

Lecture 1! Extra!

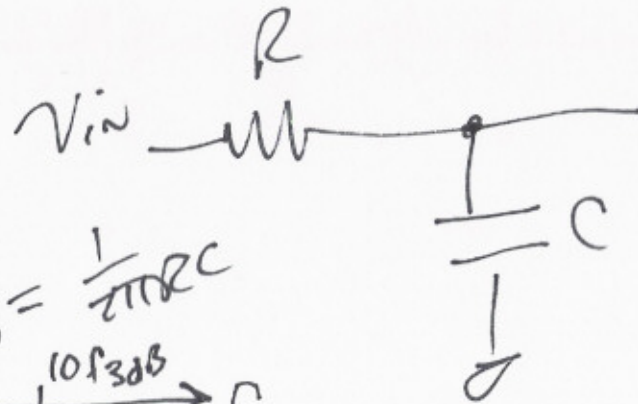
Analogs &

SEC. 4.3, digital Filtering.

1.2 kHz $\xrightarrow{10 \times}$ 12 kHz $\xrightarrow{2 \times}$ 24 kHz

Lowpass RC

$$V_{out} = V_{in} \cdot \frac{1}{j\omega C + R}$$

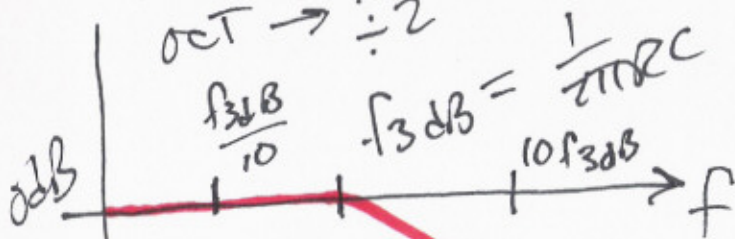


$$\frac{V_{out}}{V_{in}} = \frac{1 + j0}{1 + j\omega RC}$$

$$\left| \frac{V_{out}}{V_{in}} \right| = \frac{1}{\sqrt{1 + (\pi f RC)^2}}$$

$$\angle \frac{V_{out}}{V_{in}} = 0 - \tan^{-1} \frac{2\pi f RC}{1}$$

-6dB $\rightarrow \frac{1}{2}$
 +6dB $\rightarrow \times 2$
 OCT $\rightarrow \times \div 2$



