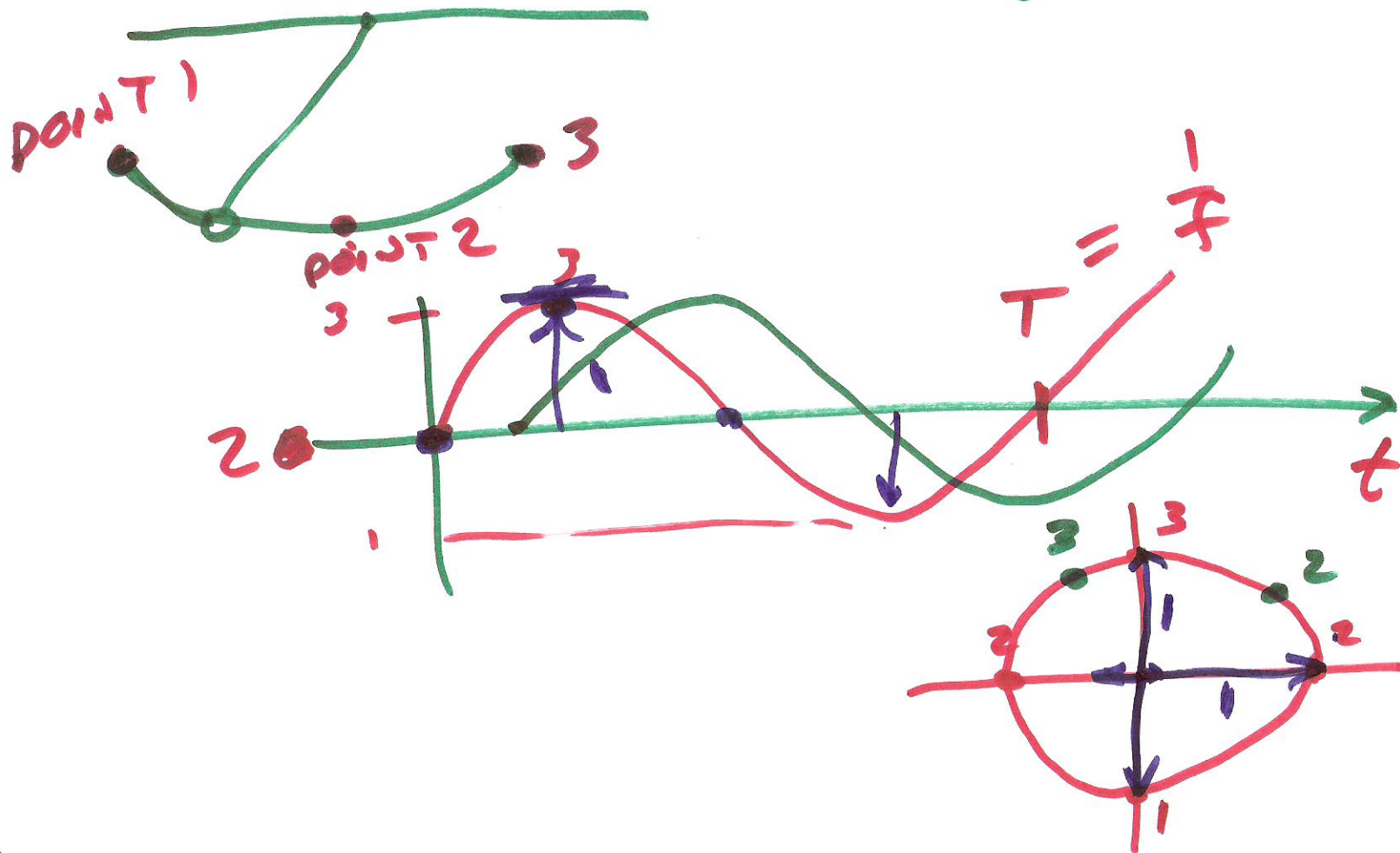
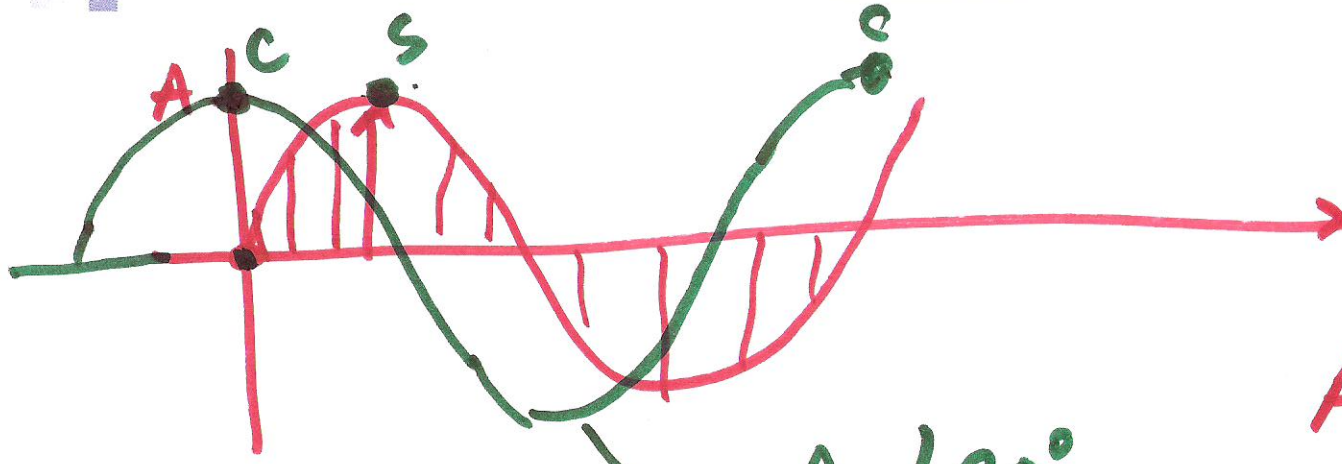


