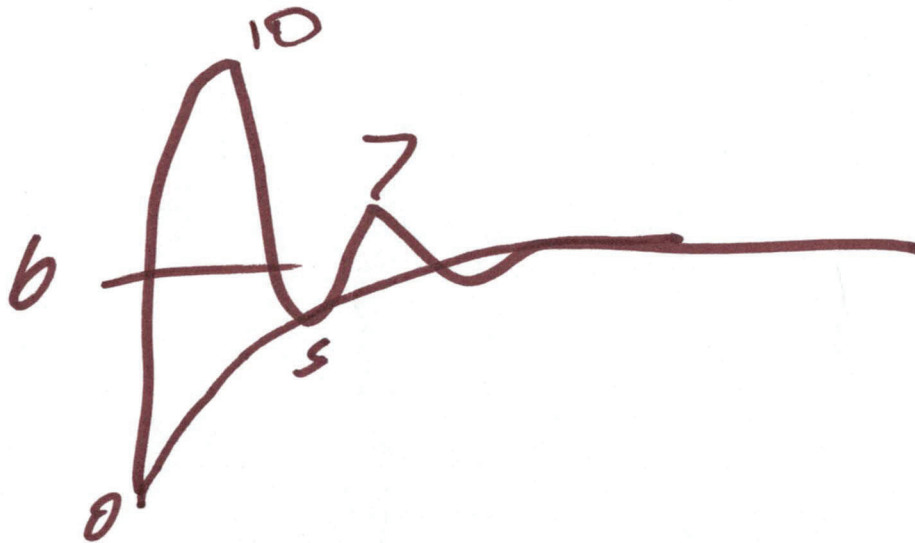
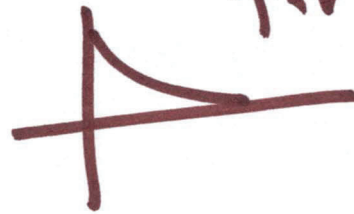