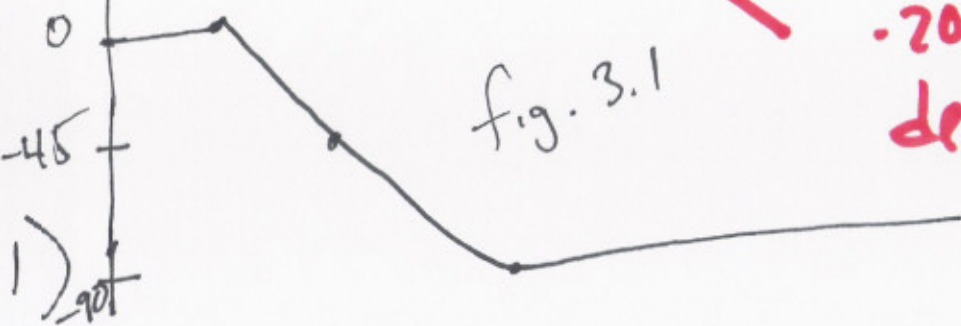
$-20 \frac{dB}{dec}$

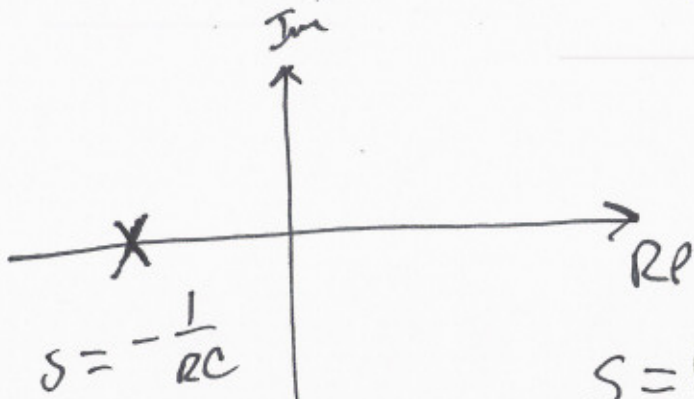
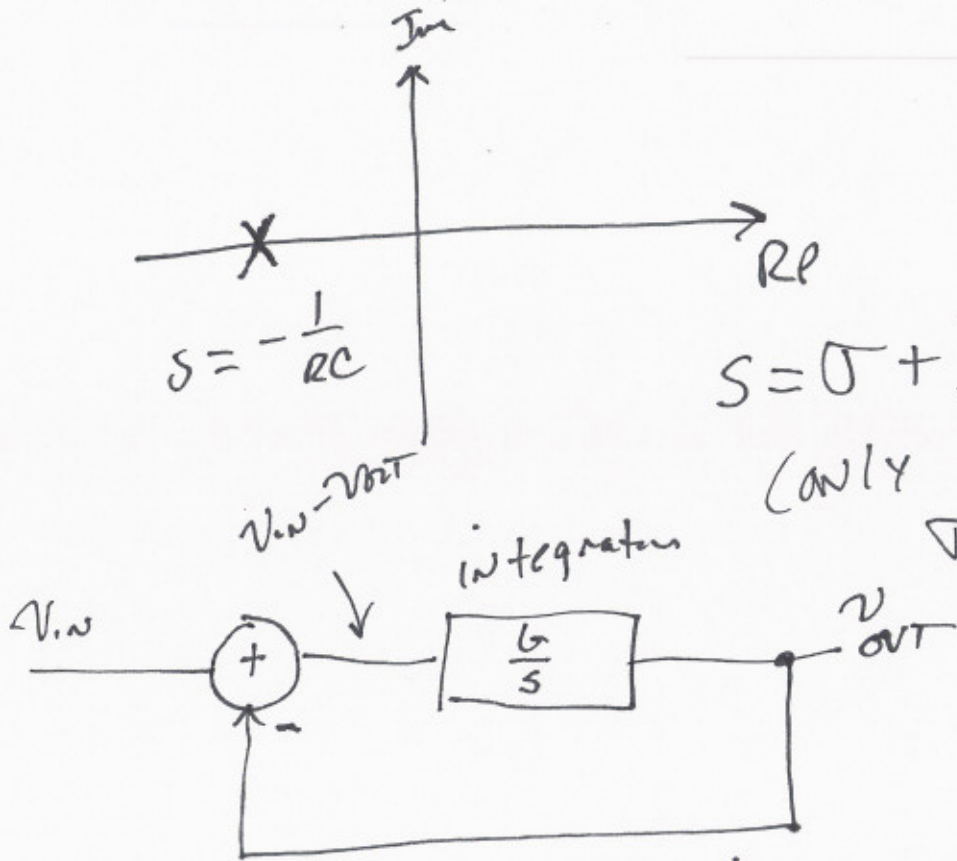
$-20 dB \rightarrow \frac{1}{10}$

dec $\rightarrow \times 10$

$$\frac{1}{\sqrt{1 + \left(\frac{f}{f_{3dB}}\right)^2}}$$

fig. 3.1





$$s = \sigma + j\omega$$

(ONLY SINUSOIDS)

$$\sigma = 0, s = j\omega$$

$$\frac{1}{1 + j\omega RC}$$

$$= \frac{1}{1 + sRC}$$

where is the pole?