Lecture 2

Aug. 23, 2010



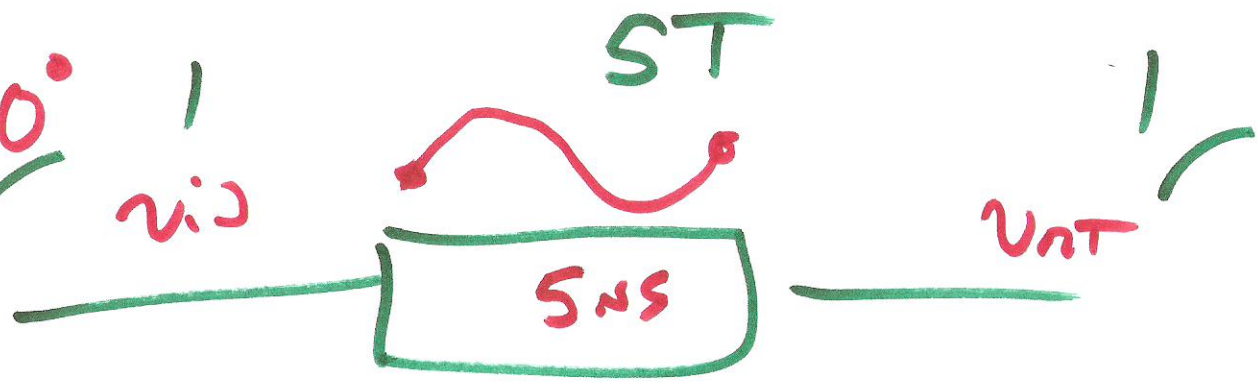
1)



