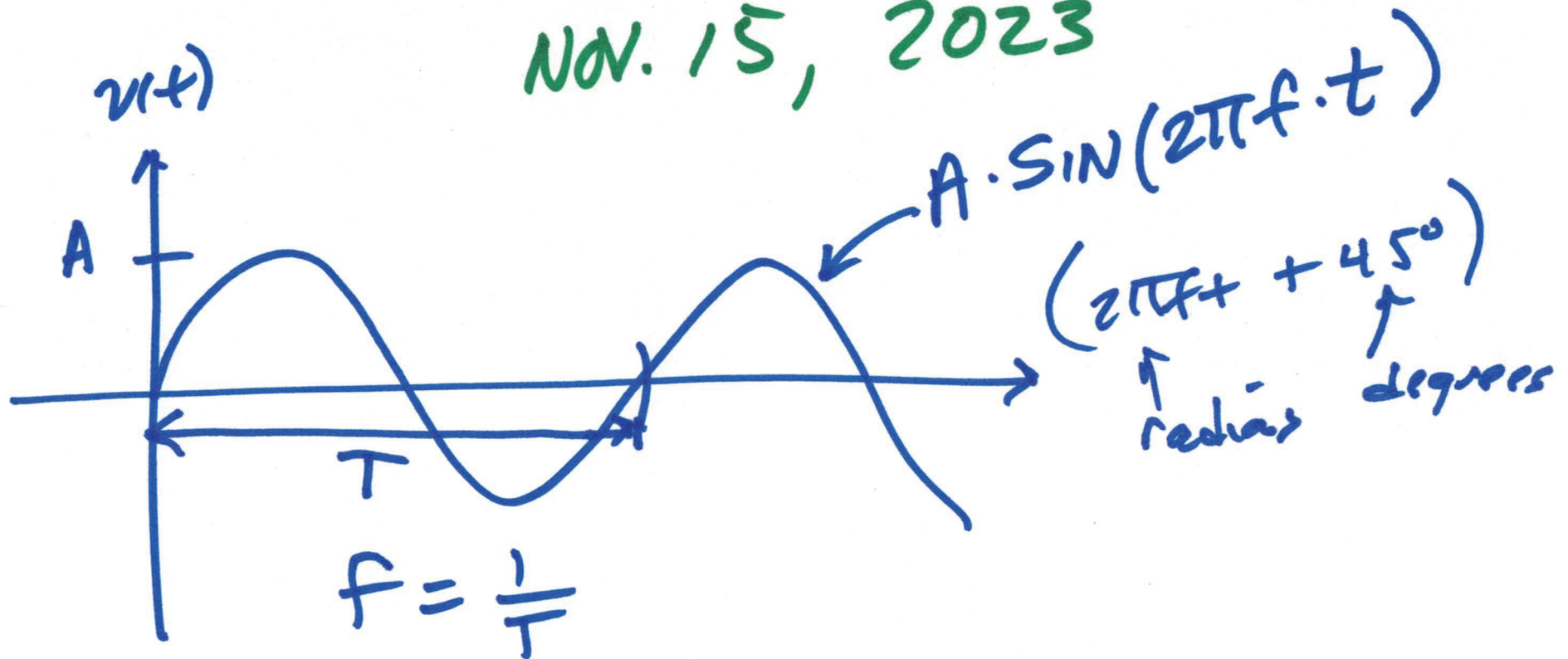


EE 220 Circuits I

Lecture 21