$$s = -\frac{1}{RC}$$

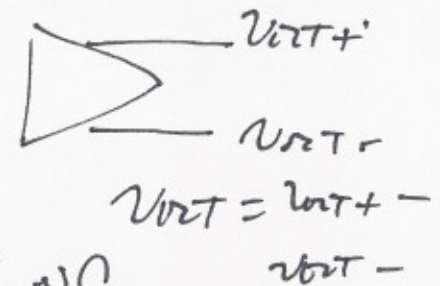
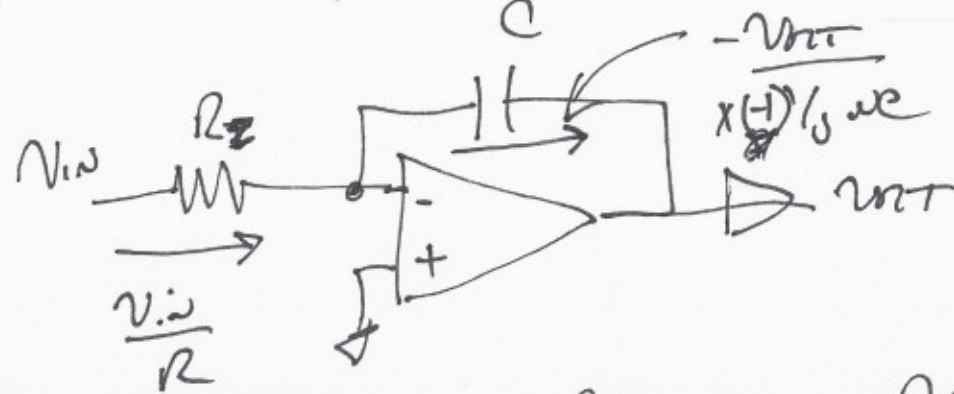
$$v_{out} = (v_{in} - v_{out}) \cdot \frac{G}{s}$$

$$v_{out} \left(1 + \frac{G}{s}\right) = \frac{v_{in} \cdot \frac{G}{s}}{1}$$

$$\frac{v_{out}}{v_{in}} = \frac{\frac{G}{s}}{1 + \frac{G}{s}} = \frac{1}{1 + \frac{s}{G}}, G = \frac{1}{RC}$$

2)

Miller integrator, active RC integrator, etc.



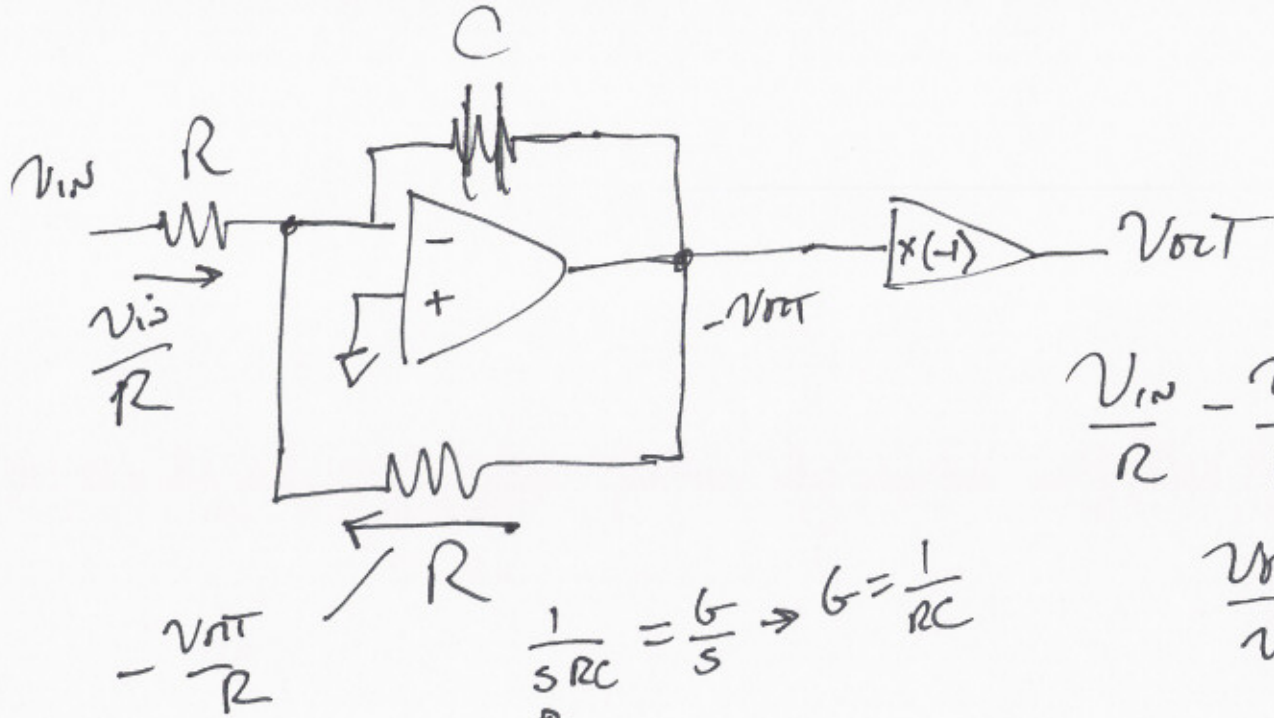
$$\frac{v_i}{R} = -v_{oT} \cdot j\omega C$$

