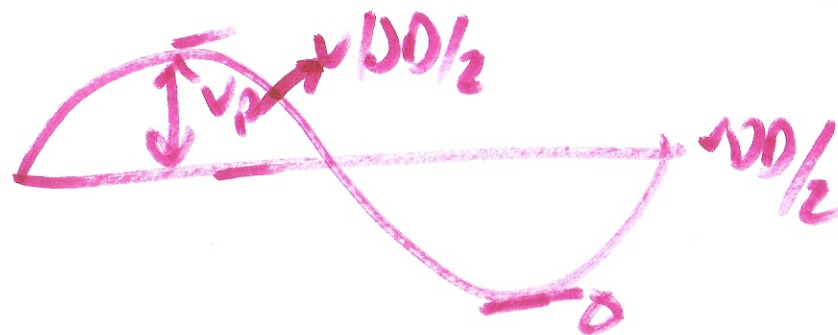


Lecture 17 OCT. 20,

SNR in data converters 2010

$$V_{Q2, RMS} = \frac{V_{LSB}}{\sqrt{12}} = \frac{V_{REF+} - V_{REF-}}{2^N \cdot \sqrt{12}}$$

$$SNR_{Data} = 20 \log \frac{V_P / \sqrt{2}}{\frac{V_{LSB}}{\sqrt{12}}} = 6.02N + 1.76 \text{ dB}$$



$$V_P = \frac{V_{DD}}{2}$$

$$V_{LSB} = \frac{V_{DD}}{2^N}$$

$$SNR_{ideal} = 6.02N + 1.76$$

Effective # of bits =

$$N_{eff} = \frac{SNR_{meas} - 1.76}{6.02}$$

Example 5.3

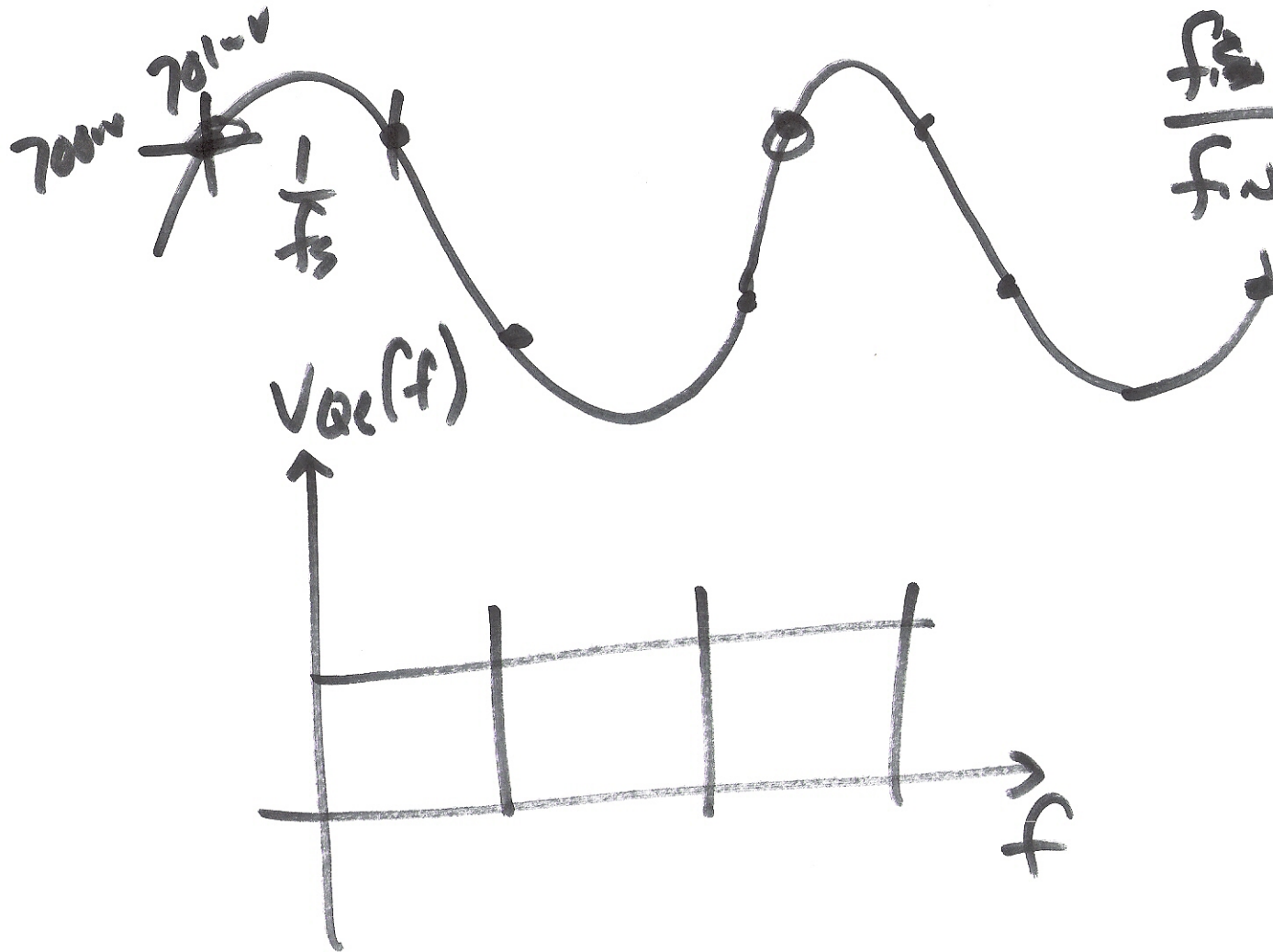
$$SNR = 20 \log \frac{0.5/\sqrt{2}}{2^{-v}} \approx 45 \text{ dB}$$

