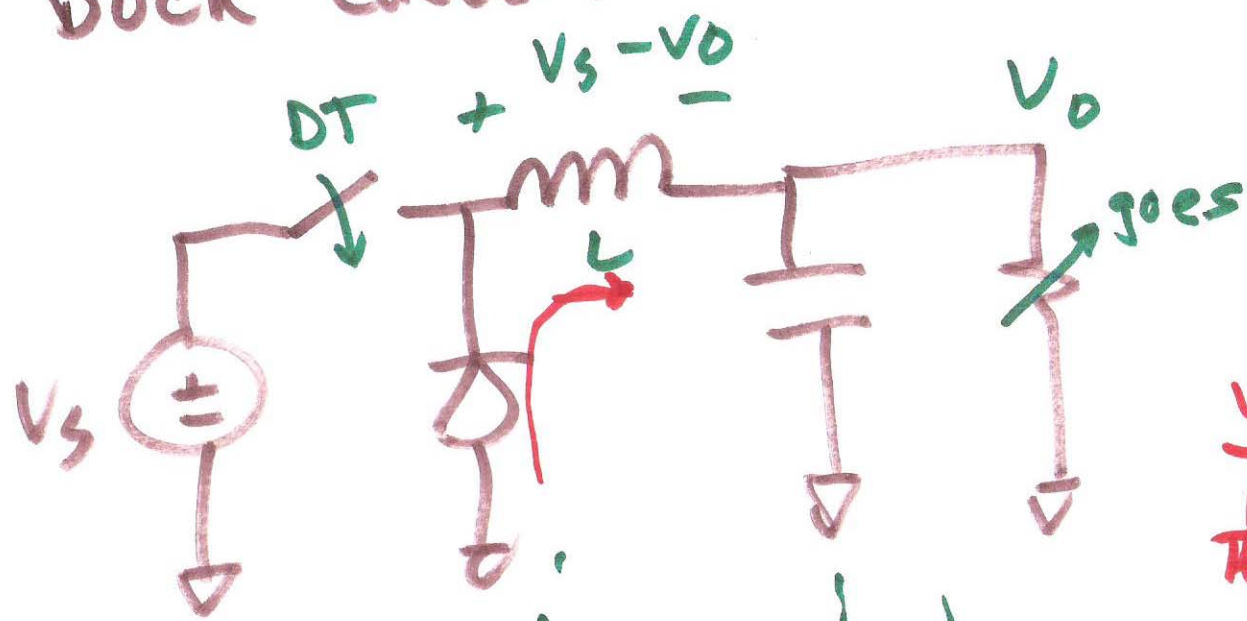


Lecture 9

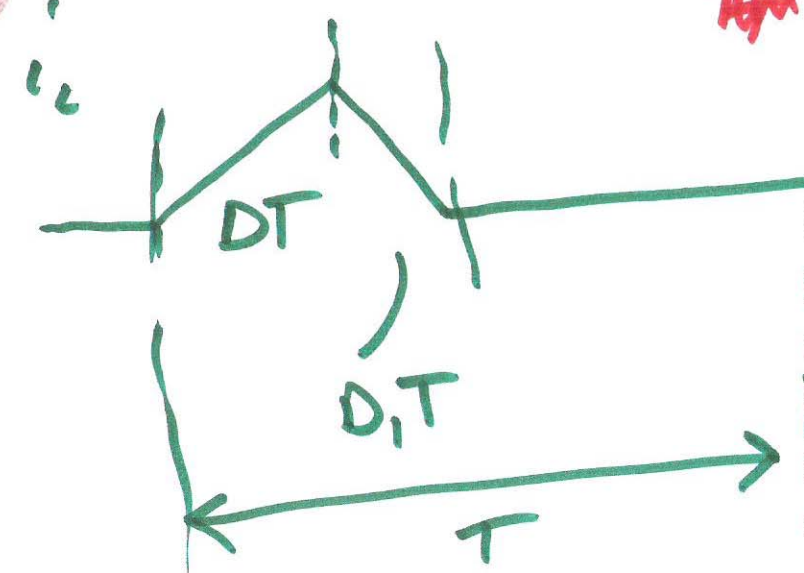
Sept. 20, 2011

Buck converter



$$V = L \frac{di}{dt}$$

$$\Delta i_L = DT \cdot \frac{(V_s - V_o)}{L}$$

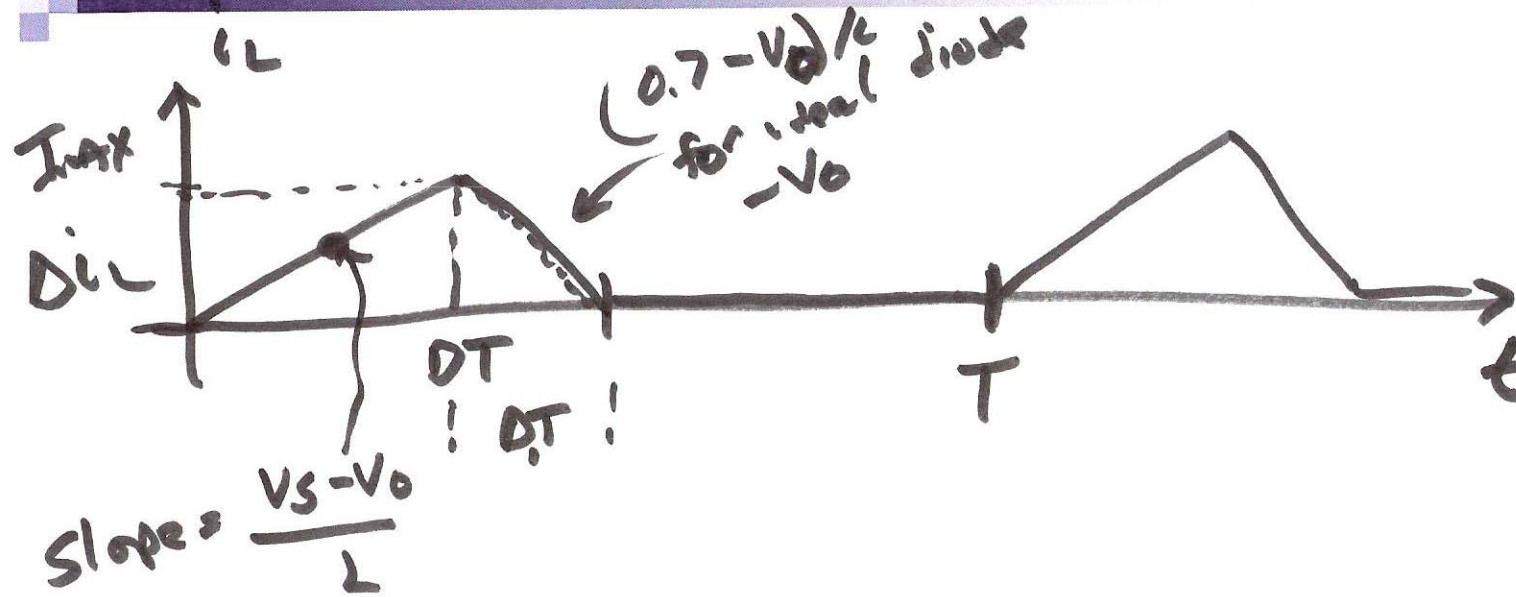


$$\frac{V_o^2}{R} = P_o$$

$$W = J/s$$

$$\frac{V_o^2}{R} \cdot T$$

$$\frac{V_o^2}{R} T$$



$$\frac{V_s - V_o}{L} \cdot DT + D_1 T \frac{D - V_o}{L} = 0$$

$$(V_s - V_o) D = D_1 V_o$$

$$V_o = V_s \cdot \frac{D}{D + D_1}$$

2)

Load current

$$\frac{V_O}{R} = I_R = I_L$$

$$\frac{V_O}{R} = \frac{1}{T} \left(\frac{I_{MAX}}{2} \cdot DT + \frac{I_{MAX}}{2} \cdot D_1 T \right)$$



$$= \frac{1}{2} I_{MAX} (D + D_1) = \frac{V_O}{R}$$

Switch closed $\rightarrow I_{MAX} = \frac{V_S - V_O}{L} \cdot DT \rightarrow \frac{V}{L} = \frac{di}{dT} = \frac{\Delta I_{MAX}}{DT}$