$$\frac{v_{oT}}{v_i} = -\frac{1}{j\omega RC} = \frac{-1}{sRC}$$

$$\left| \frac{v_{oT}}{v_i} \right| = \left| \frac{1}{j\omega RC} \right| = \left| \frac{1}{sRC} \right|$$

$$\frac{G}{s} = \frac{1}{sRC} \Rightarrow$$

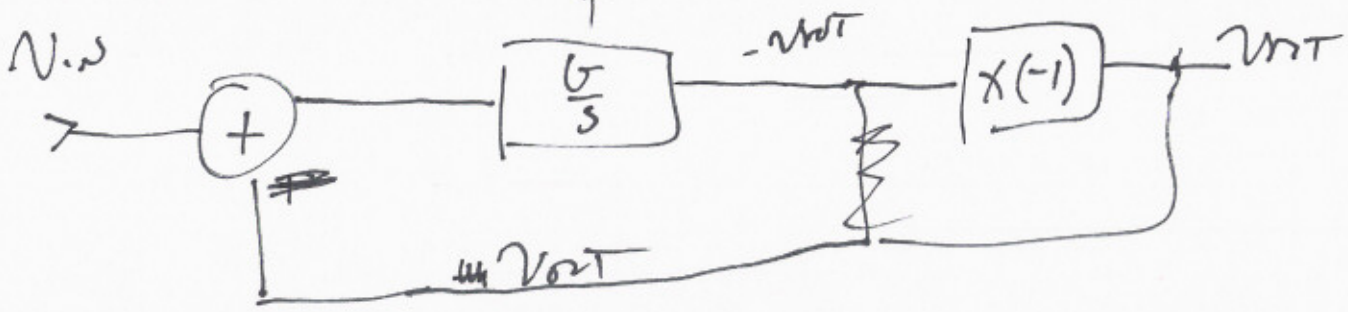
$$G = \frac{1}{RC}$$



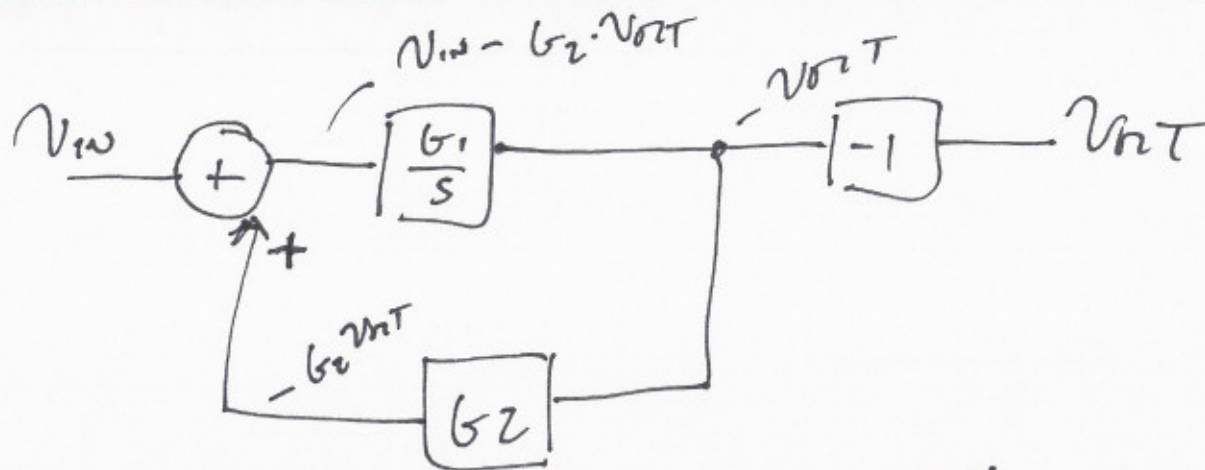
$$\frac{v_{in}}{R} - \frac{v_{out}}{R} = -v_{out} \cdot j\omega C$$

$$\frac{v_{out}}{v_{in}} = \frac{1}{1 + j\omega RC}$$