$v_{REF} = 1$
 $v_{RE} = 0$
 $v_p = 0.5$

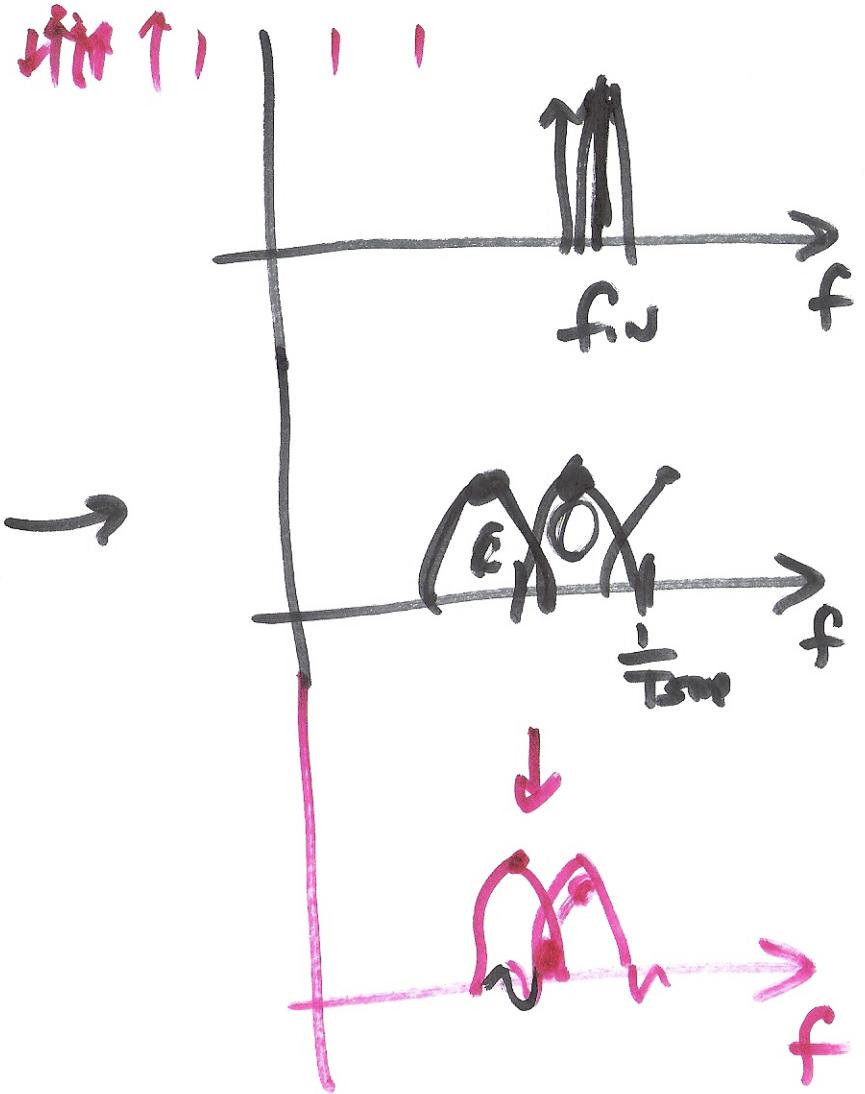
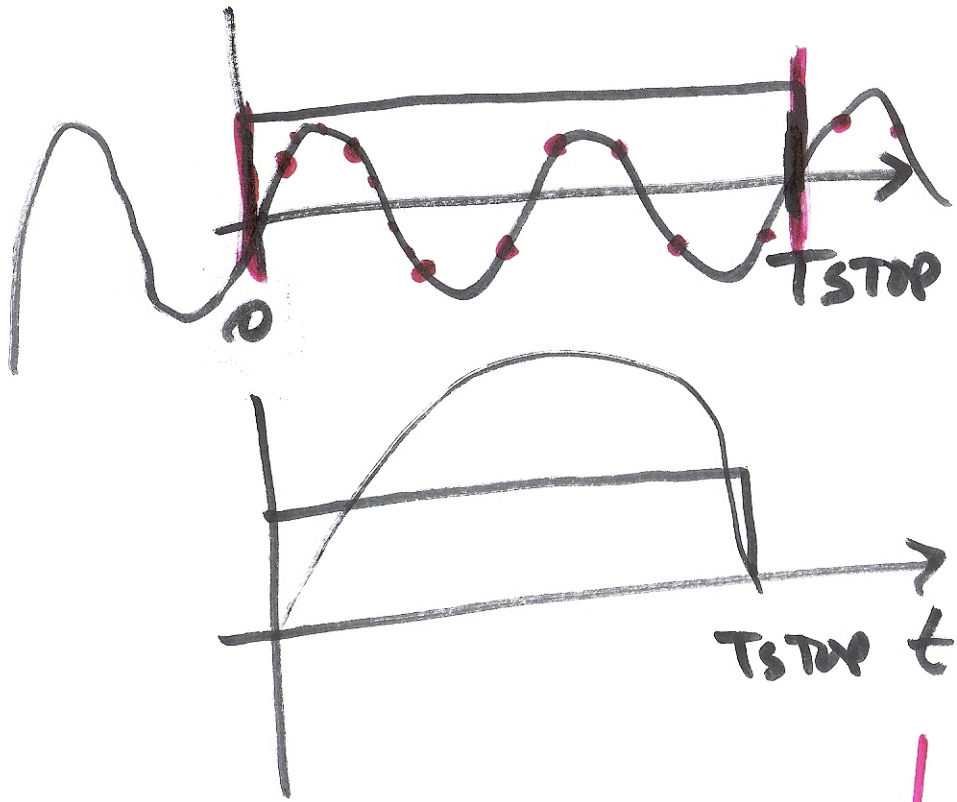
$$N_{eff} = \frac{45 - 1.76}{6.02} = 7.18 \text{ bits}$$

2)

Coherent Sampling



3)