$\angle \frac{v_{out}}{v_{in}} \rightarrow \text{deg}$

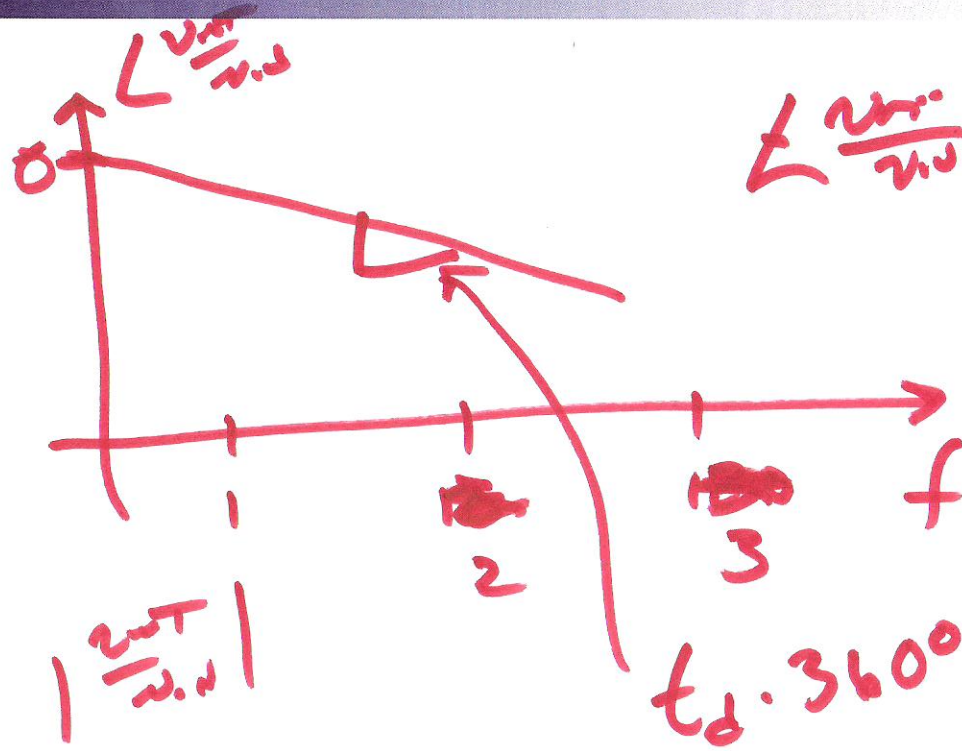
$\theta = \frac{t_d}{T} \cdot 360^\circ$

$= t_d \cdot f \cdot 360^\circ$



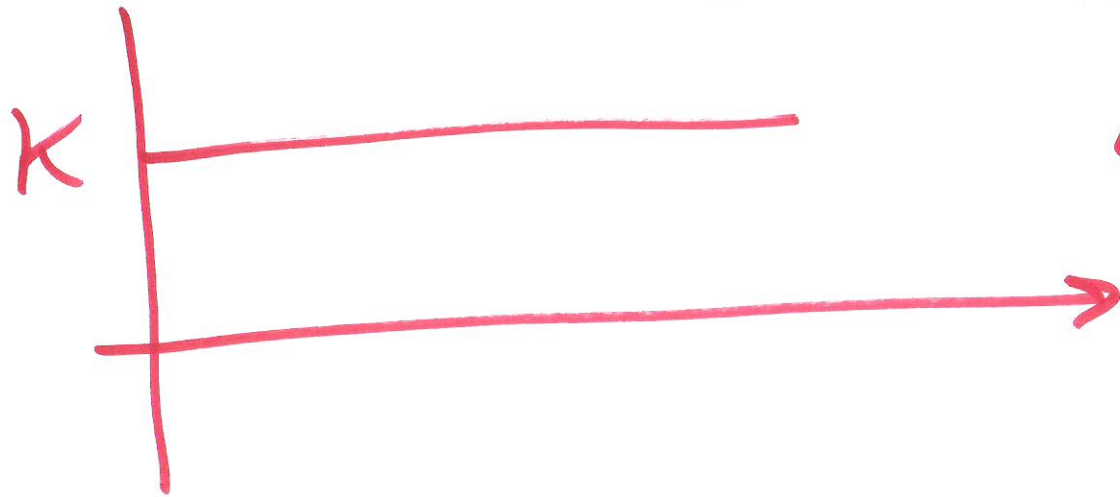
$\angle \frac{v_{out}}{v_{in}} = - \frac{5N}{t_d} \cdot f \cdot 360^\circ$

2)