$$\frac{1}{sRC} = \frac{G}{s} \Rightarrow G = \frac{1}{RC}$$



4)



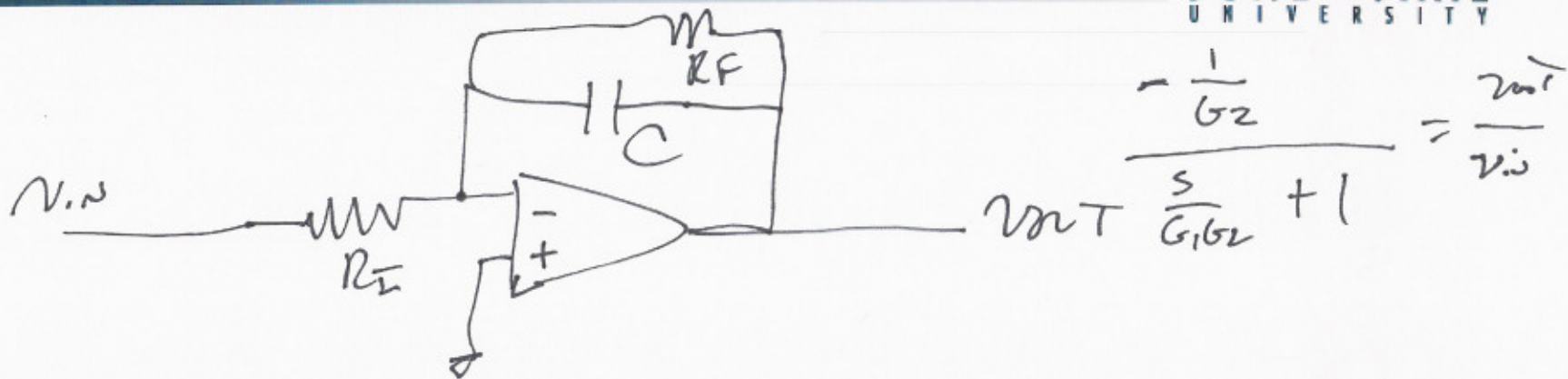
$$+V_{out} = \frac{G_1}{s} (V_{in} - G_2 V_{out})$$

$$V_{out} \left(1 + \frac{G_1 G_2}{s} \right) = \frac{G_1}{s} \cdot V_{in}$$

$$\frac{V_{out}}{V_{in}} = \frac{\frac{G_1}{s}}{1 + \frac{G_1 G_2}{s}}$$

$$\text{Low frequency Gain} = \frac{1}{G_2} = \frac{\frac{1}{G_2}}{\frac{s}{G_1 G_2} + 1}$$

5)