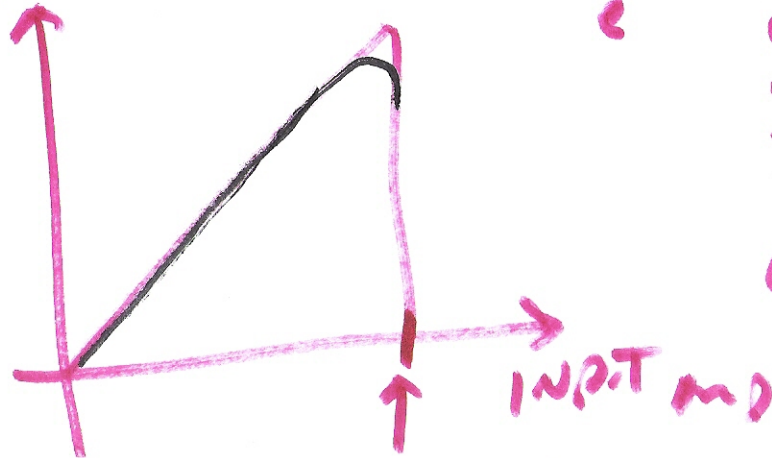
4)

$$SNOR = 20 \log \frac{0.5/\sqrt{2}}{22.7 \mu V} = 24 \text{ dB}$$

$$N_{\text{eff}} = \frac{24 - 1.7}{6} = \underline{\underline{3.7 \text{ b.t.s.}}}$$

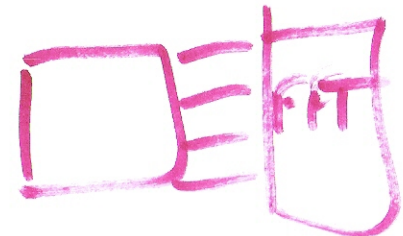
$$\text{SINAD} = \text{SNOR}$$

SNR, SNOR



full scale

SINAD
SINAD
SINAD
SINAD
SINAD
SINAD
SINAD
SINAD
SINAD
SINAD



SNOR
SNR_{meas.}

$$SNR = 6.02N + 1.76$$

5)

DYNAMIC RANGE

$$DR = \frac{V_{REF+} - \left(\frac{V_{REF+} - V_{REF-}}{2^N} \right) - V_{REF-}}{\frac{V_{REF+} - V_{REF-}}{2^N}}$$

$$= \frac{1 - \frac{1}{2^N}}{\frac{1}{2^N}} = (2^N - 1) \approx 2^N$$

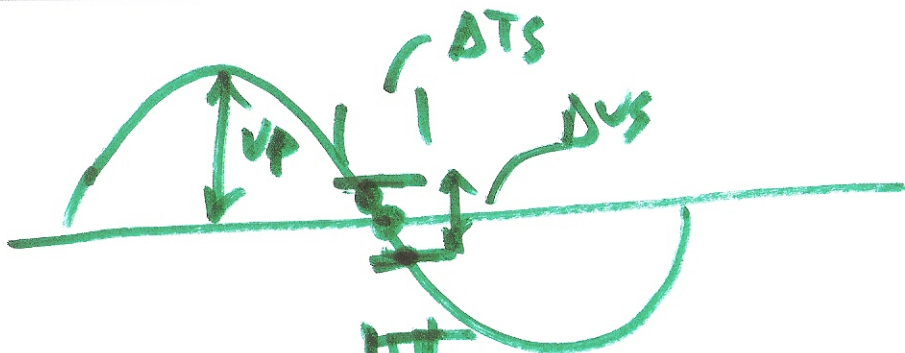
$$DR = 20 \log 2^N = 6.02 N$$

Another is to say when does SNR → 0 dB

DR → SNOR 60 dB

6)