Switch open $\rightarrow -I_{MAX} = \frac{-V_O}{L} \cdot D_1 T$

$$\frac{V_O}{R} = \frac{1}{2} \frac{V_O D_1 T}{L} (D + D_1)$$

3)

$$\frac{V_0}{R} = \frac{1}{2L} V_0 T (D_1 D + D_1^2)$$

$$T \frac{D_1^2}{2L} + \frac{D_1 D T}{2L} - \frac{1}{R} = 0$$

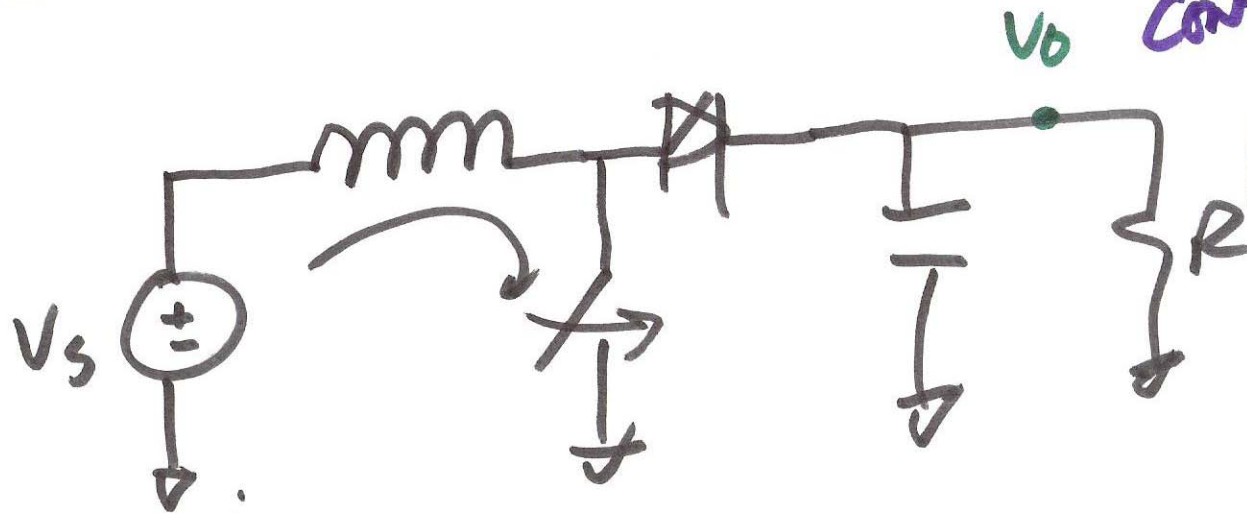
$$D_1^2 + D_1 D - \frac{2L}{RT} = 0$$

$$D_1 = \frac{-D \pm \sqrt{D^2 + 4 \frac{2L}{RT}}}{2}$$

$$V_0 = V_s \cdot \frac{D}{D + D_1} = V_s \left[\frac{2D}{D + \sqrt{D^2 + 8L/RT}} \right]$$

4)

BOOST DISCONTINUOUS



Continuous current

$$\frac{\Delta i_L \uparrow I_{max}}{DT} = \frac{V_s - 0}{L}$$

$$\frac{\Delta i_L \downarrow - I_{max}}{(1-D)T} = \frac{V_s - V_o}{L}$$



$$\frac{DT \cdot V_s}{L} = \frac{(V_o - V_s) \cdot D_1 T}{L}$$

$$V_o = V_s \left(\frac{D + D_1}{D_1} \right)$$

No. Inductor current $I_{max} = DT \cdot \frac{V_s}{L}$

$$L = \frac{V_s^2 V_o}{R} = \frac{1}{T} \left(\frac{DT \cdot V_s}{2L} + \frac{V_o - V_s \cdot D_1 T}{2L R} \right)$$

$$\frac{D V_s}{2L} + \frac{V_o - V_s}{2L} D_1 - \frac{V_o}{R} = 0$$

5)

$$V = L \cdot \frac{di}{dt} \quad L = \frac{V \cdot s^2}{C} \quad , \quad \frac{V}{C} = \frac{di}{dt}$$