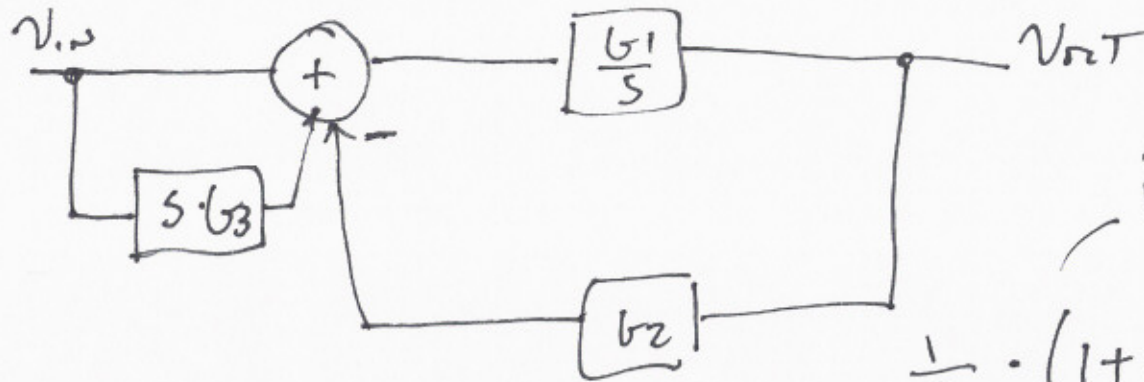
$$\frac{R_F \cdot \frac{1}{j\omega C}}{R_F + \frac{1}{j\omega C}} = \frac{R_F}{1 + j\omega C R_F}$$

$$\frac{v_o(s)}{v_i(s)} = \frac{-R_F}{R_I} \cdot \frac{1}{1 + j\omega C R_F}$$

$$G_2 = \frac{R_I}{R_F} \qquad \frac{1}{G_1 G_2} = s C R_F$$

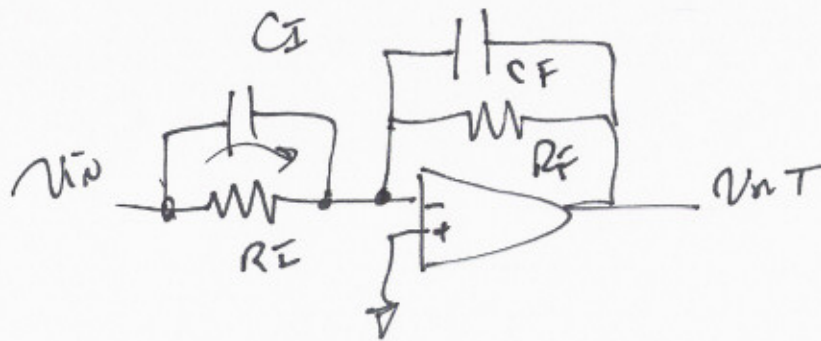
$$G_1 = \frac{1}{R_I \cdot C}$$

b)



Bilinear

$$\frac{\frac{1}{G_2} \cdot \left(1 + \frac{s}{Y_{G3}}\right)}{1 + \frac{s}{G_1 G_2}} = \frac{v_{out}}{v_{in}}$$