Clock jitter



$$\text{stability} = \frac{\Delta T_s}{T_s}$$

10 ppm
 \downarrow
 10^{-6}

$$\Delta T_s \frac{dV_p}{dt} \sin\left(2\pi \frac{f_s}{2} \cdot t\right)$$

$$\frac{\pi}{V_{DD}} \cdot \frac{V_{DD}}{2^{N+1}}$$

$$= V_p \cdot \pi \cdot f_s \cdot \cos(\pi f_s \cdot t)$$

$$V_p \cdot \pi \cdot f_s =$$

$$\frac{\Delta V_s}{\Delta T_s}$$

$$\frac{1}{2} V_p = \frac{V_{DD}}{2}$$

$$1 \text{ LSB} = \frac{V_{DD}}{2^N}$$

peak to peak jitter

$$\Delta T_s \leq \frac{1}{2^N} \cdot \frac{1}{\pi f_s}$$

→

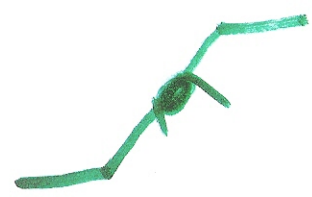


$$\Delta T_s \geq \frac{1}{2^n} \cdot \frac{1}{2\pi f_{in}}$$

↑
reduces SNR > 0.5 bits

$$\Delta T_s = \frac{1}{2^{n-N_{loss}}} \cdot \frac{1}{2\pi f_{in}}$$

$$SNR = 6.02 \left(\underbrace{N - N_{loss} - 0.5}_{N_{eff}} \right) + 1.76 \text{ dB}$$



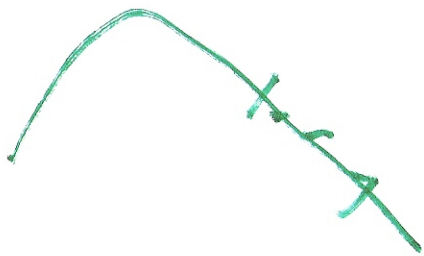
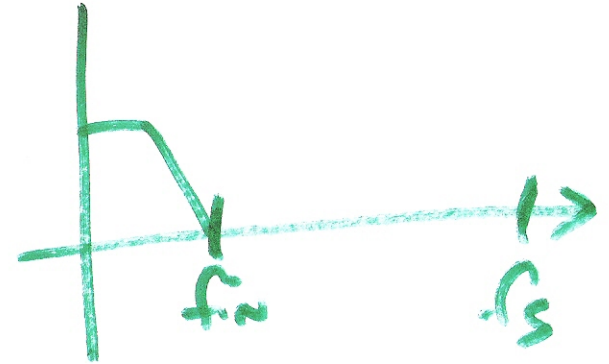
N_{eff} → due to clock jitter

8)