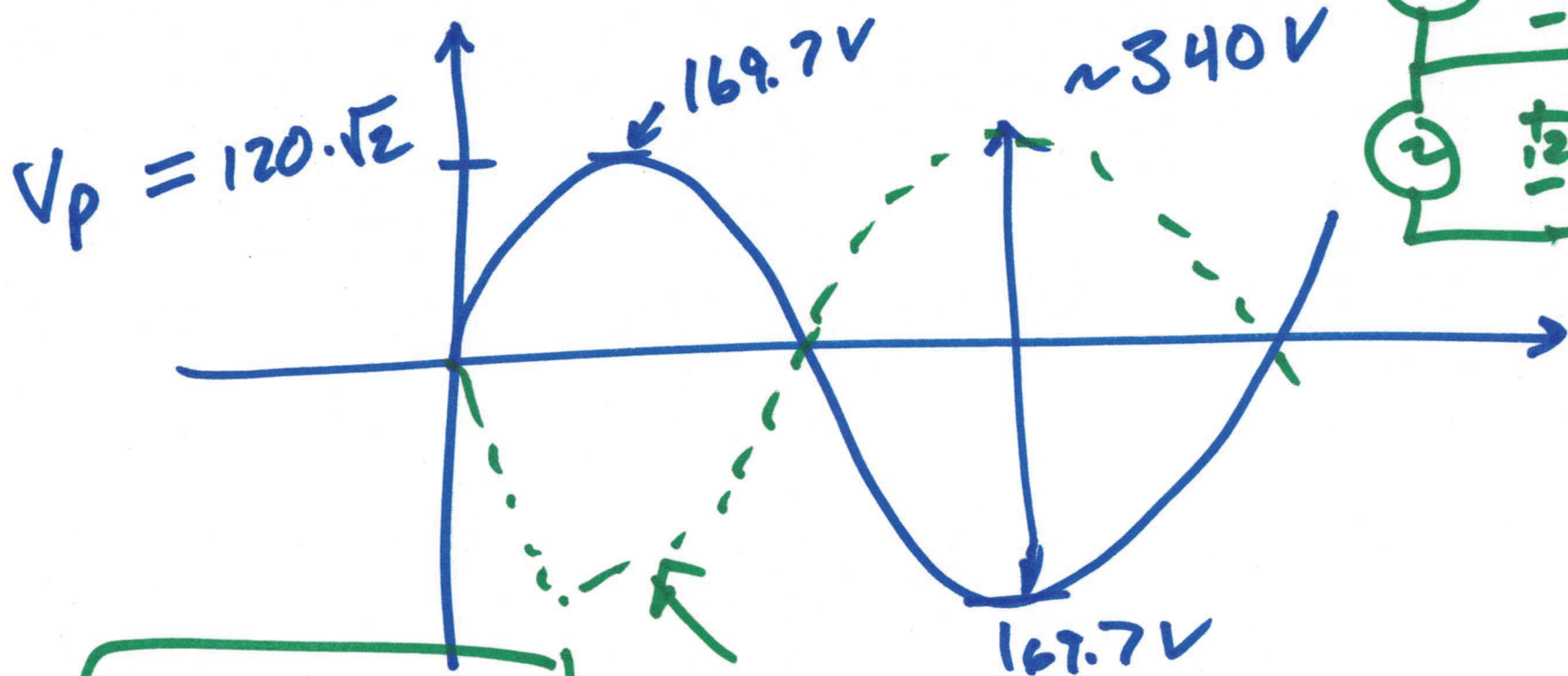
Nov. 15, 2023



$$f = 60 \text{ Hz}, T = 16.67 \text{ ms}$$

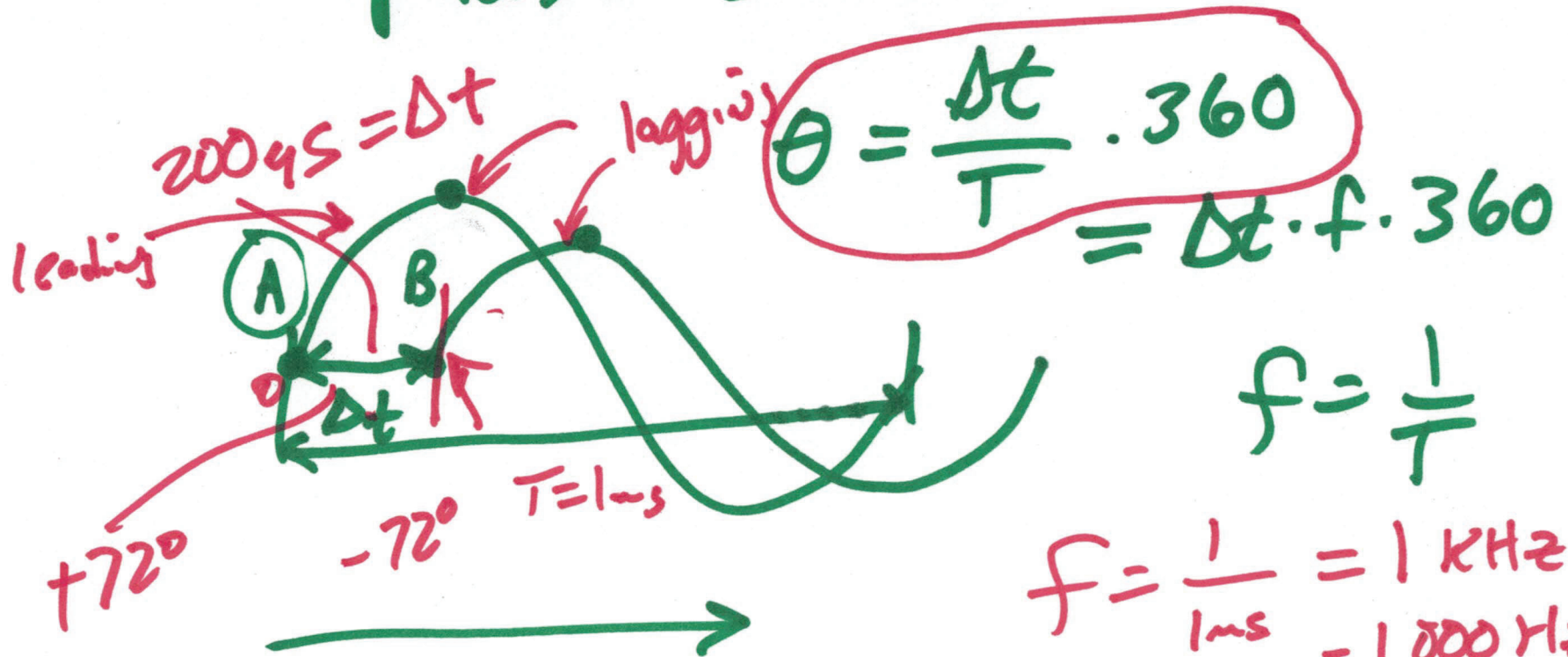
Root Mean Square (RMS)