$$G_1 = \frac{1}{R_I \cdot C_I}$$

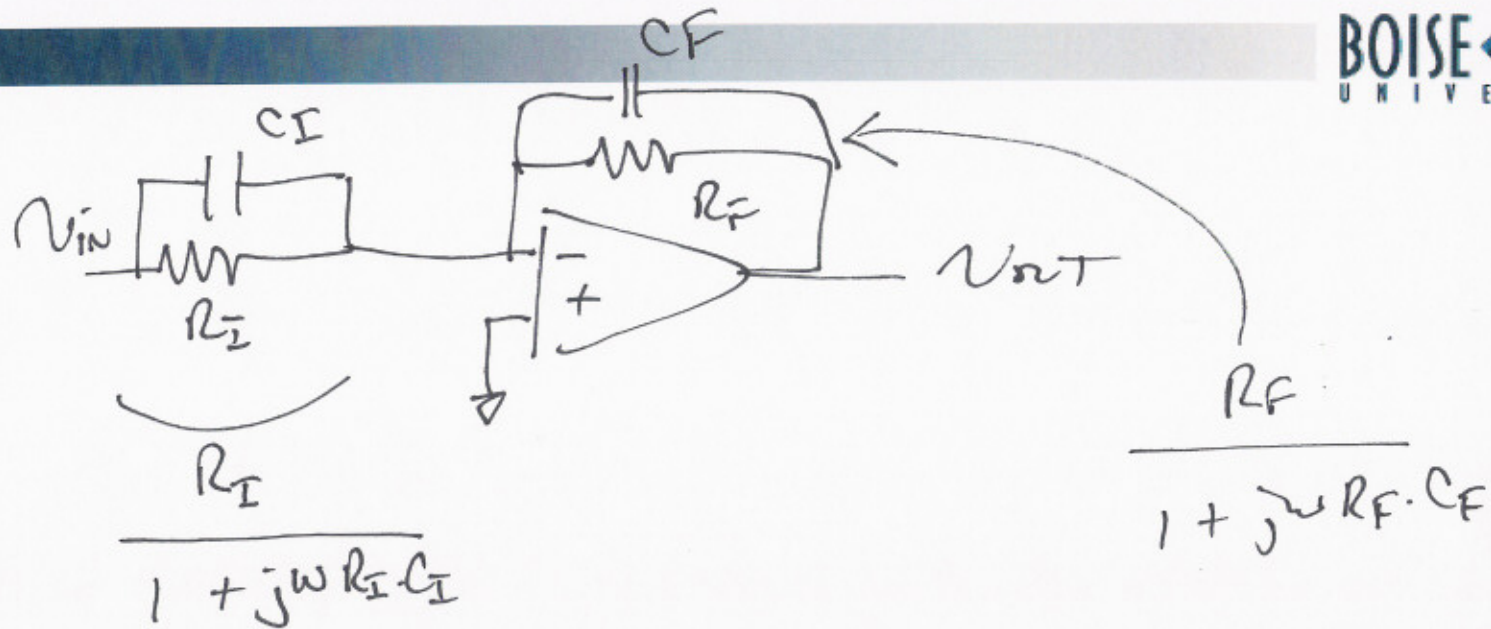
$$G_2 = \frac{R_I}{R_F}$$

$$\frac{v_{in}}{1/j\omega C_I} = j\omega C_I \cdot v_{in} = v_{in} \cdot s \cdot C_I$$

$$\frac{v_{in}}{R_I} \rightarrow v_{in} \left(\frac{1}{R_I} + s C_I \right)$$

$$G_3 = R_I \cdot C_I$$

7)



$$\frac{V_{out}}{V_{in}} = - \frac{R_F}{R_I \cdot (1 + j\omega R_F C_F)}$$

$$f_z = \frac{1}{2\pi R_I C_I}$$

$$f_p = \frac{1}{2\pi R_F C_F}$$

$$= - \frac{R_F}{R_I} \cdot \frac{1 + j\omega R_I C_I}{1 + j\omega R_F C_F} = \frac{R_F}{R_I} \frac{1 + j \frac{f}{f_z}}{1 + j \frac{f}{f_p}}$$

8)

Biquad

$$\frac{V_{out}}{V_{in}} = \frac{a_2 s^2 + a_1 s + a_0}{s^2 + \left(\frac{2\pi f_0}{Q}\right)s + (2\pi f_0)^2}$$