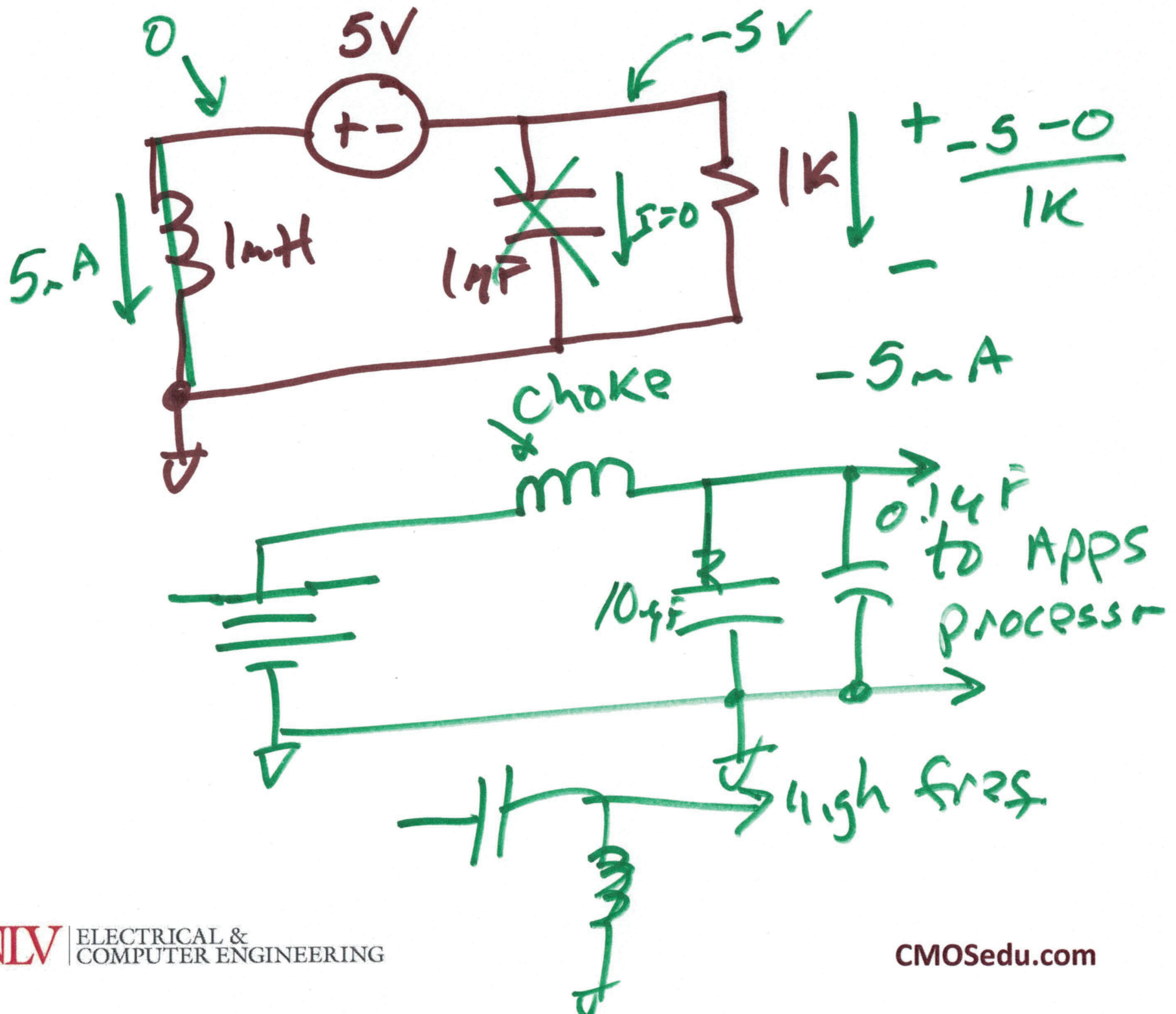
EE 220 CIRCUITS I

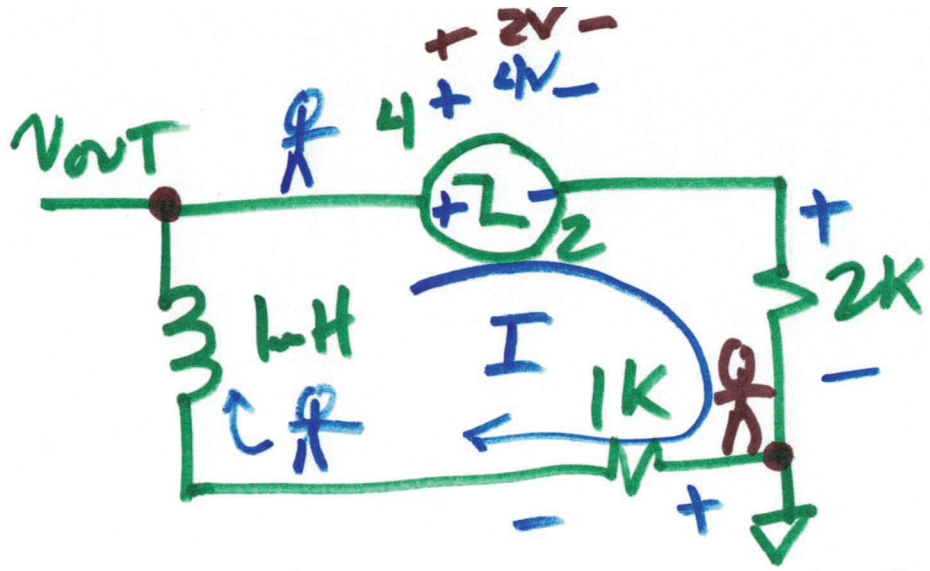
Nov. 1, 2023

Lecture 18

first-order
response







$$v_{OUT} = ?$$

$$\tau = \frac{L}{R} = \frac{3\text{mH}}{1\text{k} + 2\text{k}} = \frac{1}{3} \frac{\text{m} \cdot 10^{-3}}{\text{k} \cdot 10^3} = \frac{1}{3} \mu\text{s}$$

$$-4 - 2\text{k}I_I - 1\text{k}I_I = 0$$

$$-3\text{k}I_I = 4\text{V}$$

$$I_I = -\frac{4}{3} \mu\text{A}$$

$$i(t) = i_f + (i_i - i_f)e^{-t/\tau}$$

$$= -\frac{2}{3} \mu\text{A} + \left(-\frac{4}{3} \mu\text{A} - \left(-\frac{2}{3} \mu\text{A}\right)\right)e^{-t/(\frac{1}{3}\mu\text{s})}$$

$$= -\frac{2}{3} \mu\text{A} - \frac{2}{3} \mu\text{A} e^{-t/(\frac{1}{3}\mu\text{s})}$$

$$i(t) = -\frac{2}{3} \mu\text{A} (1 + e^{-t/(\frac{1}{3}\mu\text{s})}) = -666 \mu\text{A}$$