120 V RMS



$$\frac{V_p}{\sqrt{2}} = V_{\text{RMS}}$$

Phase shift

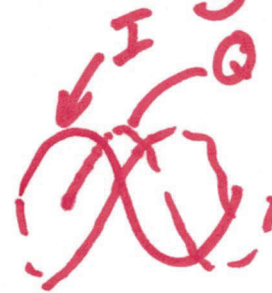


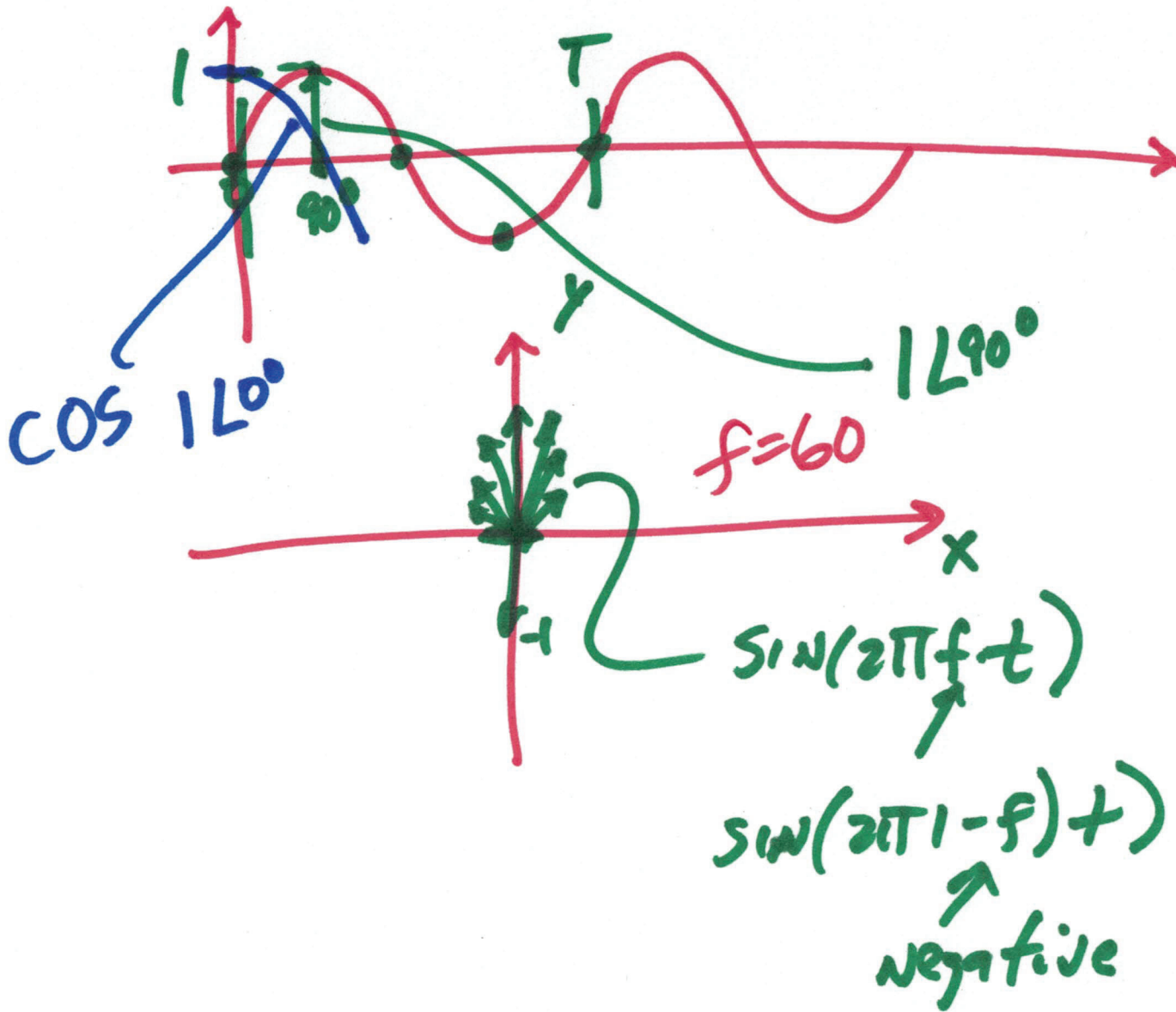
$$\theta = \frac{\Delta t}{T} \cdot 360 = \Delta t \cdot f \cdot 360$$