Fig. 3.35

Fig. 3.39

lowpass

$$a_2 = a_1 = 0$$

BANDpass

$$a_2 = a_0 = 0$$

highpass

non-zero

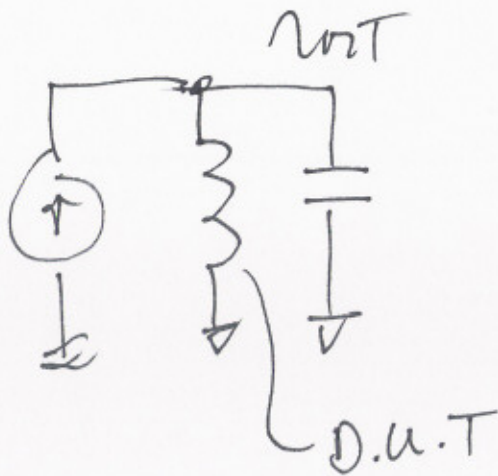
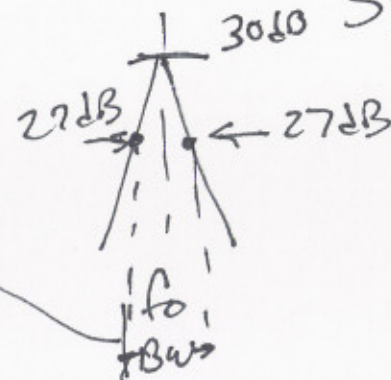
Know Q!

$\frac{\text{energy stored}}{\text{energy lost}}$

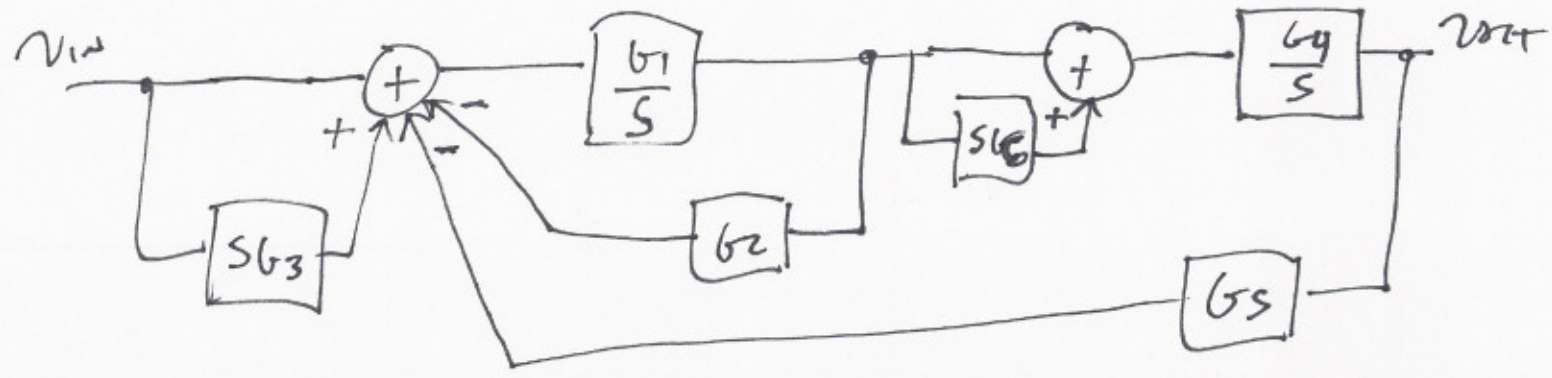
IN a resonant

30dB System

$$Q = \frac{f_0}{Bw}$$



9)



$$\frac{v_{out}}{v_{in}} = \frac{\overbrace{s^2 \cdot b_1 b_3 b_4 b_6}^{a_2 \text{ Biquad}} + \overbrace{s(b_1 b_3 b_4 + b_1 b_4 b_6)}^{a_1} + \overbrace{b_1 b_4}^{a_0}}{s^2 + \underbrace{s(b_1 b_2 + b_1 b_4 b_5 b_6)}_{\frac{2\pi f_0}{Q}} + \underbrace{b_1 b_4 b_5}_{(2\pi f_0)^2}}$$

$$Q = \frac{f_0}{\Delta \omega}$$

10)