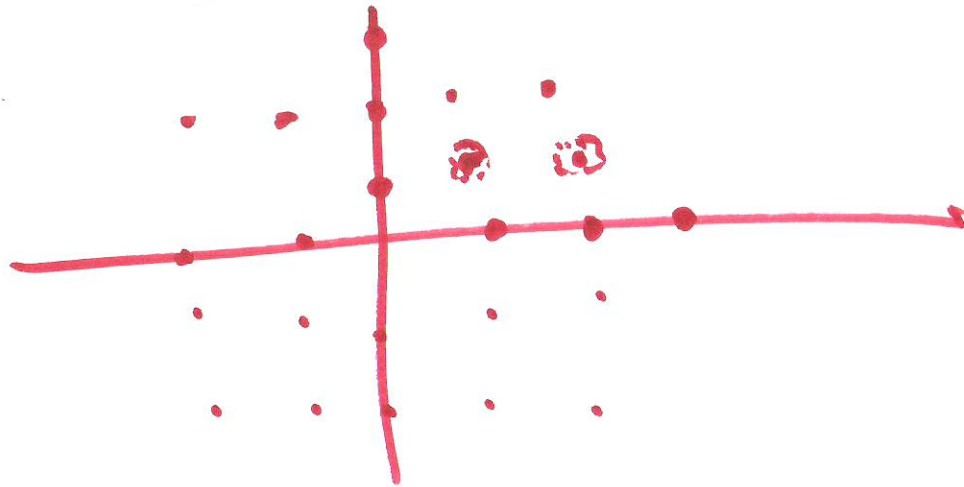
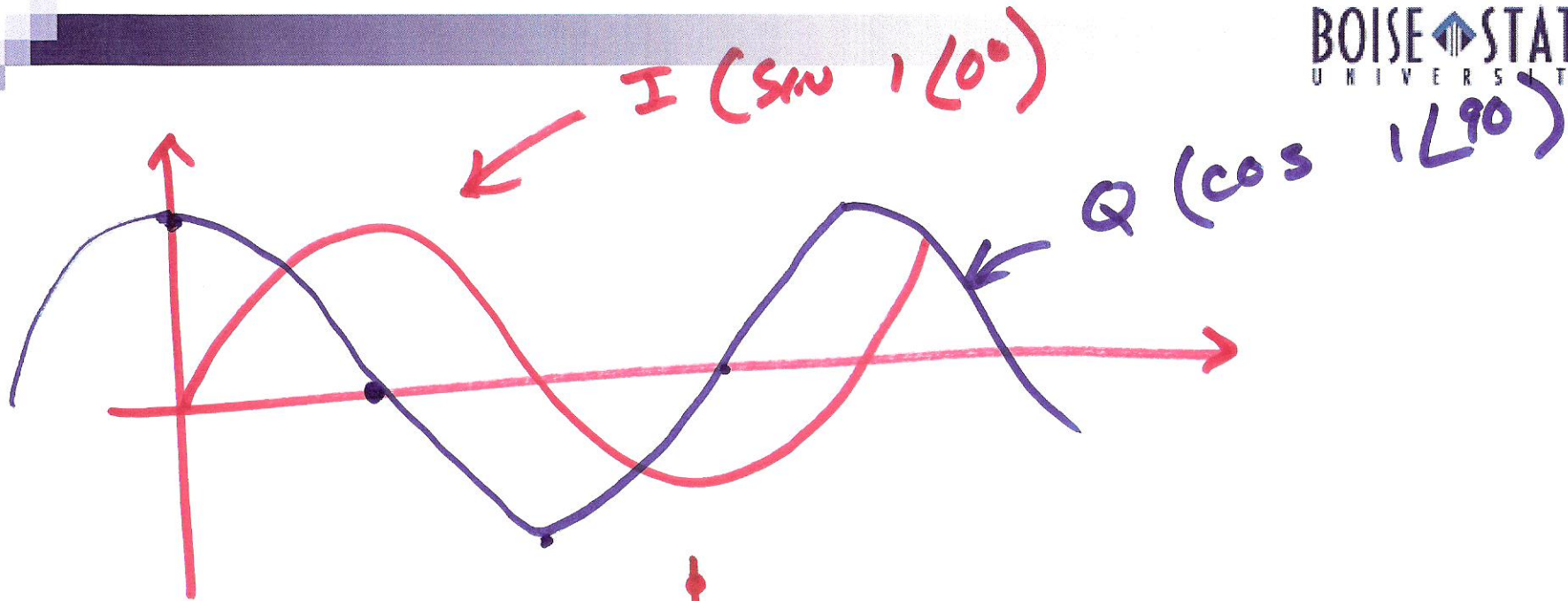
$$L \frac{\text{deg}}{\text{rad}} = -t_d \cdot f \cdot 360^\circ$$