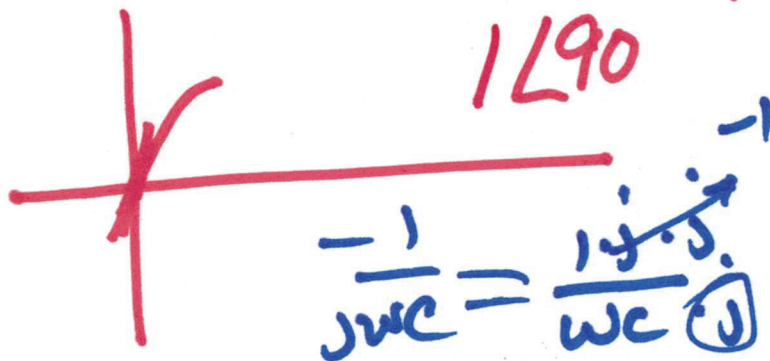
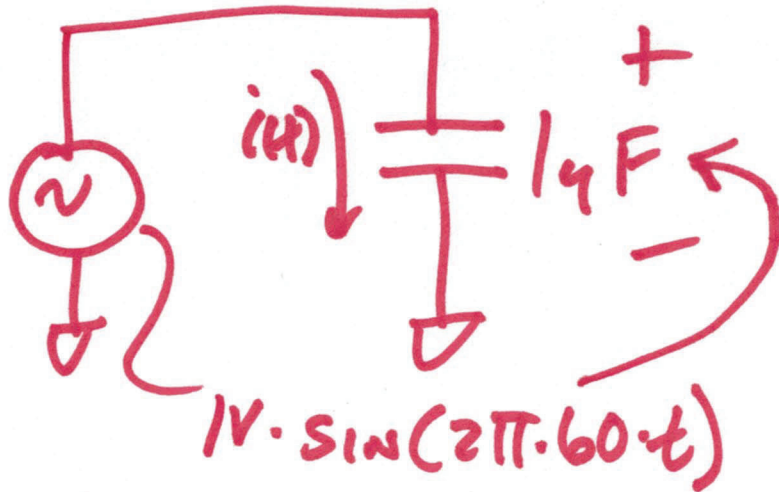
$$f = \frac{1}{T}$$

$$f = \frac{1}{1 \text{ ms}} = 1 \text{ kHz} = 1,000 \text{ Hz}$$

$$\theta = \frac{200 \mu s}{1,000 \mu s} \cdot 360 = \frac{360}{5} = \underline{\underline{72^\circ}}$$