3)

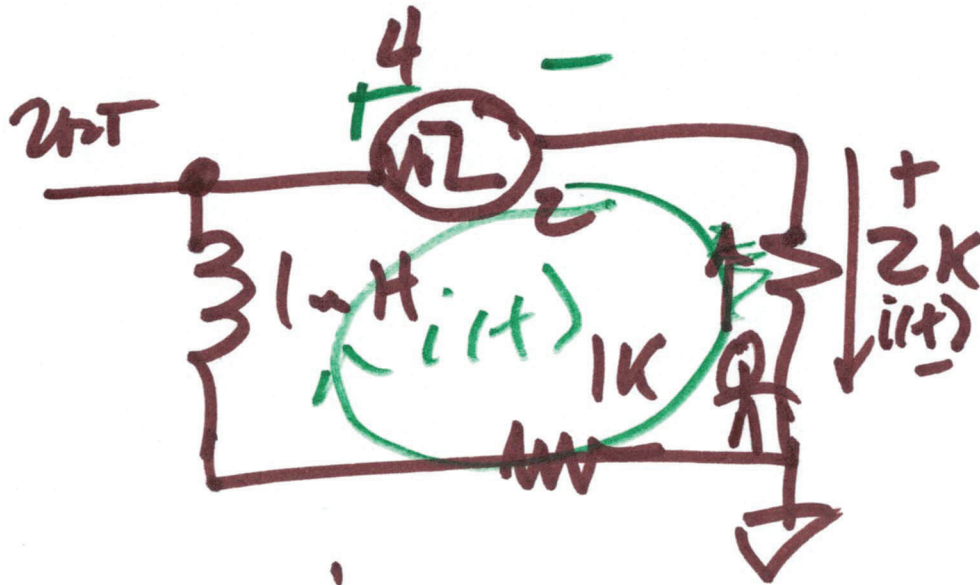
$$i(t) = -\frac{2}{3} \text{ mA} (1 + e^{-(t-24\text{s})/0.334})$$