Avg. Diode current

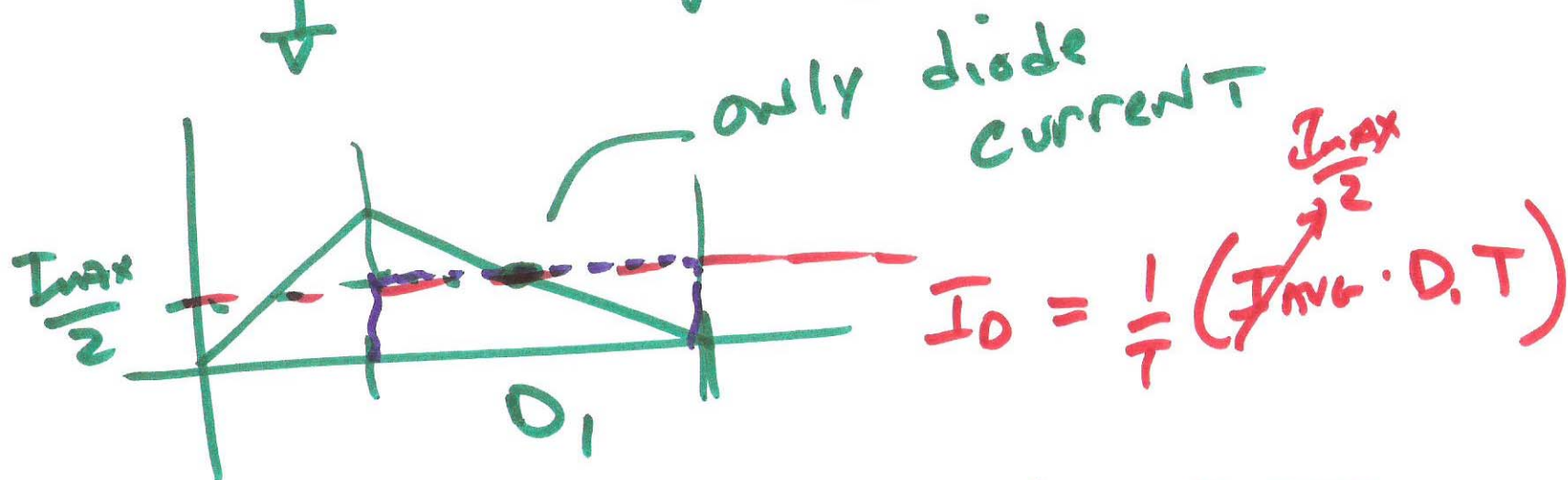
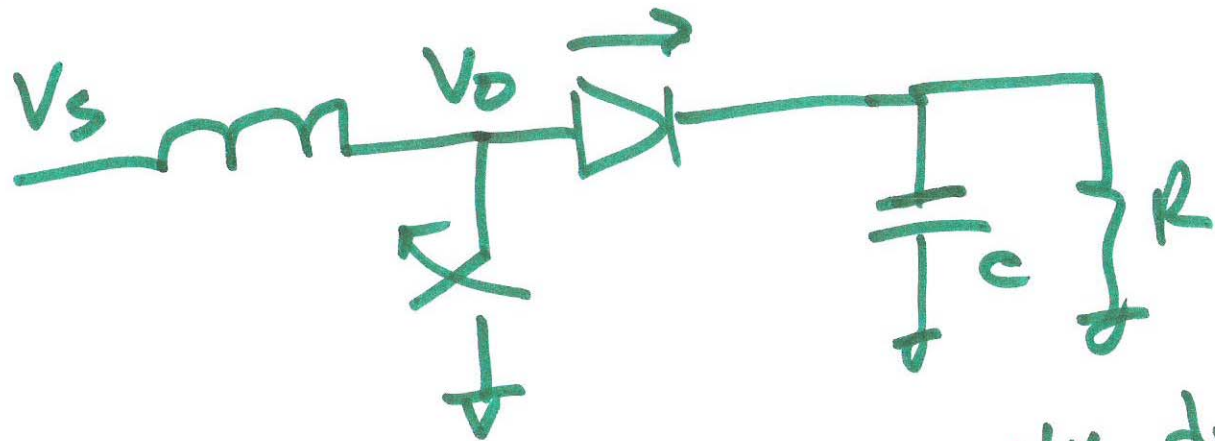
$$\frac{V_D}{R} = \frac{1}{T} \left(0 \text{ switch closed} + \frac{I_{max} \cdot \frac{V_D - V_s \cdot D_1 T}{L}}{\text{switch open}} \right)$$