$\omega = 2\pi f$
 ↑
 omega
 RADIANS / SEC

$$i = C \frac{dv}{dt} \quad \text{if } 90^\circ$$

$$i(t) = C \cdot 2\pi 60 \cos(2\pi 60 t)$$

$$\frac{1}{\omega C} = 10^{-6} \cdot 2\pi \cdot 60 \cdot \cos(\uparrow)$$

$\omega C = 2\pi f$

$$i(t) = 377 \mu A \cos(\uparrow)$$

$$I(j\omega) = \frac{C \cdot 2\pi 60 \cdot 100}{C \cdot \omega}$$

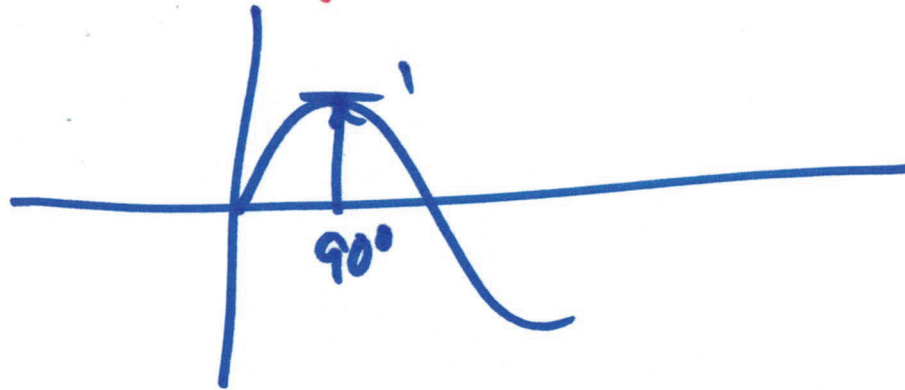
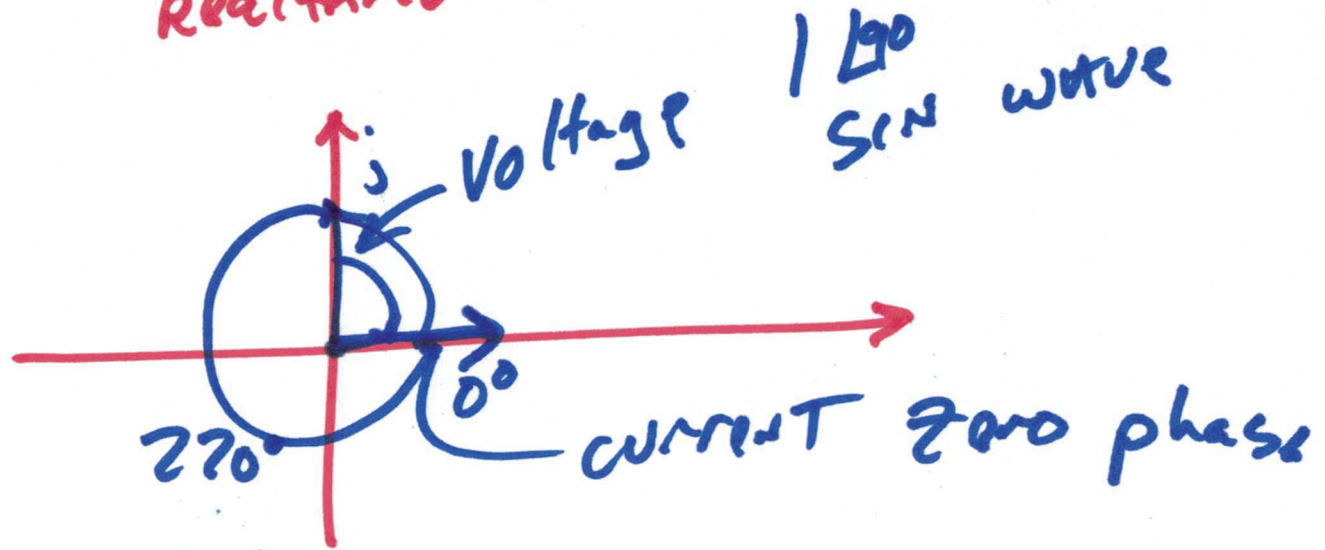
$$V = I \cdot Z$$