$$t \geq 24$$

$$t \leq 24$$

$$i(t) = \frac{-4}{3} \text{ mA}$$

$$= -1.33 \text{ mA}$$



$$V = L \cdot \frac{di}{dt}$$

$$v_{2k} = 2k i(t) + 2$$

$$= 2k \left(-\frac{2}{3} \text{ mA} (1 + e^{-(t-24)/0.334}) \right) + 2$$

$$v_{2k} = -\frac{4}{3} \text{ V} + \frac{-4}{3} e^{-(t-24)/0.334} + 2$$

$$v_{UT} = -\frac{4}{3}V + \frac{6}{3}V - \frac{4}{3}e^{-(t-24)/\tau}$$

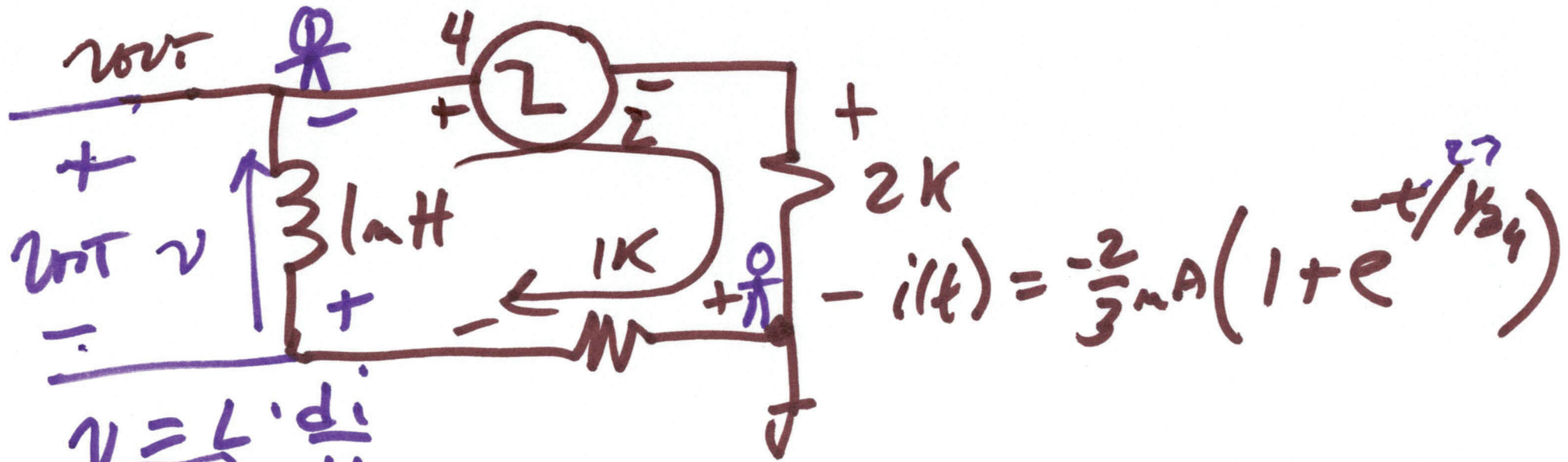
$$= \frac{2}{3}V - \frac{4}{3}e^{-(t-24)/\tau}$$

$$v_{UT}(24) = -\frac{2}{3}V$$

$$v_{UT}(\infty) = \frac{2}{3}V$$

$$e^{-\infty} = 0$$

$$\frac{1}{e^{\infty}} = 0$$



$$-i(t) = -\frac{2}{3} \text{mA} \left(1 + e^{-t/134} \right)$$

$$v = L \cdot \frac{di}{dt}$$

$$\frac{d}{dx} e^{-ax} = -ae^{-ax}$$

$$20V = -1k \cdot i(t) - 1mH \cdot \frac{di(t)}{dt}$$

$$= \frac{2}{3}V + \frac{2}{3}e^{-(t-20)/134} - 1mH \left(\frac{d}{dt} \left(-\frac{2}{3}mA - \frac{2}{3}mA \right) \right)$$

$-1mH \left(-\frac{2}{3}mA \right)$ see next page

b)

$$\frac{d}{dt} \left(-\frac{2}{3} \mu A - \frac{2}{3} \mu A e^{-(t-2\mu)/\tau_{3\mu}} \right)$$

$$= 0 - \frac{2}{3} \mu A \left(-\frac{1}{\tau_{3\mu}} \right) e^{-(t-2\mu)/\tau_{3\mu}}$$

$$\frac{1}{\tau_3} = 3$$

$$\frac{d}{dt} \left(-\frac{2}{3} \mu A e^{+2\mu} e^{-t/\tau_{3\mu}} \right)$$

$$d \left(-\frac{2}{3} \mu A e^{+2\mu} e^{-3\mu t} \right)$$

$$\frac{d}{dt} \left(-\frac{2}{3} \mu e^{+2\mu} (-3\mu) e^{-3\mu t} \right)$$

$$v_{out}(t) = -1k \cdot i(t) - 1mH \cdot \frac{di(t)}{dt}$$

$$= -1k \cdot \left(-\frac{2}{3} \mu A (1 + e^{-t/134}) \right) - 1mH \frac{di(t)}{dt}$$

$$= \frac{2}{3} V (1 + e^{-t/134}) - 1mH \frac{di(t)}{dt}$$

$$\frac{d e^{-ax}}{dx} = d e^{-ax} \cdot \frac{d-ax}{dx}$$

$$-1mH \frac{di(t)}{dt} = -1mH \frac{d}{dt} \left(-\frac{2}{3} \mu A - \frac{2}{3} \mu A e^{-t/134} \right)$$

$$= -1mH \left(-\frac{2}{3} \mu A \right) \cdot \left(\frac{1}{134} \right) e^{-t/134}$$

$$= -2 e^{-t/134}$$

$$v_{out} = \frac{2}{3} \left(1 + e^{-t/\tau} \right) - 2e^{-t/\tau}$$

a)