{MHz}$ |
| VDD $=4 \mathrm{v}$ | 133 uV | 13.3 uV |

> | VDD $=5.5 \mathrm{v}$ | $677 \mathrm{uV} \quad 67.7 \mathrm{uV}$ |
| :--- | :--- | :--- |

## Comparator Design

To determine the difference between the output voltage and the desired voltage, a comparator was used. Through the use of feedback, the output of the power supply is fed into the input of a comparator through a voltage divider with a gain of ( $1 / 3$ ) producing a voltage of 1.25 volts. This voltage is compared to the bandgap voltage which is also 1.25 volts. Any difference between the inputs of the comparator will be amplified through the comparators. The comparator design used is shown below.


A self-biasing PMOS comparator was used for this design. The PMOS differential pair was chosen over the NMOS differential pair because its common-mode voltage range extends lower to ground which is appropriate when the input voltages to the comparator will be at 1.25 volts.

Because the gain of the individual comparator was roughly 20, four stages were cascaded to increase the overall gain. Increasing this gain means that the comparator will be able to detect smaller differences between the output and the voltage reference resulting in smaller ripple voltage. The drawback to using multiple stages is that there will be an increased amount of delay through the feedback loop. This could mean having an operating frequency that is lower than desired. To work around this, the device sizes were kept at minimum length for high speed operation.

Inverters were placed on the output of the comparator so that it would be able to switch the output MOSFET either 'on' or 'off'. Since the output of the comparator swings closer to ground, the switching point of these inverters was lowered by increasing the strength of the NMOS and decreasing the strength of the PMOS. Also, a second inverter was implemented to sharpen the transition from low-to-high or high-to-low so that it can approximate an ideal inverter.


Pictured above is the output buffer of the comparator and a simulation showing its lowered switching point voltage of 1.2 volts and a steep transition from low-to-high.


The performance of the comparator with output buffer was simulated while varying the power supply voltage and temperature. From the results above, the gain increases with the power supply and the increases in temperature produce very small to no decreases in gain.

## Lockout Circuit

During the switching of the NMOS and the PMOS, there is point where both devices are on. This causes a significant spike of unwanted contention current to flow through both devices. This causes power to be dissipated across the MOSFETs thus reducing the efficiency of the circuit. To solve this, a lockout circuit was designed which would ensure that the MOSFETs were never in the 'in between' state by turning off one device before turning on the other.
The schematic of the lockout circuit is shown below.


## Sizing the PMOS and NMOS switches

When determining the size of the output MOSFETs, the switching resistance had to be considered. The transistors had to be capable of supplying up to 100 mA while maintaining a low voltage drop from drain to source (or source to drain). The following calculations were used to size the PMOS transistor.

$$
R_{P}^{\prime}=40 k \frac{L}{W}
$$

For a VDD of 4.5 v , the voltage across the PMOS at full current load is approximately,

$$
\begin{aligned}
& V_{s d}=4.5-4.2=0.3 v \\
& R_{P}=\frac{V_{s d}}{I}=0.3 / 0.1=3 \Omega
\end{aligned}
$$

Using the switching resistance of the PMOS one can then solve for the width of the device assuming minimum length.
$W=\frac{40 k}{3}=13333$
Actual Width $=13333(0.6 \mathrm{um})=8000 \mathrm{um}$

Adjusting this width so that it is a multiple of 0.6 um and using 100 parallel devices, the final device width is,

$$
W(\text { actual })=80.4 u m \text { with } M=100
$$

Since the switching resistance for the NMOS is half that of the PMOS, the device width of the NMOS was chosen to be,
$W($ actual $)=40.2 u m$ with $M=100$

## Transient Response

The transient response of the output voltage can be approximated as an RLC circuit where the resistance (R) is the switching resistance of the NMOS or PMOS.
The transfer function of this circuit is shown below,

$$
\frac{V \text { out }}{\text { Vin }}=\frac{(1 / L C)}{s^{2}+(R / L) s+(1 / L C)}=\frac{\omega_{n}^{2}}{s^{2}+2 \zeta \omega_{n}+\omega_{n}^{2}}
$$

Equating the approximated transfer function to the 2nd Order transfer function equation we get,

$$
\begin{aligned}
& \omega_{n}=1 / \sqrt{L C} \\
& \zeta=\frac{1}{2} \sqrt{\frac{R^{2} C}{L}}
\end{aligned}
$$

Using the device sizes above led to transient responses that had a very large overshoot. One effort made to reduce this was to obtain a ratio between the capacitor and the inductor that would yield a critically damped response $(\zeta=1)$. Using the switching resistances of the devices $(3 \Omega)$, and setting the damping ratio to one yielded a ratio of,
$C=0.444 L$

Although the final values selected for the inductor and capacitor don't adhere to the above ratio, the overshoot was still greatly reduced by trying component values near this ratio. This approach also helped further understand the transient response of the power supply.