$$= -\frac{t_d}{T} \cdot 360^\circ$$



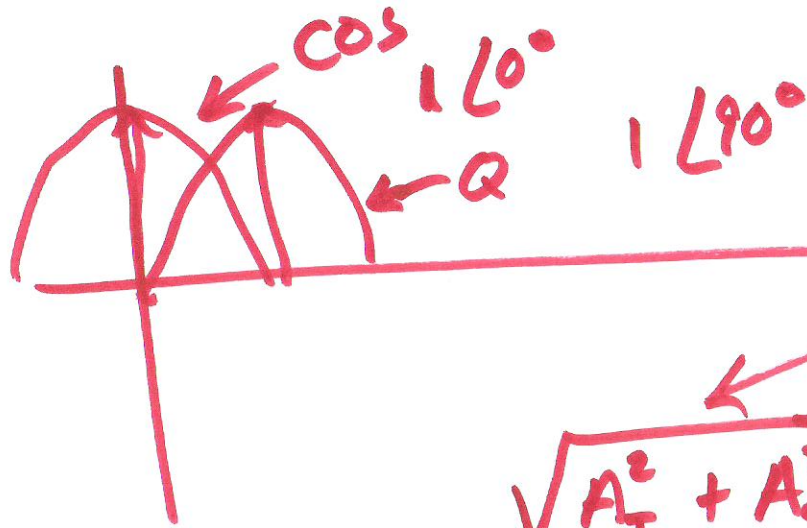
CONSTANT $\left(\frac{\text{mag}}{\text{rad}}\right)$
 Linear
 phase L

3)

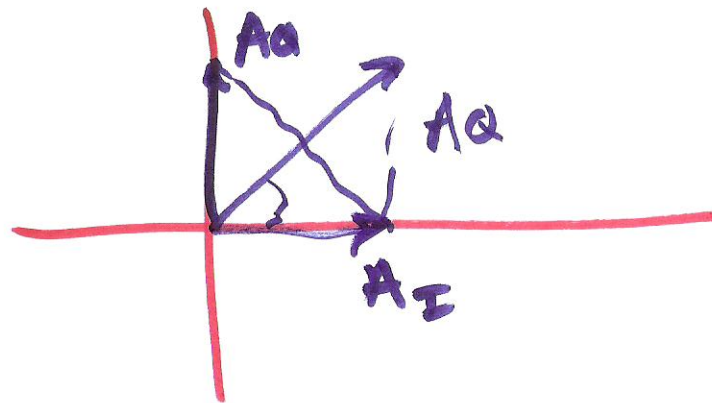


4)

$$S_{IQ}(t) = A_I \cos 2\pi f_0 \cdot t + A_Q \sin 2\pi f_0 \cdot t$$

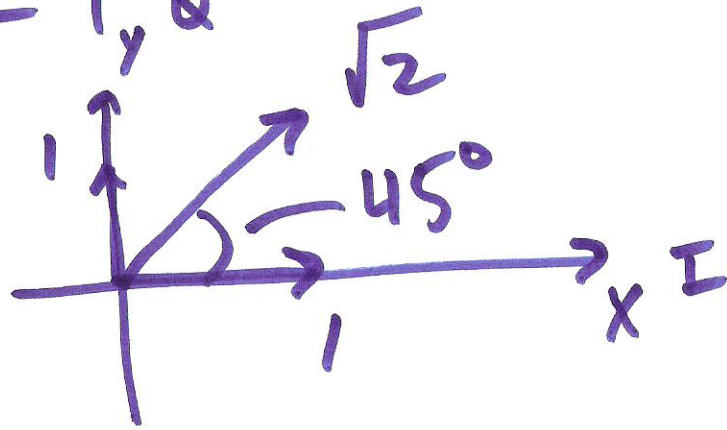


$$\sqrt{A_I^2 + A_Q^2} \cos\left(2\pi f_0 \cdot t + \tan^{-1} \frac{A_Q}{A_I}\right)$$

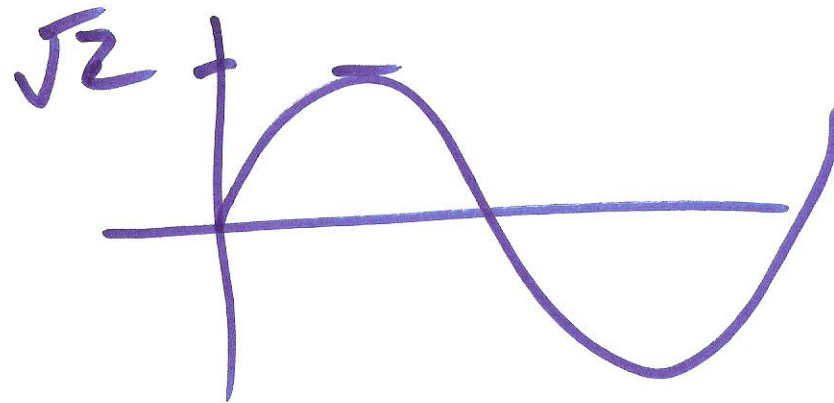


5)