$$\frac{V_D}{R} (\text{Amps}) = \frac{V_D - V_s \cdot D_1}{L} \cdot D_1$$

$\swarrow \frac{V \cdot s^2}{C}$

$$\frac{1}{T} (I_{max} \cdot D_1 T)$$

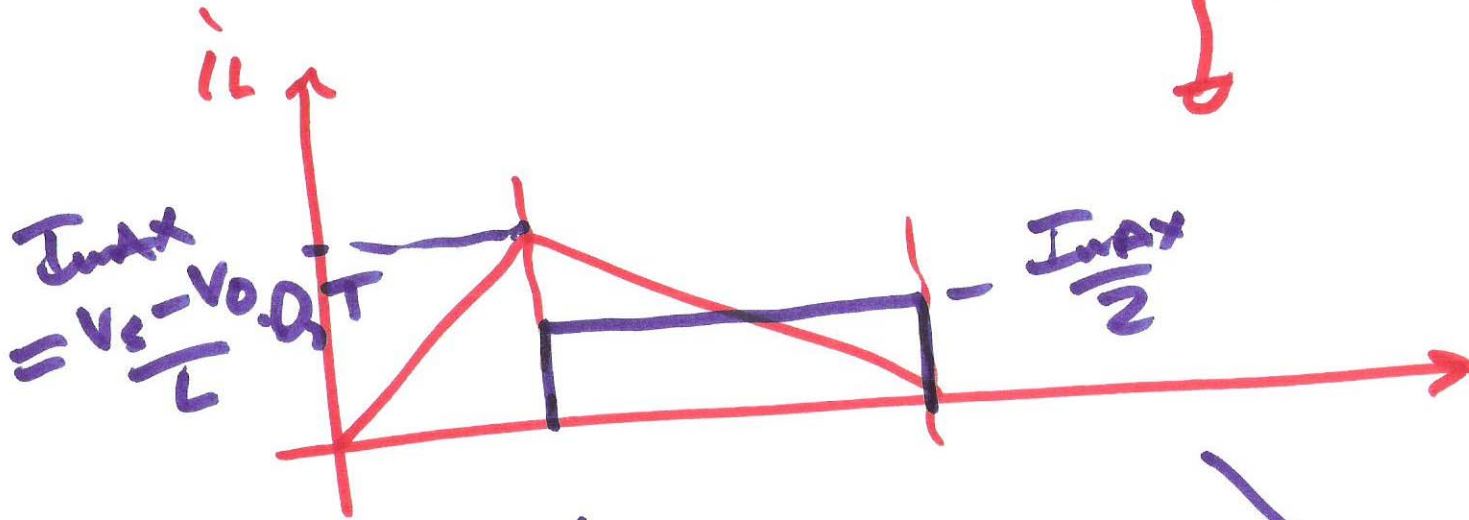
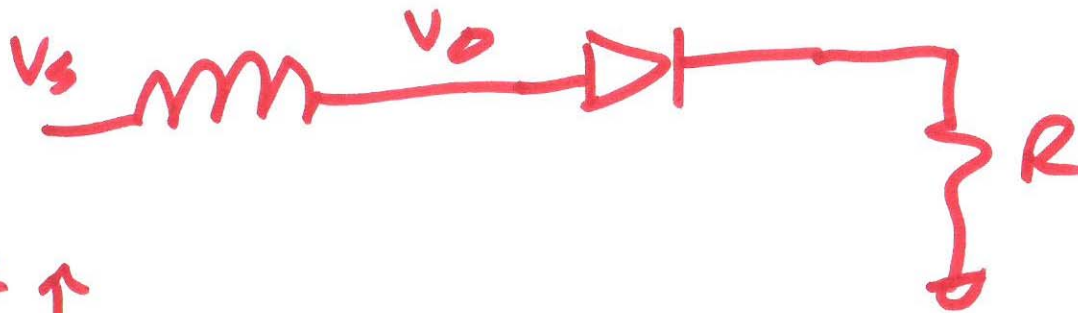
6)



$$I_{max} = \frac{V_s - V_o}{L} \cdot D \cdot T$$

$$I_0 = \frac{1}{T} \left(\frac{V_s - V_o}{L} \cdot D \cdot T \cdot \frac{1}{2} \right)$$

→



$$I_{\text{diode avg}} = \frac{1}{T} \left(\frac{V_s - V_o}{2L} \cdot D_1 T \cdot D_1 T \right) = \frac{V_s - V_o}{2L} D_1^2 T$$

$\frac{I_{max}}{2}$

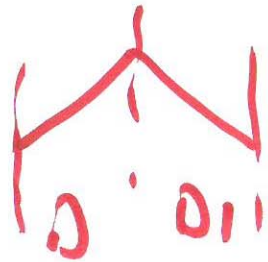
Average diode current $= \frac{I_{max}}{2} D_1$

8)