## Driving the switches

Increasing the sizes of the output MOSFETS means that their input capacitance has also increased. This input capacitance serves as a large load capacitance to the inverters in the lockout circuit. Simply connecting the lockout circuit directly into the gates of the devices won't be enough to switch the MOSFETs on and off. A set of buffers must be designed to go after the lockout circuit and before the output MOSFETs.
Starting from the sizes of the output MOSFETs, each previous stage's size was decreased by a factor of eight until the standard inverter size of $12 \mathrm{u} / 6 \mathrm{u}$ was reached. A total of two inverters were added so that there wouldn't be any inversion between the lockout circuit and the gates of the MOSFETs.

The drivers schematic is shown below,


## Power Supply Circuit

The switch mode power supply was finally assembled with all the previous circuits as shown below.


In the feedback loop, a voltage divider consisting of three $25 \mathrm{k} \Omega$ resistors was used to generate the gain of $1 / 3$. The total resistance of $75 \mathrm{k} \Omega$ ensures that the amount of current drawn by the feedback loop is $50 \mu \mathrm{~A}$. In addition, the value of these resistors also affects the delay since there is an RC delay from the parallel combination of the resistors and the input capacitance of the comparator. Selecting the resistors at $25 \mathrm{k} \Omega$ keeps the delay small while only drawing the maximum allowable current of $50 \mu \mathrm{~A}$.

Capacitors ( 3 pF ) were added across the resistors in the feedback loop to further reduce the delay across the loop. An additional 6 pF capacitor was placed from the output of the bandgap voltage reference to ground to reduce any ripple due to noise from the comparator. This improved the design by reducing the output voltage ripple.

## Simulations

The final design was simulated using the schematic shown below.


The above simulation shows a parametric analysis where the power supply voltage is held at 4 volts while varying the temperature and the load current. From this plot one can see the underdamped transient response at the start of the simulation. Because of this, the output voltage overshoots to 5 volts.


Shown above is the zoomed in view of the previous simulation for better clarity. Using this plot the following data was recorded.

| vdd | Temp <br> (celsius) | Load Current | Vavg | Voltage <br> ripple (v) | Freq. (Hz) | $\mathrm{T}(\mathrm{s})$ |
| ---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 4 | 0 | 1 uA | 3.7495 | $68.8 \mu$ | 439 k | $2.28 \mu$ |
| 4 | 0 | 100 mA | 3.7495 | $105.4 \mu$ | 284 k | $3.52 \mu$ |
| 4 | 50 | 1 uA | 3.742 | $182.6 \mu$ | 273 k | $3.66 \mu$ |
| 4 | 50 | 100 mA | 3.742 | $313.2 \mu$ | 157 k | $6.38 \mu$ |
| 4 | 100 | 1 uA | 3.727 | $528.1 \mu$ | 164 k | $6.11 \mu$ |
| 4 | 100 | 100 mA | 3.727 | $960.1 \mu$ | 86.2 k | $11.6 \mu$ |

At a VDD $=4 \mathrm{v}$, the power supply generates a voltage of 3.74 volts with minimal voltage ripple. In the worst case the ripple voltage varies by just under 1 mV at full load and at 100 degrees celsius. The operating frequency also stays around 100 kHz which was on the low end of the desired frequency range.
Regarding temperature, the average output voltage seems to decrease with increases in temperature.

The same simulation was run again at the maximum power supply voltage of 5.5 volts.


This simulation again show the underdamped transient response at the start of the power supply. This time the output voltage overshoots to 6 volts.

A zoomed in view of this simulation is shown below along with a table of data collected from the simulation.


Shown above is a zoomed in view of the simulation with VDD $=5.5 \mathrm{v}$.

| vdd | Temp <br> (celsius) | Load <br> Current | Vavg | Voltage <br> ripple (v) | Freq. <br> $(\mathrm{Hz})$ | $\mathrm{T}(\mathrm{s})$ |
| :---: | :---: | :---: | :---: | :---: | :--- | :--- |
| 5.5 | 0 | 1 uA | 3.762 | $15 \mu$ | 2.08 M | 481 n |
| 5.5 | 0 | 100 mA | 3.762 | $15 \mu$ | 2.08 M | 481 n |
| 5.5 | 50 | 1 uA | 3.7533 | $26.1 \mu$ | 1.558 M | 642 n |
| 5.5 | 50 | 100 mA | 3.7533 | $26.7 \mu$ | 1.558 M | 642 n |
| 5.5 | 100 | 1 uA | 3.7379 | $53.7 \mu$ | 1.130 M | 885 n |
| 5.5 | 100 | 100 mA | 3.7379 | $53.7 \mu$ | 1.096 M | 912 n |

At a VDD of 5.5 volts the power supply generates a more stable output voltage with voltage ripples in the tens of microvolts. The operating frequency is also in the MHz range.
Once again, increases in the operating temperature caused the average output voltage to drop by tens of millivolts.