$$A_a = A_I = 1, \theta$$



$$\sqrt{2} \cos(2\pi f \cdot t + 45^\circ)$$



6)

$$e^k = 1 + k + \frac{k^2}{2!} + \frac{k^3}{3!} + \frac{k^4}{4!} + \dots$$

$$\cos k = 1 - \frac{k^2}{2!} + \frac{k^4}{4!} - \frac{k^6}{6!} + \dots$$

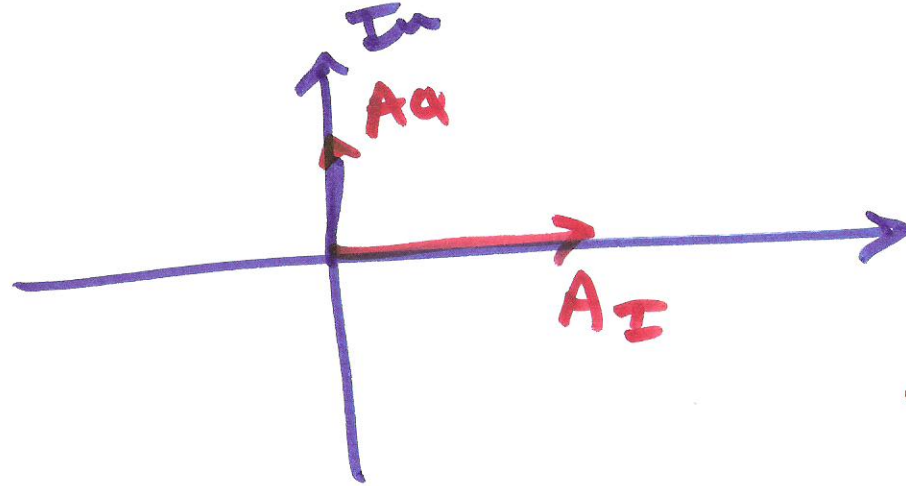
$$j \sin k = jk - \frac{k^3}{3!}j + \frac{k^5}{5!}j - \frac{k^7}{7!} + \dots$$

$j = i = \sqrt{-1}$

$$e^{jk} = 1 + jk + \frac{k^2}{2!} + \frac{-jk^3}{3!} + \frac{k^4}{4!} + \frac{jk^5}{5!}$$

7)

$$e^{jk} = \underbrace{A \cos k}_I + j \cdot \underbrace{A \sin k}_{Q \text{ Im}}$$



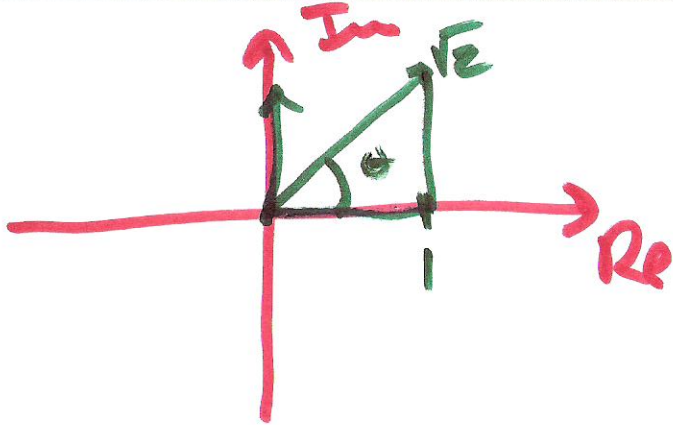
$$90 = \frac{t_d}{T} \cdot 360$$



$$\angle \theta = t_d \cdot f \cdot 360$$

$$\angle A n^{-1}$$

8)



$$A_I \cos 2\pi f t + A_Q \sin 2\pi f t$$

$$\theta = \tan^{-1} \frac{I_{Im}}{I_{Re}} \quad e^{jk} = \underbrace{\cos k}_{Re} + j \underbrace{\sin k}_{Im}$$

$$\theta = \tan^{-1} \frac{\sin k}{\cos k} = k$$

$$k = 2\pi f \cdot t$$

9)



$$e^{j\theta} \leftarrow \theta = -2\pi \cdot \frac{t_d}{T} \equiv 2\pi \cdot t_d \cdot f$$