over-sampling

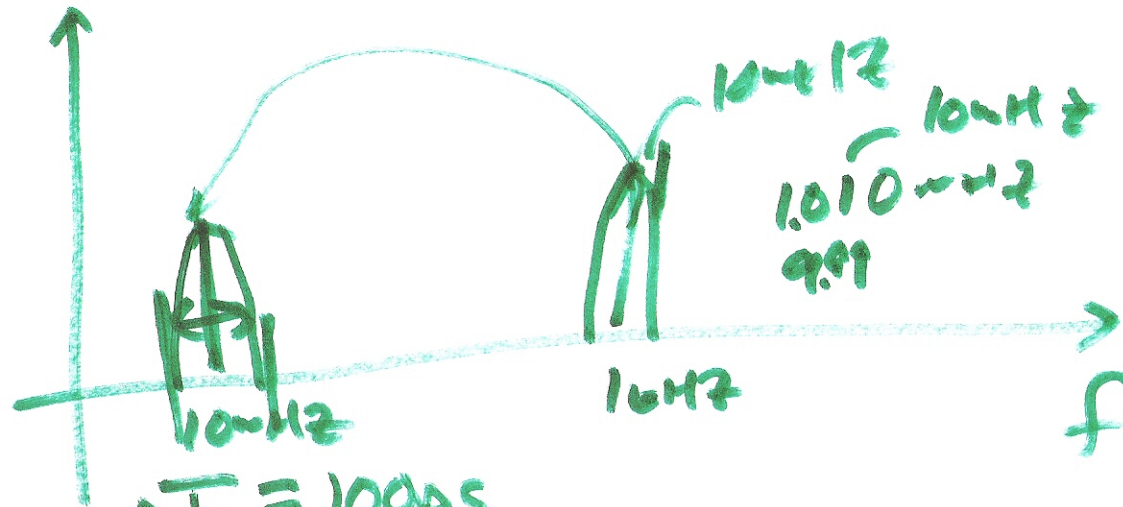
$$\frac{f_s}{2} = K \cdot f_{in}$$

↑
max



~~Eq~~
 new stability, $p_{an} =$
 old, $p_{an} \cdot K$

Clock signal



$\Delta T_s = 100 \text{ ps}$
 10 ns

10
 99.9 ns
 100.1

10.
 10.01 MHz
 9.99 MHz

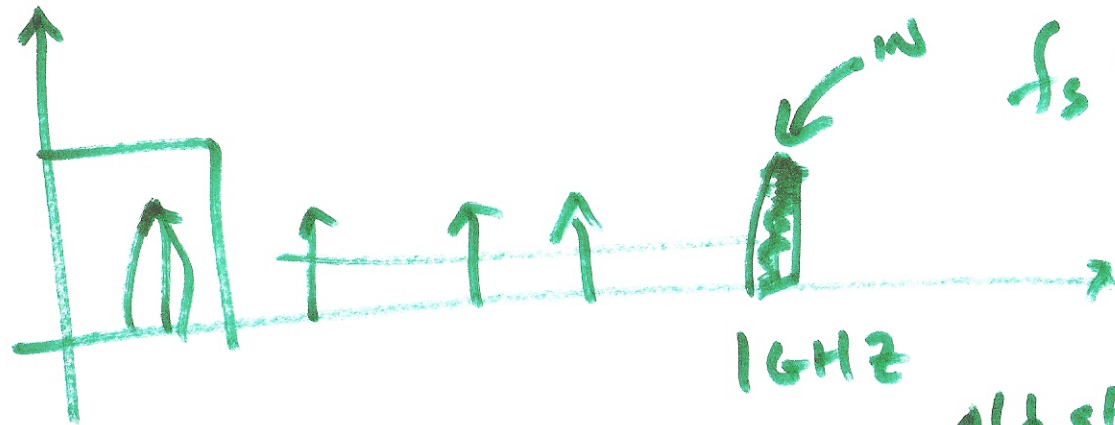
1
 1 ns
 $\Delta T_s = 1 \text{ ps}$

$|100 \text{ ps}|$

$1,000 \text{ ppm}$
 $= 0.1\%$
 $= 0.001$

$1 \text{ ns} \pm 1 \text{ ps}$
 $10 \text{ MHz} \pm 100 \text{ ps}$

10)



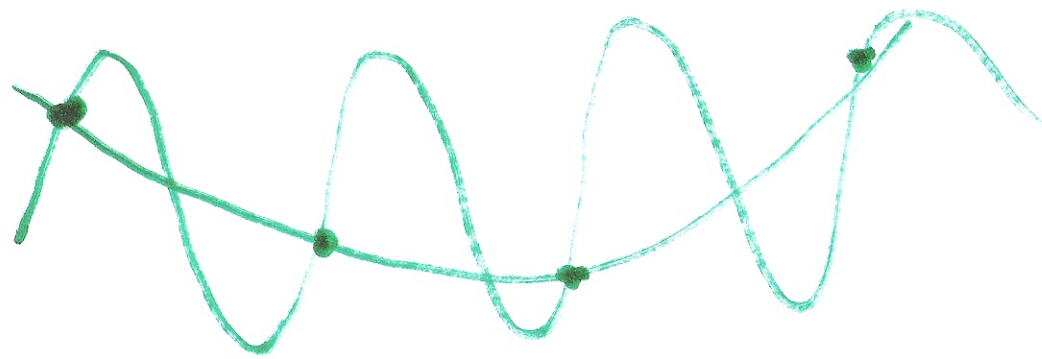
$$f_s = 100 \text{ MHz}$$

$$\frac{\text{old stability}}{K} = \text{new, stability}$$

8

$$\frac{1000 \text{ ppm}}{8}$$

$$\underline{\underline{125 \text{ fs}}}$$



~~fs~~

11)