## Efficiency vs. Current load (VDD=4)



| vdd=4 | temp=0 | temp=100 |
| :--- | ---: | ---: |
| current <br> load | efficiency | efficiency |
| 1 u | 0.03 | 0.03 |
| $25 m$ | 89.52 | 89.51 |
| 50 m | 93.59 | 93.62 |
| 75 m | 94.65 | 93.24 |
| 100 m | 94.84 | 94.83 |

The chart above shows a plot of the power supply's efficiency with varying current loads at a VDD of 4 volts. From the data in the chart, we see that the efficiency is generally at or over $90 \%$ with loads that draw at least 25 mA . The best efficiency achieved was $94.83 \%$ at full load current.

The efficiency didn't change much with changes in temperature but higher temperatures yielded slightly less efficiencies.

Efficiency vs. Current Load (VDD=5.5)


| vdd=5.5 | temp=0 | temp=100 |
| :--- | :--- | :--- |
| current load | efficiency | efficiency |
| 1 u | 0.01 | 0.01 |
| 25 m | 69.22 | 68.85 |
| 50 m | 81.02 | 80.81 |
| 75 m | 85.73 | 85.5 |
| 100 m | 88.03 | 87.79 |

The chart above plots the efficiency of the power supply with varying current load at a VDD of 5.5 volts. At this VDD, the efficiencies drop to around 70 to $80 \%$ with a peak efficiency of $88.04 \%$ at full load. In this chart we can see again that the efficiencies decreased slightly with increases in temperature.

## Conclusion

Regarding the performance of the design, the efficiency of the power supply at a VDD of 5.5 volts has some room for improvement. An optional addition that could help the efficiency is by implementing zero voltage switching. The operating frequency of the power supply might have also been improved by reducing the number of stages in the comparator and increasing the gain by using higher length devices for the current source.
Overall the project helped me learn a lot about how buck converters worked and it helped reinforced was I learned in the lecture class.

## Layouts:

Bandgap Voltage Reference


| Pins | Location |
| :--- | :--- |
| vdd! | top ntap rail |
| gnd! | ptaps on the diodes |
| Vref | left side of top-most electrode resistor |

Comparator with Output inverters


| Pins | Location |
| :--- | :--- |
| vdd! | top ntap rail |
| gnd! | bottom ptap rail |
| plus | pmos gate m1_poly on the far left |
| minus | pmos gate m1_poly on the left |
| out | horizontal metal_1 wire on the right |

Inverters on the output of the comparator


| Pins | Location |
| :--- | :--- |
| vdd! | top ntap rail |
| gnd! | bottom ptap rail |
| in | left m1_poly connection |
| out | m1 wire joining the inverters on the right |

Lockout Circuit


| Pins | Location |
| :--- | :--- |
| vdd! | top ntap rail |
| gnd! | bottom ptap rail |
| ip | left $\mathrm{m} 2 \_\mathrm{m} 1 \_$poly connection on gate of first inverter |
| opn | right $\mathrm{m} 2 \_\mathrm{m} 1$ connection just under the nwell |
| opp | right m 2 wire just above the NMOSs |

Drivers


| Pins | Location |
| :--- | :--- |
| vdd! | top ntap rail |
| gnd! | bottom ptap rail |
| in1 | left-most m1_poly on first inverter |
| out1 | metal_1 joining the left side inverters together. |
| in2 | middle of layout. Just above the middle NMOS. |
| out2 | metal_1 joining the right side inverters together. |



Dimensions/value of Resistor:
Width: 1.2 um
Length: 25.8 um
Extracted resistance: 25.63 k
3 pF Capacitor


Dimensions/value of Capacitor:
Width: 58.8 um
Length: 58.35 um
Extracted capacitance: 2.738 pF

## Switch-mode Power Supply



| Pins | Location | info |
| :---: | :---: | :---: |
| vdd! | top ntap rail |  |
|  | bottom ptap rail under output NMOS |  |
| gnd! | ptaps around diodes in bandgap |  |
| out | horizontal metal_1 wire on right between the PMOS and NMOS | connects to inductor |
| Vout | metal_2 square on right side of bottom-most capacitor | connects to inductor and capacitor |



## DRC and LVS results for the final layout:

```
DRC started, +.+.+. Sun Nov 26 20 #17%50 2017
    completed ++++Sun Nov 26 20;17 %51 2017
    CPU TIME = 00 #00 #00 TOTAL TIME = 00 #00 %01
********* Summary of rule violations for cell "smps layout" **********
    Total errors found; 0
Net-list summary for /home/arteag1/CMOSedu/LVS/schematic/1
    count
                5 9 ~ n e t s
                4 terminals
                    15 res
                    4 cap
                    9 diode
                    37 pmos
                    32 nmos
            Terminal correspondence points
            N57 N8 Vout
            N55 N1 gnd!
            N58 N5 out
            N56 NO vod!
Devices in the netlist but not in the rules:
    res diode
Devices in the rules but not in the netlist;
    nfet pfet nmos4 pmos4
7 \text { net-list ambiguities were resolved by random selection.}
The net-lists match.
```