$$= \cos \theta + j \sin \theta$$

$$= \sqrt{\cos^2 \theta + \sin^2 \theta}$$

$$\angle \tan^{-1} \frac{\sin \theta}{\cos \theta}$$

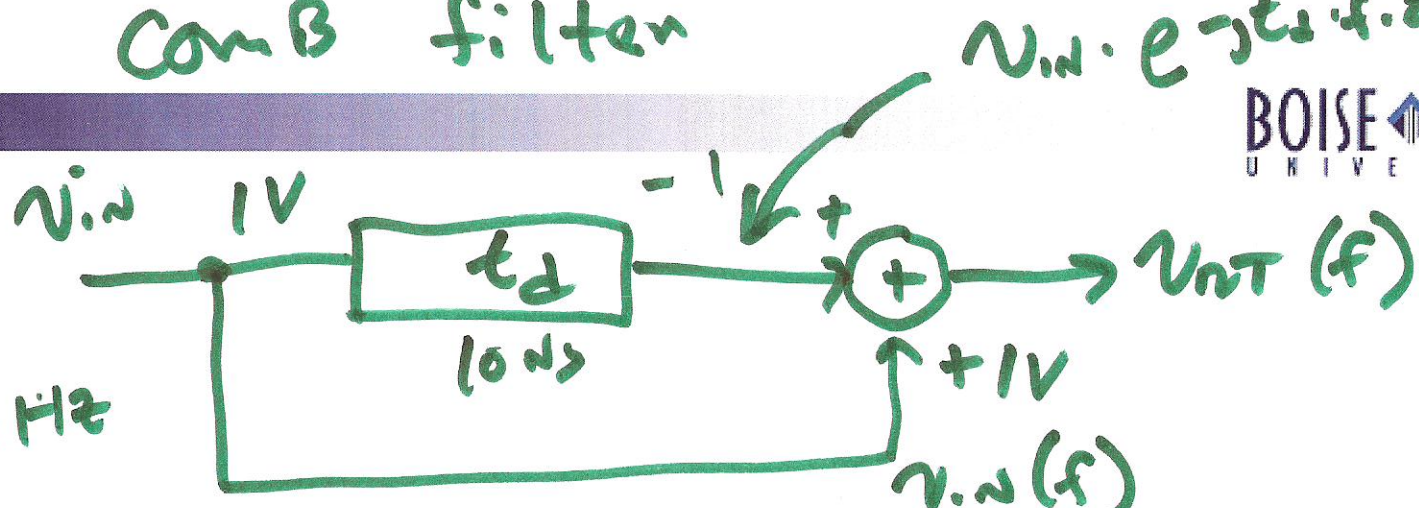
$$= \sqrt{1} \angle \theta$$

$$e^{-j2\pi \cdot \frac{t_d}{T}} = 1 \angle \theta$$

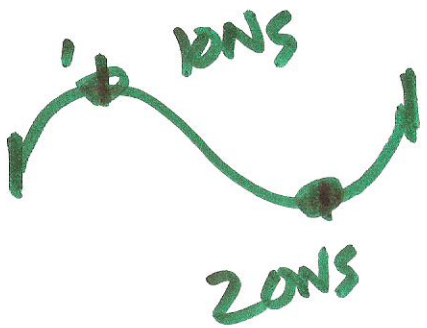
$$= e^{j\theta}$$

10)

COMB filter



$f = 50\text{MHz}$



$$v_{out} = v_{in} + v_{in} \cdot e^{-j2\pi f t}$$

$$\frac{v_{out}}{v_{in}} = 1 + e^{-j2\pi f t}$$

Re + Im

$$= \underbrace{1 + \cos(2\pi f t)}_{\text{Re}} +$$

$$j \sin(-2\pi f t)$$

11)

$$\left| \frac{v_{out}}{v_{in}} \right| = \sqrt{(1 + \cos(2\pi ft))^2 + \sin^2(2\pi ft)}$$

$$\angle = \frac{\sin(-2\pi ft)}{1 + \cos(-2\pi ft)}$$

$$1 + \cos x = 2 \cos^2 \frac{x}{2}$$

$$\sin x = 2 \sin \frac{x}{2} \cos \frac{x}{2}$$

$$\left| \frac{v_{out}}{v_{in}} \right| = 2 |\cos \pi f \cdot t_d|$$

$$\angle \frac{v_{out}}{v_{in}} = \pi(-t_d) \cdot f$$

$$f < \frac{1}{2t_d}$$

12)