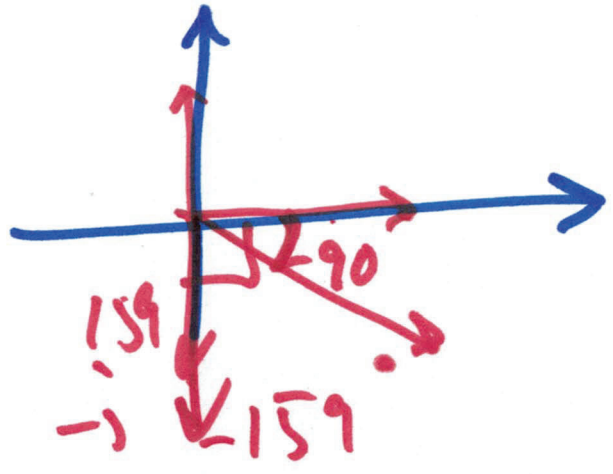
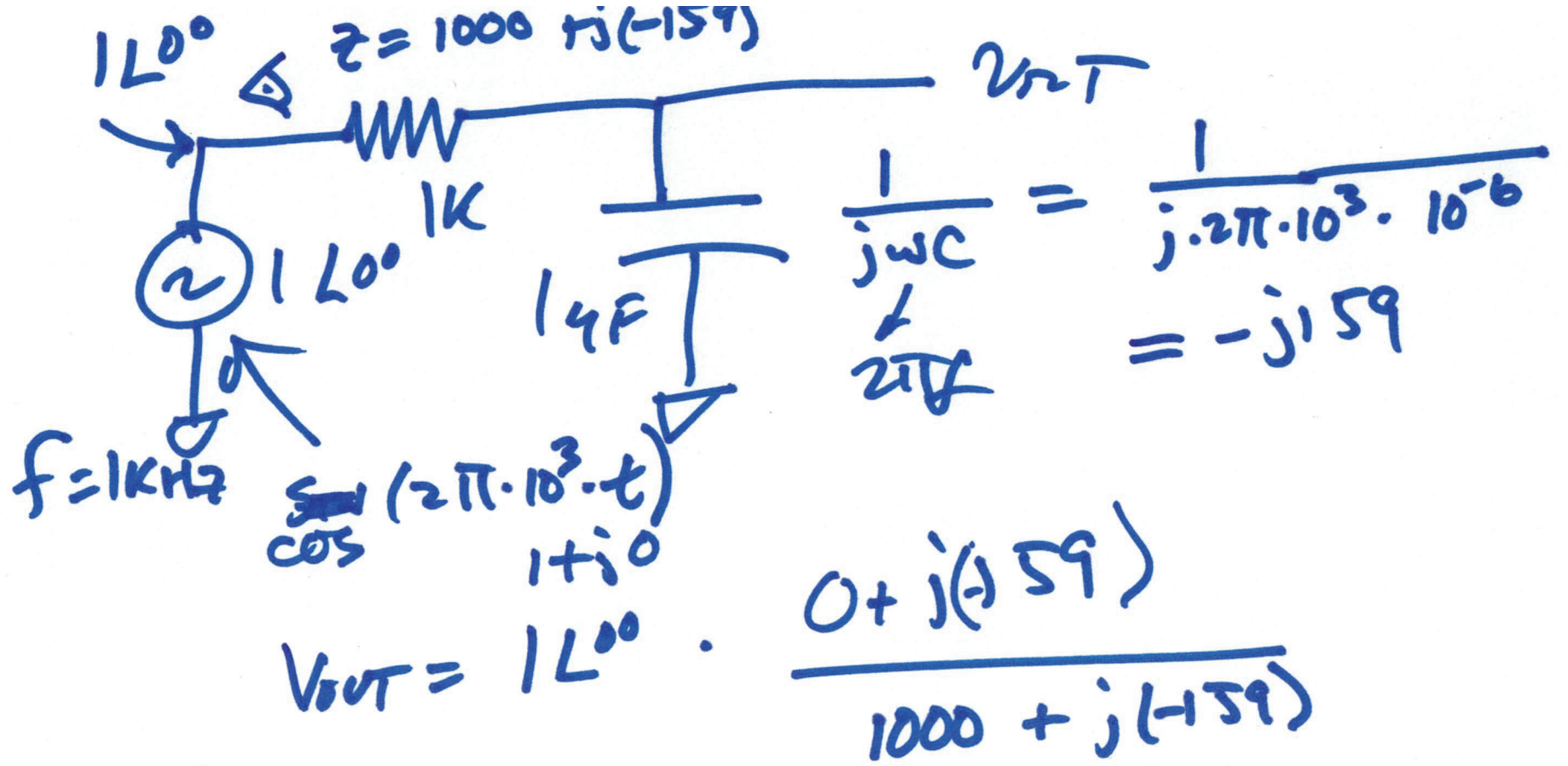
↑
impedance
(Resistance + Reactance)

$$Z = \frac{1}{j\omega C}$$

$$Z_C = \frac{1}{j\omega C} = \frac{1}{j2\pi fC}$$

↑
Reactance





$V_{out} = 1\angle 0^\circ \cdot j159 \angle -90^\circ$
 $V_{out} = \frac{1\angle 0^\circ \cdot 159 \angle -90^\circ}{\sqrt{(1000)^2 + (-159)^2} \angle \tan^{-1} \frac{-159}{1000}}$

$$V_{out} = \frac{120 \cdot 159 \angle -90}{1012 \angle -90}$$

$$V_{out} = .157 \angle -90 - (-90)$$

$$0.157 \angle -81^\circ$$

$$\begin{array}{l} \uparrow \\ \text{lagging} \end{array} -81 = \frac{\Delta t}{1ms} \cdot 360$$
$$\Delta t = 225 \mu s$$