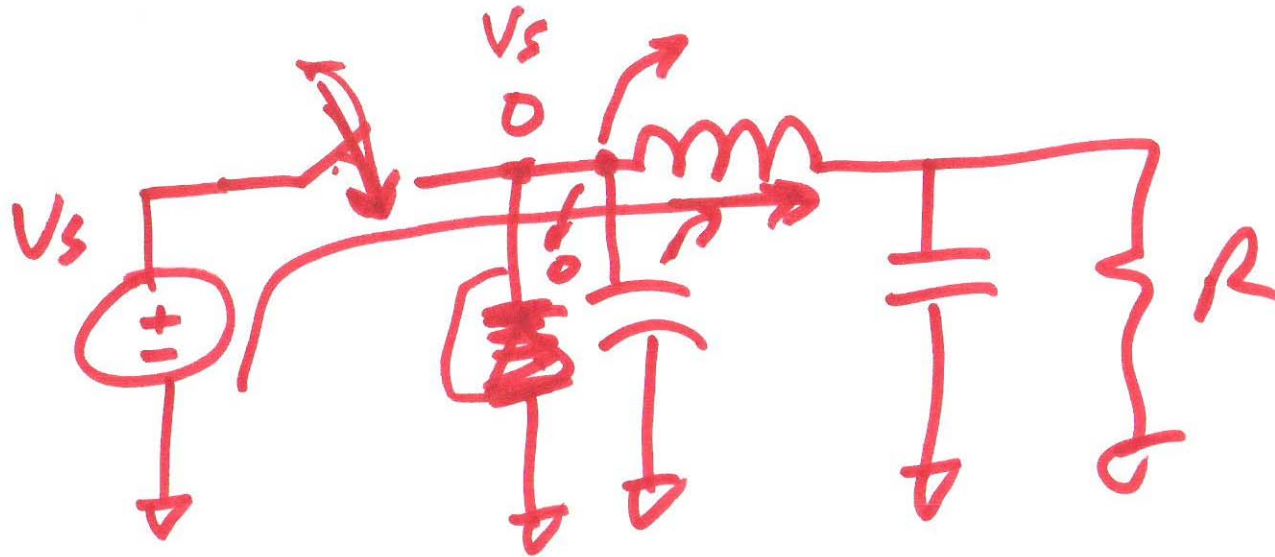
$$I_D = \frac{1}{2} \left(\frac{V_s D T}{L} \right) D_1 = \frac{V_D}{R}$$

$$D_1 = \left(\frac{V_D}{V_s} \right) \cdot \frac{2L}{RDT}$$

$$\frac{V_D}{V_s} = \frac{1}{2} \left(1 + \sqrt{1 + \frac{2D^2 RT}{L}} \right)$$



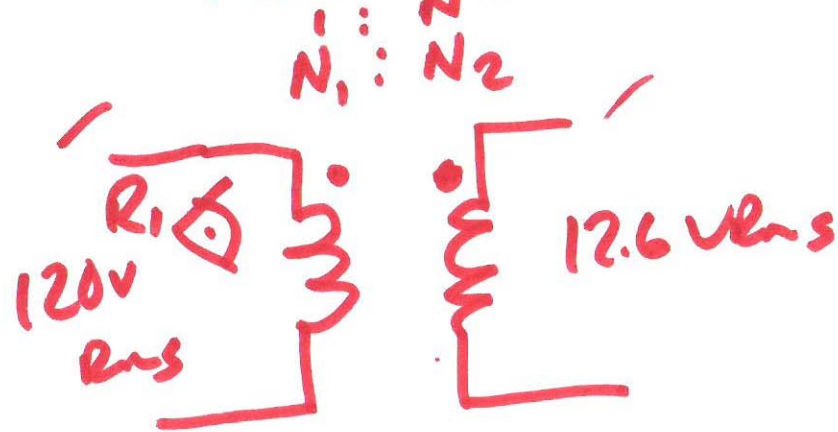
RESONANT



zero-voltage switching

10)

Modeling Xformers



$$\frac{V_1}{I_1} = \frac{V_2}{I_2} \cdot \frac{N_1^2}{N_2^2} = \frac{V_2}{I_2} \cdot \frac{1}{N^2}$$

$$\frac{V_1}{V_2} = \frac{N_1}{N_2} = \sqrt{\frac{L_1}{L_2}} = \frac{1}{N}$$

Inductance of the primary = 1mH

$$\frac{120}{12.6} = 9.52 = \sqrt{\frac{1\text{mH}}{L_2}} = \frac{1\text{mH}}{9.52^2}$$

$$L_2 = 114\text{H}$$

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